Supply Chain Disruptions, the Structure of Production Networks, and the Impact of Globalization

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BUSINESS

Tesla to Halt Production in Germany as Red Sea Conflict Hits Supply Chains

Disruption related to attacks on ships by Houthi rebels raise risk of supply-chain crisis in Europe

By William Boston Follow, Costas Paris Follow and Benoit Faucon Follow Updated Jan. 12, 2024 1:45 pm ET

BERLIN—Tesla TSLA -3.67% ▼ plans to halt production at its only large factory in Europe for two weeks because of a lack of parts, a sign of how the fallout from recent attacks on ships in the Red Sea is starting to ripple through the global economy.

Yemen-based, Iran-backed Houthi fighters have launched successive attacks on



Tractable model of (global, complex) supply chains to:

- characterize short-run impact of a shock,
- contrast with long-run impact,
- investigate how impacts depend on network/complexity,
- examine impact of globalization on fragility.

Some Related Literature

- Foundational work: Leontief (1936), Long Jr and Plosser (1983), Acemoglu et al. (2012)
- **Surveys:** Bernard (2018), Carvalho and Tahbaz-Salehi (2019), Baqaee and Rubbo (2022), Antràs and Chor (2022), Elliott and Golub (2022), Baldwin and Freeman (2022).
- Production networks: e.g., Dhyne et al. (2015); Magerman et al. (2016); Brummitt et al. (2017); Baqaee (2018); Oberfield (2018); Acemoglu and Tahbaz-Salehi (2020), Acemoglu and Azar (2020), Baqaee and Farhi (2021), Kopytov et al. (2021), Di Giovanni et al. (2022); Bernard et al. (2022), Elliott et al. (2022), Bui et al. (2022), König et al. (2022), Pellet and Tahbaz-Salehi (2023), Grossman et al. (forthcoming), Grossman et al. (2023a), Grossman et al. (2023b)
- Trade networks: e.g., Furusawa and Konishi (2007); Chaney (2014); Bernard et al. (2019); Grossmand et al. (2021)
- Micro network structure: e.g., Bimpikis et al. (2018), Bimpikis et al. (2019), Amelkin and Vohra (2020)







2 Model

3 The Impacts of Shocks: Contrasting Short and Long Runs

4 Complexity, Fragility, Globalization

5 The Impact in the Medium Run

Model



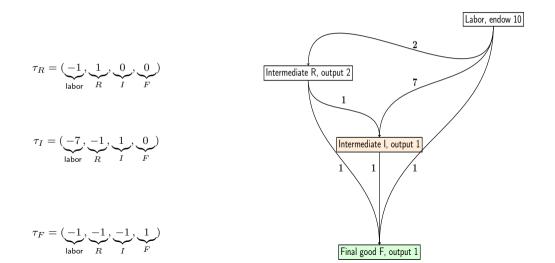
- $n \in \{1, \dots, N\}$ countries,
- $\bullet \ m \in \{1, \dots, M\}$ intermediate goods,
- $f \in \{1, \ldots, F\}$ final goods,
- L_n units of labor country n,
- T_n (finite) set technologies country n.



- $\theta_{\tau\tau'} \ge 1$ units of $O(\tau)$ shipped from τ for 1 unit to get to τ' .
- Iceberg cost on labor $\theta_{n\tau} \ge 1$.
- No iceberg costs on final goods.
- Local prices before iceberg costs $p \in \mathbb{R}^{N+|T|}_+$

Example: Technologies





Arrow-Debreu (1954) Technologies

Constant returns to scale technologies $\boldsymbol{\tau}$

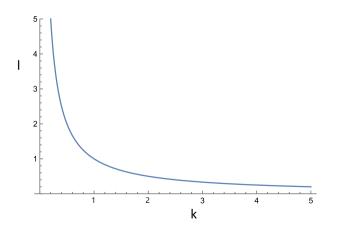
$$\begin{pmatrix} \mathsf{labor}, & \underbrace{m_1, \dots, m_M}_{\mathsf{intermediate}}, & \underbrace{f_1, \dots, f_F}_{\mathsf{final goods}} \end{pmatrix}$$

e.g., (-2, 0, -3, 0, 1): 2 units labor & 3 units m_2 make 1 unit f_2 .

