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THE HOUSING MARKET(S) OF SAN DIEGO

Tim Landvoigt
Monika Piazzesi
Martin Schneider

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ABSTRACT

This paper uses an assignment model to understand the cross section of house prices within a metro area. Movers' demand for housing is derived from a lifecycle problem with credit market frictions. Equilibrium house prices adjust to assign houses that differ by quality to movers who differ by age, income and wealth. To quantify the model, we measure distributions of house prices, house qualities and mover characteristics from micro data on San Diego County during the 2000s boom. The main result is that cheaper credit for poor households was a major driver of prices, especially at the low end of the market.

Tim Landvoigt
Department of Economics
Stanford University
579 Serra Mall
Stanford CA 94305-6072
timlandvoigt@googlemail.com

Martin Schneider
Department of Economics
Stanford University
579 Serra Mall
Stanford, CA 94305-6072
and NBER
schneidr@stanford.edu

Monika Piazzesi
Department of Economics
Stanford University
579 Serra Mall
Stanford, CA 94305-6072
and NBER
piazzesi@stanford.edu

1 Introduction

During the recent housing boom, there were large differences in capital gains across houses, even within the same metro area. Figure 1 illustrates the basic stylized fact for San Diego County, California. Every dot corresponds to a home that was sold in both year 2000 and year 2005. On the horizontal axis is the 2000 sales price. On the vertical axis is the annualized real capital gain between 2000 and 2005. The solid line is the capital gain predicted by a regression of capital gain on log price. It is clear that capital gains during the boom were much higher on low end homes. For example, the average house worth \$200K in the year 2000 appreciated by 17% (per year) over the subsequent five years. In contrast, the average house worth \$500K in the year 2000 appreciated by only 12% over the subsequent five years.¹

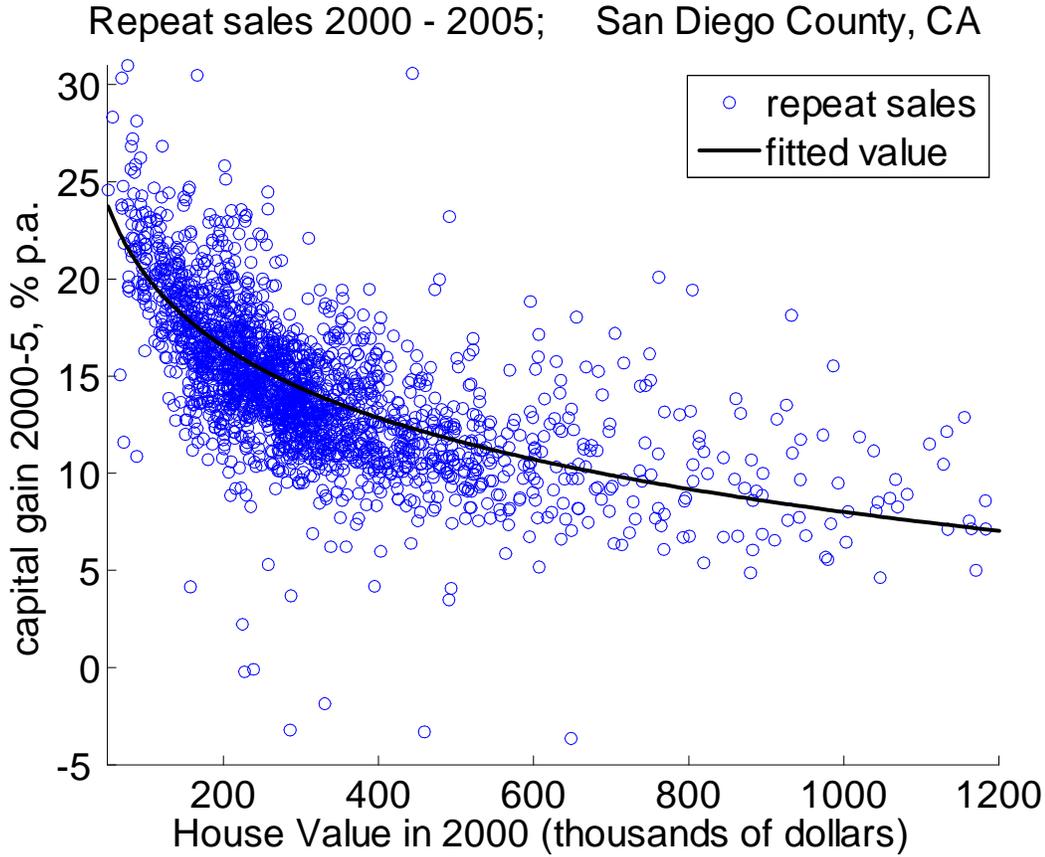


Figure 1: Repeat sales in San Diego County, CA, during the years 2000-2005. Every dot represents a residential property that was sold in 2000 and had its next sale in 2005. The horizontal axis shows the sales price in 2000. The vertical axis shows the real capital gain per year (annualized change in log price less CPI inflation) between 2000 and 2005.

This paper considers a quantitative model of the housing market in the San Diego metro area

¹While Figure 1 only has repeat sales from two particular years, Table 1 below documents the basic stylized fact in a joint estimation using *all* repeat sales in San Diego County over the last decade.

over the boom period. Its key feature is that houses are indivisible and movers are assigned, in equilibrium, to one of a large number of house types. We use the model to examine the connection between various changes in the San Diego housing market (or markets – one for each type) with the cross section of capital gains. In particular, we look at changes in the composition of houses that were transacted, shifts in the distribution of movers’ characteristics, and the availability of cheap credit.

We find that the model is consistent with the large and uneven price changes apparent in Figure 1. Two changes in the environment are particularly important for this result. First, the availability of cheap credit has larger effects on housing demand at the low end of the market, thus increasing relative prices there. Second, the relatively larger number of low quality houses transacted during the boom led richer marginal investors to drive up prices at the low end. Once these two features are taken into account, the lifecycle model of housing demand matches not only prices but also key moments of the joint distribution of house quality, age, wealth and income.

In the model, movers meet houses. Houses differ by quality: there is a continuum of indivisible houses provide different flows of housing services. Movers differ by age, income, and wealth: their demand for housing is derived from an intertemporal savings and portfolio choice problem with transaction costs and collateral constraints. In equilibrium, prices adjust to induce agents with lower demand for housing services to move into lower quality houses. The distribution of equilibrium prices thus depends on the (three-dimensional) distribution of movers’ characteristics as well as the distribution of house qualities.

To implement the model quantitatively, we use micro data to measure the distribution of movers’ characteristics and the quality distribution of transacted houses. We do this both for the year 2000 and for the year 2005 – the peak of the boom. We then compute model predictions for equilibrium prices in both years and derive the cross section of capital gains by quality. We compare those predictions to a repeat sales model estimated on transaction data. Our numerical solution not only finds equilibrium prices, but also an equilibrium assignment that we compare to the assignment in the data. To understand how the model works, we explore model-implied capital gains for different assumptions on changes in the environment; in particular, we capture cheaper credit by lower interest rates and downpayment constraints.

Changes in the distribution of mover characteristics as well as credit conditions jointly generate a housing boom that is very similar to that shown in Figure 1. The only difference is that the model somewhat overpredicts price increases at the high end of the market. At the same time, we check that the equilibrium assignment predicted by the model resembles the assignment observed in the data. In particular, the model matches the fact that house quality rises faster with wealth and income for younger cohorts of households. The reason is that in a lifecycle model with nontradable labor income and collateral constraints, younger households choose more levered portfolios and thus

invest a larger share of cash on hand in housing.

Our exercise fits into a tradition that links asset prices to fundamentals through household optimality conditions. For housing, this tradition has given rise to the “user cost equation”: the per-unit price of housing is such that all households choose their optimal level of a divisible housing asset. With a *single* per-unit price of housing, capital gains on all houses are the same. In our model, there is no single user cost equation since there are many types of indivisible houses, with marginal investors who differ across house types.² Instead, there is a *separate* user cost equation for every house type, each reflecting the borrowing costs, transaction costs, and risk premia of only those movers who buy that house type. Changes in the environment thus typically give rise to a nondegenerate cross section of capital gains.

The fact that there is a *family* of user cost equations is crucial for our results in two ways. First, it implies that changes in the environment that more strongly affect a subset of movers will more strongly affect prices of houses which those movers buy. For example, lower minimum downpayment requirements more strongly affect poor households for whom this constraint is more likely to be binding. As a result, lower downpayment constraints lead to higher capital gains at the low end of the market.