Arrow-Debreu (1954) Technologies

Suppose country n can produce according to $y=L^{\alpha}K^{1-\alpha}$

Then $T_n = \{(-l, -k, 1) : l^{\alpha}k^{1-\alpha} = 1\}$

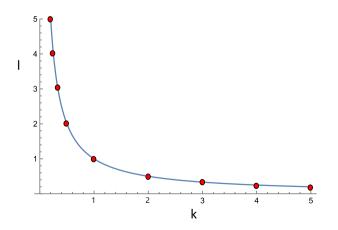




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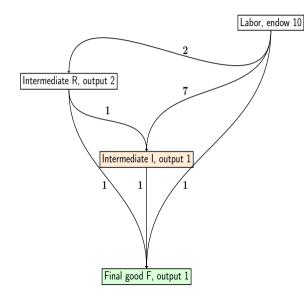
Equilibrium



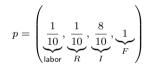
- Laborers/Consumers
 - supply labor inelastically, L_n in country n;
 - maximize homothetic preferences for final goods, $U(c_1, \ldots, c_F)$.
- Producers

 - maximize profits p_τy_τ − Σ_{τ'} p_{τ'}x_{τ'τ},
 s.t feasible production: −τ_ky_τ = Σ_{τ':O(τ')=k} x_{τ'τ}/θ_τ.
- Markets clear standard Arrow-Debreu equilibrium.





Example Equilibrium

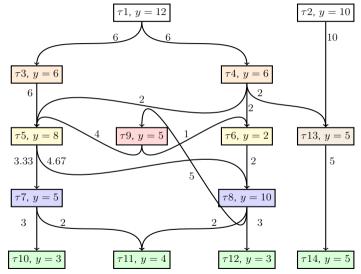


producers earn 0 profits,

markets clear,

labor buys full output

Example w Cycles (Labor Omitted, Final Goods in Green)







1 Introduction

2 Model

The Impacts of Shocks: Contrasting Short and Long Runs

4 Complexity, Fragility, Globalization

5 The Impact in the Medium Run

Impact of Shock



For τ with output k, we normalized $\tau_k = 1$.

Let's vary au_k to capture shocks/disruptions

Analyze/contrast:

- Long run: new equilibrium using shocked technologies,
- Short run: work with existing supplies/shortages.

Long-Run: Hulten's Theorem

Proposition (Hulten's Theorem)

Consider a generic equilibrium and technology $\tau,$ with $O(\tau)=k,$ used in positive amounts in equilibrium. Then

$$\frac{\partial \log(U)}{\partial \log(\tau_k)} = \frac{\partial \log(GDP)}{\partial \log(\tau_k)} = \frac{p_\tau y_\tau}{GDP}.$$

Long-Run: Hulten's Theorem

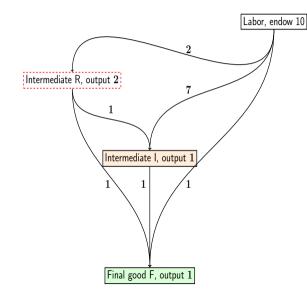
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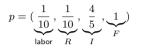
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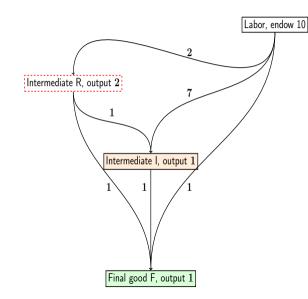
- Sufficient statistic: spending on shocked technology.
- Intuition—adjust by sourcing more inputs at the margin.
- Network matters in background as it determines equilibrium
 - but don't need to see network to estimate long-run impact.