Second, higher moments of the quality and mover distributions matter. For example, we show that the quality distribution of transacted homes in San Diego County at the peak of the boom had fatter tails than at the beginning of the boom. This implied, in particular, that relatively lower quality homes had to be assigned to relatively richer households than before the boom. For richer households to be happy with a low quality home, homes of slightly higher quality had to become relatively more expensive. The price function thus had to become steeper at the low end of the market, which contributed to high capital gains in that segment.

Since we measure the quality distribution of transacted homes directly from the data, we do not take a stand on where the supply of houses comes from. A more elaborate model might add an explicit supply side, thus incorporating sellers’ choice of when to put their house on the market, the effects of the availability of land to developers (as in Glaeser, Gyourko, and Saks 2005), or gentrification (as in Guerrieri, Hartley, and Hurst 2013.) At the same time, any model with an explicit supply side also gives rise to an equilibrium distribution of transacted homes that has to be priced and assigned to an equilibrium distribution of movers. The assignment and pricing equations we study thus hold also in equilibrium of *many* larger models with different supply side assumptions. Our results show what it takes to jointly match prices and mover characteristics, independently of the supply side. In this sense, our exercise is similar to consumption-based asset pricing, where the goal is to jointly match consumption and prices, also independently of the supply side.

²In contrast, the user cost equation determines a unique price per unit of housing, so every investor is marginal with respect to every house.

This paper is the first to study a quantitative assignment model with a continuum of houses and a multidimensional distribution of mover characteristics. Assignment models with indivisible heterogeneous goods and heterogeneous agents have been used in several areas of economics, most prominently to study labor markets where firms with different characteristics hire workers with different skill profiles (for an overview, see Sattinger, 1993.) In the context of housing, an early reference is Kaneko (1982). Caplin and Leahy (2010) characterize comparative statics of competitive equilibria in a general setting with a finite number of agents and goods. Stein (1995), Ortalo-Magne and Rady (2006) and Rios-Rull and Sanchez-Marcos (2008) study models with two types of houses and credit constraints. Määttänen and Terviö (2013) study no trade equilibria of a continuous assignment model with income heterogeneity but no credit frictions; they use their model to relate changes in income inequality to house price distributions across US cities.

We provide new evidence on the cross section of capital gains as well as the composition of trading volume by quality over the recent housing boom. Our results use property level data for San Diego County and several statistical models of price change. Our finding of a nontrivial cross section of capital gains is related to existing empirical studies that compare house price dynamics across price segments within a metro area, for example Poterba (1991), Case and Mayer (1996), Case and Shiller (2005), and Guerrieri, Hartley, and Hurst (2013).³ Existing studies of volume emphasize the comovement of volume and price changes *over time* as "hot" markets with high prices and high volume turn into "cold" markets with low prices and low volume (for example, Stein 1995.) Our results show that during the recent boom the relationship between prices and volume *in the cross section* was nonmonotonic: volume became relatively higher both for cheap houses and for expensive houses.

Our quantitative model considers jointly the effect of credit constraints and changes in the house quality and mover distributions on prices as well as the cross section of household portfolios. Reduced form evidence has suggested that both credit and changes in distributions can matter for prices. For example, Poterba (1991) points to the role of demographics, whereas Bayer, Ferreira, and McMillan (2007) highlight the importance of amenities (such as schools), and Guerrieri, Hartley and Hurst (2013) relate price changes to gentrification, that is, changes in neighborhood quality. Empirical studies have also shown that credit constraints matter for house prices at the regional level. Lamont and Stein (1999) show that house prices react more strongly to shocks in cities where more households are classified as "borrowing constrained". Mian and Sufi (2010) show for the recent US boom that house price appreciation and borrowing were correlated across zip codes. Mian and Sufi (2009) show that areas with many subprime borrowers saw a lot of borrowing even though income there declined.

³Interestingly, these studies do not find a common capital gain pattern across all booms – depending on time and region, low quality houses may appreciate more or less than high quality houses during a boom. This suggests that it is fruitful to study a single episode in detail, as we do in this paper.

Our exercise infers the role of cheap credit for house prices from the *cross section* of capital gains by quality. This emphasis distinguishes it from existing work with quantitative models of the boom. Many papers have looked at the role of cheap credit or exuberant expectations for prices in a homogeneous market (either a given metro area or the US.) They assume that houses are homogeneous and determine a single equilibrium house price per unit of housing capital. As a result, equilibrium capital gains on all houses are identical, and the models cannot speak to the effect of cheap credit on the cross section of capital gains. Recent papers on the role of credit include Himmelberg, Mayer, and Sinai (2005), Glaeser, Gottlieb, and Gyourko (2010), Kiyotaki, Michaelides, and Nikolov (2010) and Favilukis, Ludvigson, and Van Nieuwerburgh (2010). The latter two papers also consider collateral constraints, following Kiyotaki and Moore (1995) and Lustig and van Nieuwerburgh (2005). Recent papers on the role of expectation formation include Piazzesi and Schneider (2009), Burnside, Eichenbaum, and Rebelo (2011), and Glaeser, Gottlieb, and Gyourko (2010).

The paper proceeds as follows. Section 2 presents evidence on prices and transactions by quality segment in San Diego County. Section 3 presents a simple assignment model to illustrate the main effects and the empirical strategy. Section 4 introduces the full quantitative model.

2 Facts

In this section we present facts on house prices and the distribution of transacted homes during the recent boom. We study the San-Diego-Carlsbad-San-Marcos Metropolitan Statistical Area (MSA) which coincides with San Diego County, California.

2.1 Data

We obtain evidence on house prices and housing market volume from county deeds records. We start from a database of all deeds written in San Diego County between 1997 and 2008. In principle, deeds data are publicly available from the county registrar. To obtain the data in electronic form, however, we take advantage of a proprietary database made available by Trulia.com. We use deeds records to build a data set of households' market purchases of single-family dwellings. This involves screening out deeds that reflect other transactions, such as intrafamily transfers, purchases by corporations, and so on. Our screening procedure together with other steps taken to clean the data is described in Appendix A.

To learn about mover characteristics, we use several data sources provided by the U.S. Census Bureau. The 2000 Census contains a count of all housing units in San Diego County. We also use the 2000 Census 5% survey sample of households that contains detailed information on house

and household characteristics for a representative sample of about 25,000 households in San Diego County. We obtain information for 2005 from the American Community Survey (ACS), a representative sample of about 6,500 households in San Diego County. A unit of observation in the Census surveys is a dwelling, together with the household who lives there. The surveys report household income, the age of the head of the household, housing tenure, as well the age of the dwelling, and a flag on whether the household moved in recently.⁴ For owner-occupied dwellings, the census surveys also report the house value and mortgage payments.

2.2 The cross section of house prices and qualities

In this section we describe how we measure price changes over time conditional on quality as well as changes over time in the quality distribution. We first outline our approach. We want to understand systematic patterns in the cross section of capital gains between 2000 and 2005. We establish those patterns using statistical models that relate capital gain to 2000 price. The simplest such model is the black regression line in Figure 1. Below we describe a more elaborate model of repeat sales as well as a model of price changes in narrow geographic areas – the patterns are similar across all these models.

If there is a one-dimensional quality index that households care about, then house quality at any point in time is reflected one-for-one in the house price. In other words, the horizontal axis in Figure 1 can be viewed as measuring quality in the year 2000. The regression line measures common changes in price experienced by all houses of the same initial quality. More generally, any statistical model of price changes gives rise to an expected price change that picks common changes in price by quality.

There are two potential reasons for common changes in price by quality. On the one hand, there could be common changes in quality itself. For example, quality might increase because the average house in some quality range is remodeled, or the average neighborhood in some quality range obtains better amenities.⁵ On the other hand, there could simply be *revaluation* of houses in some quality range while the average quality in that range stays the same. For example, prices may change because more houses of similar quality become available for purchase. In practice, both reasons for common changes in price by quality are likely to matter, and our structural model below thus incorporates both.

Independently of the underlying reason for price changes, we can determine the number of houses

⁴In the 2005 ACS, the survey asks households whether they moved in the last year. In the 2000 Census, the survey asks whether they moved in the last two years.