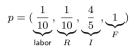










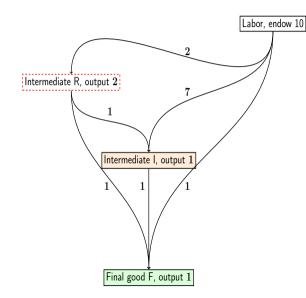


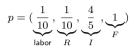
 $\begin{array}{l} p_R y_R = 1/10 * 2;\\ GDP = \sum_f p_f c_f = 1; \end{array}$

Marginal impact:

$$\frac{p_R y_R}{\mathsf{GDP}} = \frac{1}{5}$$







 $p_R y_R = 1/10 * 2;$ $GDP = \sum_f p_f c_f = 1;$

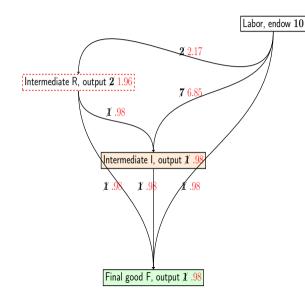
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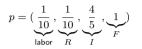
$$\frac{p_R y_R}{\mathsf{GDP}} = \frac{1}{5}$$

Extrapolating for a 10% shock, (source more)

Long Run impact: 1/50th of GDP







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Marginal impact:

$$\frac{p_R y_R}{\mathsf{GDP}} = \frac{1}{5}$$

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Long Run impact: 1/50th of GDP



"There would be a set of economists who would sit around explaining that electricity was only 4% of the economy, and so if you lost 80% of electricity, you couldn't possibly have lost more than 3% of the economy...[However,] we would understand that [...] when there wasn't any electricity, there wasn't really going to be much economy."

Short-Run Impact of a Shock

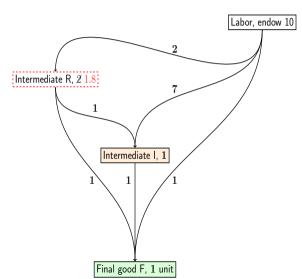


Hulten: Production is perfectly flexible and fully adjusts. (Marginal result.)

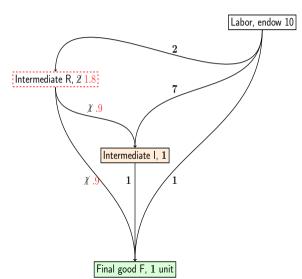
Now: Opposite benchmark with no adjustments. (Our result holds away from the margin.)

- Cannot adjust the technologies being used.
- Cannot source additional units from alternative suppliers.
- Prices cannot adjust—rationing of disrupted goods is proportional