⁵Importantly, changes in quality will be picked up by the expected price change only if they are common to all houses of the same initial quality, that is, they are experienced by the average house in the segment. The figure shows that, in addition, there are also large idiosyncratic shocks to houses or neighborhoods.

in the year 2005 that are “similar” to (and thus compete with) houses in some given quality range in the year 2000. This determination uses a statistical model of price changes together with the cross section of transaction prices. Consider some initial house quality in the year 2000. A statistical model of price changes – such as the regression line in Figure 1 – says at what price the average house of that initial quality trades in 2005. For example, from the regression line we can compute a predicted 2005 price by adding the predicted capital gain to the 2000 price. Once we know the predicted 2005 prices for the initial quality range, we can read the number of similar houses off the cross sectional distribution of 2005 transaction prices.

In our context, we can say more: counting for *every* initial 2000 quality range the “similar” houses in 2005 actually delivers the 2005 quality distribution, up to a monotonic transformation of quality. This is because the predicted 2005 price from a statistical model is *strictly increasing* in the initial 2000 price, as we document below using both parametric and nonparametric specifications. Since price reflects quality in both years, it follows that for a given 2005 quality level, there is a unique initial 2000 quality level such that the average house of that initial quality resembled the given house in 2005.⁶

Of course, we do not know the mapping from initial 2000 quality to average 2005 quality, because a model of price changes does not distinguish between common changes in quality and revaluation. Nevertheless, since we know that the mapping is monotonic, we can represent the 2005 quality distribution, up to a monotonic transformation, by the distribution of “similar” 2005 houses by 2000 quality. In other words, the 2000 price can serve as an ordinal index of quality. Quality distributions for both 2000 and 2005 can be measured in terms of this index and then used as an input into the quantitative implementation of our structural model below.

Statistical model of price changes by quality

Consider a loglinear model of price changes at the individual property level. This is the statistical model we use to produce inputs for the structural model. To capture the cross section of capital gains by quality, we allow the expected capital gain to depend on the current price. Formally, let p_t^i denote the price of a house i at date t . We assume that the capital gain on house i between dates t and $t + 1$ is

$$\log p_{t+1}^i - \log p_t^i = a_t + b_t \log p_t^i + \varepsilon_{t+1}^i, \quad (1)$$

where the idiosyncratic shocks ε_{t+1}^i have mean zero and are such that a law of large numbers holds in the cross section of houses. For fixed t and $t + 1$, the model looks like the regression displayed in Figure 1.

⁶In the San Diego housing market, common changes in quality between 2000 and 2005 did thus not upset the relative ranking of house quality segments: the average house from a high quality range in 2000 was worth more—and hence of higher quality—than the average house from a low quality range in 2000. This does not mean, of course, that there were no changes in the ranking of individual houses or neighborhoods—in our statistical model those are captured by idiosyncratic shocks.

The model estimated here differs from a simple regression since (1) is assumed to hold for every t in our sample, so that the coefficients can be estimated with data on all repeat sales simultaneously. We find this approach useful since a regression based only on 2000-2005 repeat sales might suffer from selection bias – it would be based only on houses that were bought at the beginning of the boom and sold at the peak.⁷ In contrast, under our approach the estimated coefficient a_t reflects *any* repeat sale that brackets the year t . For example, the coefficients for $t = 2004$, say, reflect repeat sales in the hot phase of the boom between 2002 and 2005, but also repeat sales between 2003 and 2008.

Equation (1) differs from a typical time series model for returns in that the coefficients are time dependent. It is possible to identify a separate set of coefficients for every date because we have data on many repeat sales. The coefficients b_t determine whether there is a nontrivial cross section of expected capital gains. If housing were a homogenous capital good, then it should not be possible to forecast the capital gain using the initial price level p_t , that is, $b_t = 0$. The expected capital gain on all houses would be the same (and equal to a_t), much like the expected capital gain is the same for all shares of a given company. More generally, a nonzero coefficient for b_t indicates that quality matters for capital gains. For example $b_t < 0$ means that prices of low quality houses that are initially cheaper will on average have higher capital gains. In contrast, $b_t > 0$ says that expensive houses are expected to appreciate more (or depreciate less).

Suppose (p_t^i, p_{t+k}^i) is a pair of prices on transactions of the same house that took place in years t and $t + k$, respectively. Equation (1) implies a conditional distribution for the capital gain over k periods,

$$\log p_{t+k}^i - \log p_t^i = a_{t,t+k} + b_{t,t+k} \log p_t^i + \varepsilon_{t,t+k}^i, \quad (2)$$

where the coefficients $a_{t,t+k}$, $b_{t,t+k}$ are derived by iterating on equation (1). We estimate the parameters (a_t, b_t) by GMM; the objective function is the sum of squared prediction errors, weighted by the inverse of their variance. The GMM estimation uses data from repeat sales between all pairs of years jointly by imposing the restriction that the multiperiod coefficients $a_{t,t+k}$ and $b_{t,t+k}$ are appropriate weighted sums and products of future a_t and b_t coefficients between t and $t + k$, respectively.

Table 1 reports point estimates based on 70,315 repeat sales in San Diego County that occurred during 1997-2008. Details of how we screen repeat sales are in Appendix A. The first row in the table shows the sequence of estimates for the intercept a_t . For example, the estimated a_t for the year 1999 is the intercept in the expected capital gain from 1999 to 2000. The intercept is positive for expected capital gains during the boom phase 2000-2005, and negative during 2006-2008, reflecting average capital gains during those two phases. The middle row shows the slope coefficients b_t .

⁷Below we compare GMM estimation results to regression results based on property level, zip code, and census tract prices reported in Appendix B. These results also suggest that selection bias is not a problem.

During the boom phase, the slopes are strongly negative. For example, for the year 2002 we have $b_t = -.09$, that is, a house worth 10% more in 2002 appreciated by .9% less between 2002 and 2003. During the bust phase, the relationship is reversed: positive b_t s imply that more expensive houses depreciated relatively less. The estimated expected capital gains during the boom years are large: a house price between \$100K and \$500K corresponds to $\log p_t^i \in (11.5, 13.1)$, and the resulting expected capital gain $a_t + b_t \log p_t^i$ reaches double digits in many years on all houses in this range.

TABLE 1: ESTIMATED COEFFICIENTS FROM REPEAT SALES MODEL FOR SAN DIEGO

Year	1999	2000	2001	2002	2003	2004	2005	2006	2007
a_t	0.76 (0.04)	1.29 (0.04)	1.41 (0.04)	1.30 (0.04)	0.87 (0.05)	0.60 (0.06)	-0.56 (0.07)	-1.09 (0.10)	-3.18 (0.12)
b_t	-0.05 (0.003)	-0.093 (0.003)	-0.10 (0.003)	-0.09 (0.003)	-0.05 (0.004)	-0.04 (0.004)	0.04 (0.01)	0.07 (0.01)	0.22 (0.01)
σ_t^i	8.8	8.3	8.6	8.2	8.0	8.4	9.7	11.4	13.8

Note: This table reports estimates for coefficients a_t , b_t and the volatility σ_t^i in equation (1) for the indicated years. The data for this estimation are the 70,315 repeat sales in San Diego County during the years 1997-2008. The numbers in brackets are standard errors.

In a second step, we estimate the variances of the residuals (σ_t^2) by maximum likelihood, assuming the shocks ε_{t+1}^i are normally distributed and iid over time as well as in the cross section. This is to get an idea of the idiosyncratic volatility of housing returns faced by households who buy a single property. The results are reported in the bottom row of Table 1. Volatility is around 9% on average, slightly higher than the idiosyncratic volatility of 7% reported by Flavin and Yamashita (2002).⁸ Another interesting pattern is that idiosyncratic volatility increased by more than half in the bust period.

To construct the quality distribution for 2005 below, what matters are the coefficients of the predicted 2005 price given the 2000 price. To ease notation, set t equal to the year minus 2000, so we are interested in $a_{0,5} = 4.75$ and $b_{0,5} = -.322$. The predicted log price for 2005

$$\log \hat{p}_5 = a_{0,5} + (1 + b_{0,5}) \log p_0, \quad (3)$$

is therefore strictly increasing as a function of the 2000 price. In other words, even though lower quality houses appreciated more during the boom, there were no segments that became systematically more valuable than other segments. In Appendix B, we show that this monotonicity is not an

⁸Table 1A in Flavin and Yamashita (2002) reports a 14% return volatility for individual houses. Their Table 1B reports a 7% volatility for the Case-Shiller city index for San Francisco, which is comparable to San Diego. The difference between these two numbers is a 7% idiosyncratic volatility.

artifact of our loglinear functional form (1). Nonparametric regressions of 2005 log price on 2000 log price reveal only small deviations from linearity, and the predicted price function is also strictly increasing.