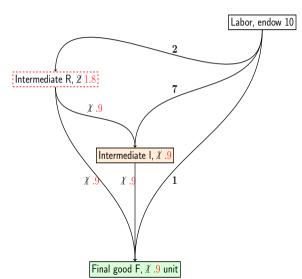






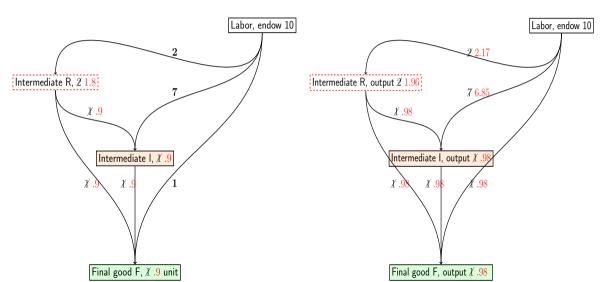


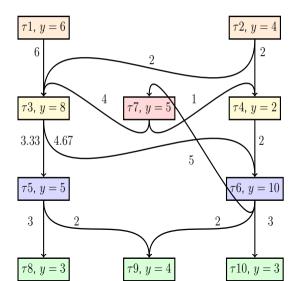




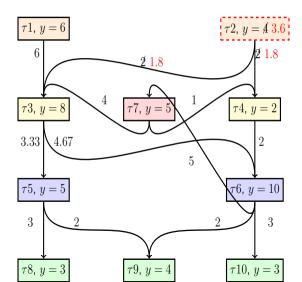


Long Run Disruption 2%

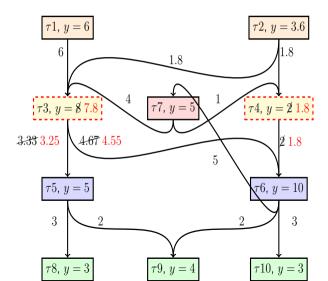




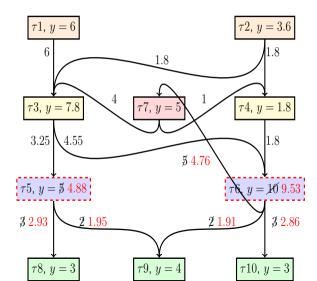




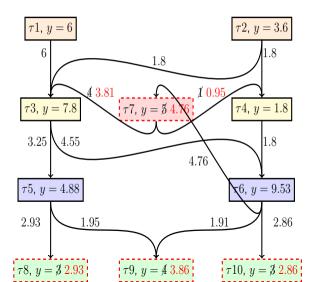




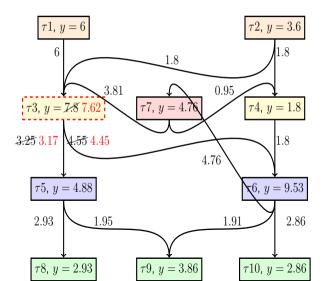




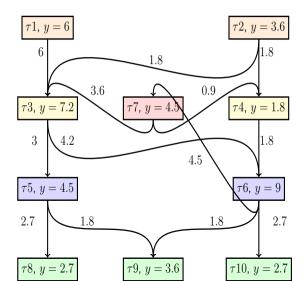














Short-Run Impact: The Minimum Disruption Problem





subject to

- **0** shock constraints: $\hat{y}_{\tau} \leq \lambda y_{\tau}$ for all $\tau \in T^{shocked}$,
- 2 technology constraints $\hat{y}_{\tau} \leq \left(\min_{\text{Inputs used by } \tau} \frac{\text{New input level}}{\text{Original input level}}\right) y_{\tau}$ for active τ ,

③ proportional rationing $\hat{x}_{\tau\tau'} = x_{\tau\tau'} \left(\frac{\hat{y}_{\tau}}{y_{\tau}}\right)$ for active $\tau'\tau$,

Inactive technologies stay inactive.

Shock Propagation Algorithm

Define an algorithm that traces shock (like example): it converges to a solution of the minimum disruption problem.

Shock Propagation Algorithm

Define an algorithm that traces shock (like example): it converges to a solution of the minimum disruption problem.

Let $F(T^{shocked})$ be the final goods on directed paths from shocked technologies.

Proposition (Upper Bound)

Consider a shock that reduces the output of technologies $\tau \in T^{shocked}$ to $\lambda < 1$ of their original levels. The proportion of lost GDP is bounded above by

$$(1-\lambda)\left(\frac{\sum_{f\in F(T^{shocked})} p_f c_f}{GDP}\right)$$

Sufficient Conditions for Bound to Bite



• All producers of given good and any "substitute" for it in a supply chain are shocked.

• Globalization: for low iceberg costs generically get unique technologies used.

• Other sufficient conditions (graph-cut) in paper.