Quality distributions

Let Φ_0 denote the cumulative distribution function (cdf) of log transaction prices in the year 2000 (or $t = 0$). With the 2000 price as the quality index, the cdf of house qualities is $G_0(p_0) = \Phi_0(p_0)$. This cdf is constructed from all 2000 transactions, not only repeat sales. The repeat sales model describes price movements of houses that exist both in 2000 and in later years. In particular, between 2000 and 2005 (that is, $t = 0$ and $t = 5$), say, common shocks move the price of the average house that starts at quality p_0 in year 0 to the predicted price (3) in year $t = 5$. Since the mapping from year 0 quality p_0 to year t price is monotonic ($1 + b_{0,5} > 0$), we know that common changes in quality do not upset the relative ranking of house qualities. Of course, the quality ranking of individual houses may change because of idiosyncratic shocks – for example, some houses may depreciate more than others. These shocks average to zero because of the law of large numbers.

We now turn to the quality distribution in 2005. Let Φ_5 denote the cdf of all log transaction prices in $t = 5$. We know that the average house that starts at quality p_0 in year 0 trades at the price \hat{p}_5 in year 5. We define the fraction of houses of quality lower than p_0 as

$$G_t(p_0) = \Phi_t(a_{0,5} + (1 + b_{0,5}) \log p_0).$$

By this definition, the index p_0 tracks relative quality across years. If the same set of houses trades in both years 0 and 5, then the quality distributions G_5 and G_0 are identical. More generally, G_5 can be different from G_0 because different sets of houses trade at the two dates. For example, if more higher quality houses are built and sold in $t = 5$, then G_5 will have more mass at the high end. Any new construction of houses will thus be included in the distribution G_5 provided that these new houses are sold in period 5.

Figure 2 shows the cumulative distribution functions G for the base year 2000 as well as for $t = 5$. The cross sectional distribution of prices Φ are taken from Census and ACS data, respectively. (We have also constructed distributions directly from our deeds data, with similar results.) The key difference between the two quality distributions is that there was more mass in the tails in the year 2005 (green line) than in 2000 (blue line.) In other words, the year 2005 saw more transactions of low and high quality homes compared to the year 2000.

What does the one-dimensional quality index measure?

Our approach treats San Diego County as a common housing market and assumes a one-dimensional quality index. The index combines all relevant characteristics of the house which includes features of land, structure, and neighborhood. Above, we have estimated the cross section

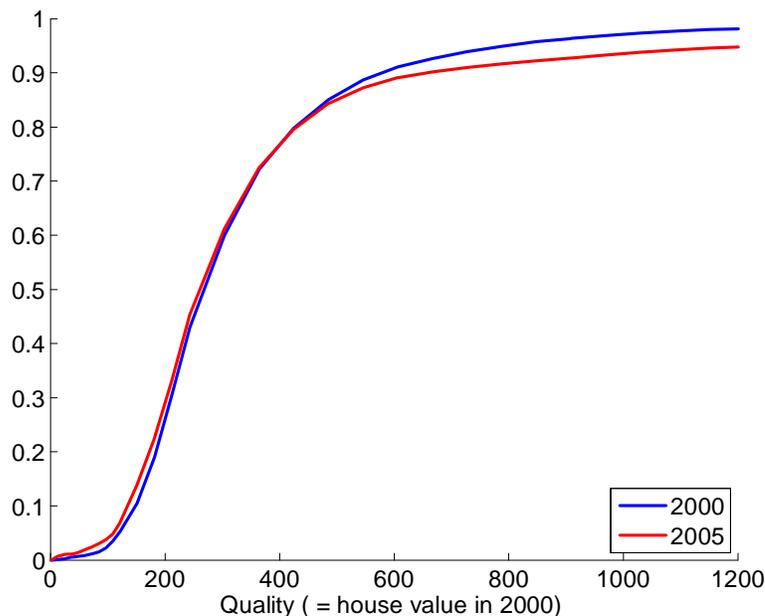


Figure 2: Cumulative distribution function of house qualities in 2000 and 2005

of capital gains by quality from property-level price data. An alternative approach is to look at median prices in narrow geographic areas such as zipcodes or census tracts. If market prices approximately reflect a one dimensional quality index, then the two approaches should lead to similar predictions for the cross section of capital gains. Moreover, adding geographic information should not markedly improve capital gain forecasts for individual houses.