Short Run vs Long Run

Long Run, Hulten's Theorem,

$$\frac{\partial \log(U)}{\partial \log(\lambda)} = \frac{\partial \log(GDP)}{\partial \log(\lambda)} = \frac{(1-\lambda)p_{\tau}y_{\tau}}{GDP}.$$

Short Run, when bound bites

$$\frac{\Delta \log(U)}{\Delta \log(\lambda)} = \frac{\Delta \log(GDP)}{\Delta \log(\lambda)} = \frac{(1-\lambda)\sum_{f \in F(\tau)} p_f c_f}{GDP}.$$



Short Run vs Long Run

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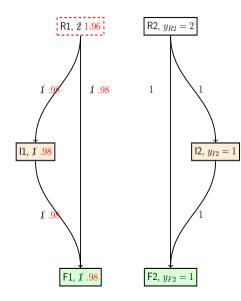
Short Run, when bound bites

$$\frac{\Delta \log(U)}{\Delta \log(\lambda)} = \frac{\Delta \log(GDP)}{\Delta \log(\lambda)} = \frac{(1-\lambda)\sum_{f \in F(\tau)} p_f c_f}{GDP}$$

• Long Run: shocking more expensive technologies has a larger impact.

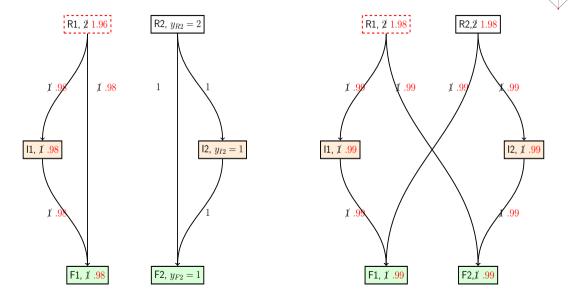
 Short Run: shocking technologies that are used in more final goods has a larger impact.

Long Run: Network Irrelevant, Impact 1%

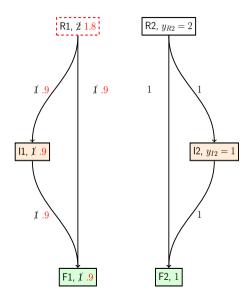




Long Run: Network Irrelevant, Impact 1%

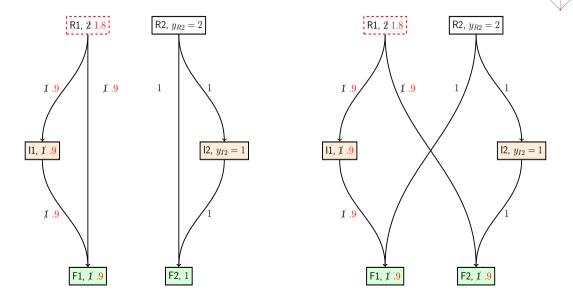


Short Run: Network Matters: Impact 5% or 10%





Short Run: Network Matters: Impact 5% or 10%



Short Run vs Long Run

 \bigcirc

Short Run:

- Network position matters,
- Disrupt all final goods downstream

Long Run:

- (Much) cheaper than Short Run,
- Relative cost of input matters,
- Network matters, but only to extent changes costs.





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Omplexity, Fragility, Globalization

5) The Impact in the Medium Run

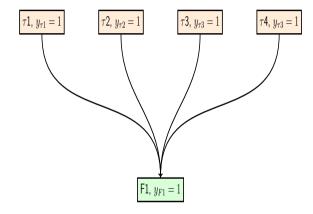
Supply Chain Complexity and Disruption

Under the bound, randomly disrupt any technology to $\lambda < 1 :$

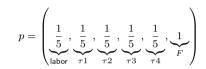
- Probability π disrupt any given technology, independent.
- $S = average \ \# \ inputs \ used \ produce \ a \ final \ good.$
- $q = \mathsf{E}[(\text{cost of random input})/(\text{cost per final good})].$
- m = average number of final goods downstream from random input.



Horizontal Supply Chain (all labor inputs = 1)



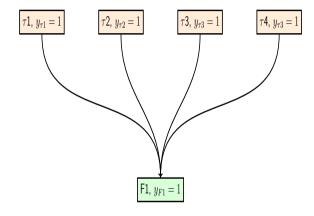
Labor endowment: 5



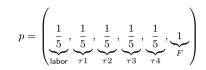
Complexity inputs/final good: S = 4.

Average input cost / final good cost: q = .2

Horizontal Supply Chain (all labor inputs = 1)



Labor endowment: 5



Complexity inputs/final good: S = 4.

Average input cost / final good cost: q = .2

Short Run expected impact: $4(1-\lambda)\pi$

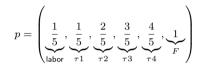
Long Run expected impact: $.8(1-\lambda)\pi$

Vertical Supply Chain (all labor inputs = 1)

$$au 1, \ y_{\tau 1} = 1$$

 $au 2, \ y_{\tau 2} = 1$
 $au 3, \ y_{\tau 3} = 1$
 $au 4, \ y_{\tau 3} = 1$
 $au 4, \ y_{\tau 3} = 1$
 $au 5$
 $au 5$

Labor endowment: 5



Complexity inputs/final good: S = 4.

Average input cost / final good cost: q = .5

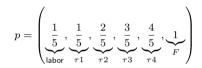


Vertical Supply Chain (all labor inputs = 1)

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Labor endowment: 5



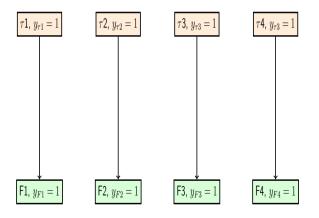
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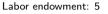
Average input cost / final good cost: q = .5

Short Run expected impact: $4(1-\lambda)\pi$

Long Run expected impact: $2(1-\lambda)\pi$

Parallel Supply Chains (intermediate labor inputs = 1, final goods = 1/4)



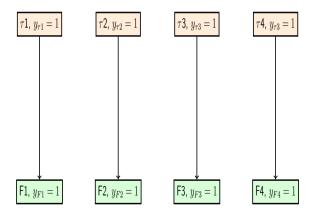


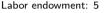
$$p = \left(\underbrace{\frac{1}{5}}_{\text{labor}}, \underbrace{\frac{1}{5}}_{\tau 1}, \underbrace{\frac{1}{5}}_{\tau 2}, \underbrace{\frac{1}{5}}_{\tau 3}, \underbrace{\frac{1}{5}}_{\tau 4}, \underbrace{\frac{1}{5}}_{\tau 4}, \underbrace{\frac{1}{4}}_{F 1}, \underbrace{\frac{1}{4}}_{F 2}, \underbrace{\frac{1}{4}}_{F 3}, \underbrace{\frac{1}{4}}_{F 3}, \underbrace{\frac{1}{4}}_{F 4}, \underbrace{\frac{1}{4}}_{F 3}, \underbrace{\frac{1}{4}}_{F 3},$$

Complexity inputs/final good: S = 1.

Average input cost / final good cost: q = .8

Parallel Supply Chains (intermediate labor inputs = 1, final goods = 1/4)





$$p = \left(\underbrace{\frac{1}{5}, \frac{1}{5}, \frac{1}{5}, \frac{1}{5}, \frac{1}{5}, \frac{1}{5}, \frac{1}{5}, \frac{1}{5}, \frac{1}{5}, \frac{1}{4}, \frac{$$

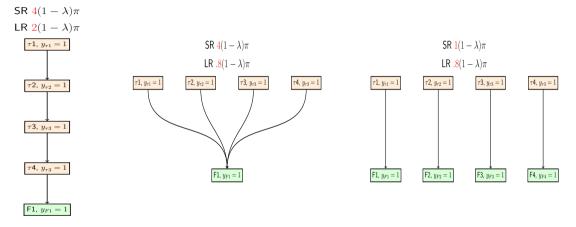
Complexity inputs/final good: S = 1.

Average input cost / final good cost: q = .8

Short Run expected impact: $(1 - \lambda)\pi$

Long Run expected impact: $.8(1-\lambda)\pi$







For small π

Short-Run
$$\mathbb{E}\left[\frac{\Delta GDP}{GDP}\right] \approx -(1-\lambda)\pi S$$
,
Long-Run $\mathbb{E}\left[\frac{\Delta GDP}{GDP}\right] \approx -(1-\lambda)\pi S\frac{q}{m}$.



Supply Chain Complexity and Disruption

Short Run:

- Increased number of goods (S) per supply chain to disrupt,
- Each would disrupt the final good fully (by 1λ).
- Overall effect $(1 \lambda)\pi S$.

Long Run:

- Increased number of goods (S) per supply chain to disrupt,
- But each has a fractional value (q) relative to final good.
- Overall effect $(1 \lambda)\pi Sq$.



Supply Chain Complexity and Disruption

Short Run:

- shape (breadth vs depth) of supply chain is irrelevant (S matters),
- $\bullet\,$ More final goods, lower S, impact compartmentalized.

Long Run :

- shape of supply chain matters as it affects relative costs,
- number of final goods does not matter, relative costs of inputs does.

Trade Costs and Globalization



 $\theta_{\tau\tau'} \geq 1$ units of $O(\tau)$ shipped from τ for 1 unit to get to τ' .

Competing Effects of dropping costs:

- Increased diversity: new technologies/goods become viable as can source inputs that were previously too expensive.
- Increased specialization: only most efficient technology is used.

Trade Costs and Globalization



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- Increased specialization: only most efficient technology is used.
- $\bullet~{\sim}90\%$ of most advanced computer chips assembled in Taiwan,
- Materials cross borders > 70 times before final assembly.

Specialization



Proposition (Specialization)

Generically, if transportation costs are sufficiently low there is a unique equilibrium with full specialization: There exists a cost threshold $\bar{\theta} > 1$ such that if $\max_{\tau,\tau'} \theta_{\tau\tau'} < \bar{\theta}$, then $y_{\tau} > 0$ and $y_{\tau'} > 0$ implies that $O(\tau) \neq O(\tau')$.

Fragility and globalization



Corollary (Globalization)

If transportation costs are sufficiently low, then in generic economies the upper bound is tight for any shock.

As supply chains consolidate: If shocks are not perfectly correlated across different producers of the same good, then the probability of the disruption of the final good decreases, but the expected short-run size of that disruption conditional upon occurrence increases.

Fragility and globalization



- More specialized production—fewer, larger producers,
- Larger shocks, but fewer producers and so (possibly) less frequent.
- As cross more borders, could face more political/transport risk...





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Medium Run



No new sourcing: existing supply chains in place

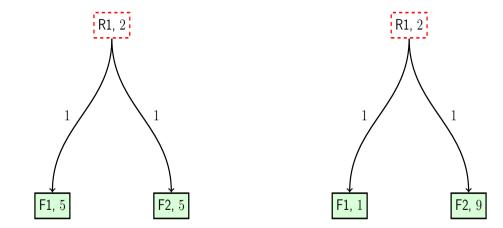
Prices can steer rationed goods to most needed technologies

If multiple flows affected:

- Different supply chains have similar final good values: looks like short run,
- Different supply chains have very different final good values: looks more like long run, only disrupt lowest value chains.

Medium Run Shock Impact

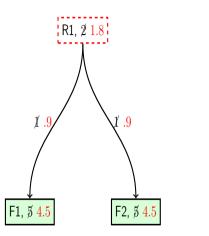




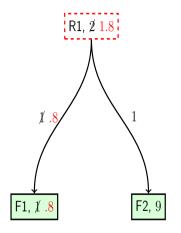
Equal-Valued Final Goods

Unequal-Valued Final Goods





Impact 1/10 Same as Short Run



Impact 1/50 Close to Long Run

Externalities!



- Competition is inefficient (missing markets)
- Competition pushes to cheaper sourcing, low inventories
- Unless compensated for resilience, leads to excessive specialization/fragility
- Policy implications of model:
 - Short run:
 - ★ target 'central' technologies
 - ★ build inventories, substitutes (decrease centrality)
 - ★ build parallel chains
 - Long run:
 - ★ target 'expensive' technologies
 - ★ support diverse technologies for same goods
 - \star favor technologies enabling shallower supply chains



Discussion

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