Appendix B investigates the role of geography by running predictive regressions for annualized capital gains between 2000 and 2005. First, we consider the cross section of capital gains by area, with area equal to either zipcode or census tract, defined as the difference in log median price in the area. We regress the area capital gain from 2000 to 2005 on the 2000 median area price (in logs). We compare the results to a regression of property capital gain on the initial property price as considered above. The coefficients on the initial area price variables are close (between .06 and .07) and the R^2 is similar (around 60%). The GMM estimate for $b_{0,5}$ implied by our repeat sales model above was $b_{0,5} = -.322 = -.064 \times 5$ and is thus also in the same range on an annualized basis. Moreover, the predicted capital gains for the median house ($\log p_{2000}^i = \log 247,000 = 12.42$) are within one percentage point of each other. We conclude that the price patterns we find are not specific to a repeat sales approach.

Second, we consider predictive regressions for property level capital gains that include not only the initial property price but also the initial area median price. For both zipcode and census tract, the coefficient on the area price is economically small (less than .015), and in the case of census tract it is not significant. The coefficient on the initial property price is almost unchanged. In both cases, the R^2 increases only marginally by 0.01 percentage points. These results are again consistent

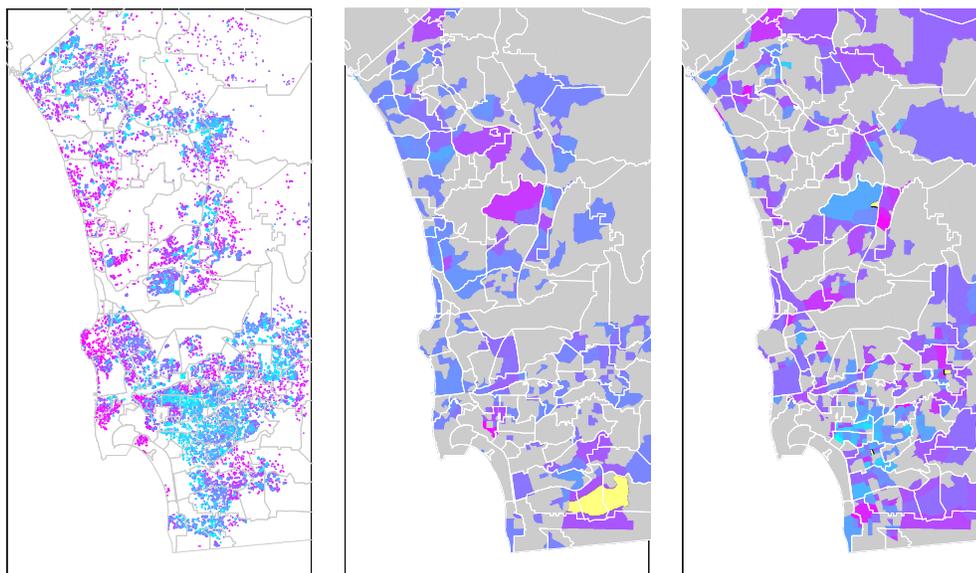


Figure 3: *Left panel:* individual transactions in San Diego County; each dot is a house that was sold in 2005. Color indicates 2005 price ranging from light blue (cheap) to pink (expensive). Grey lines delineate zip codes. *Middle panel:* census tracts colored by change (between 2000 and 2005) in their share of total countywide volume. Warm colors indicate areas where volume increased, with change in share of volume increasing from red to yellow. Cold colors indicate areas where volume decreased, with change in share of volume decreasing from green to blue. Grey areas are census tracts in which the share of total volume changed by less than .05%. *Right panel:* census tracts colored by change in the share of census tract volume contributed by houses in the lowest quintile of the overall county quality distribution. Warm (cold) colors indicate census tracts in which the composition of volume changed towards more (less) low quality housing. Here grey areas are census tracts in which the share of total volume changed by less than 5% in absolute value.

with our assumption that house prices reflect a one-dimensional index that aggregates house and neighborhood characteristics.

Given these findings, it makes sense to construct quality distributions from property level data. This will allow us to accurately capture shifts in quality that happen within narrow geographic areas. To illustrate this heterogeneity as well as the source of shifts in the quality distribution, Figure 3 shows maps of San Diego County. The left hand panel is a map of 2005 housing transactions in the western half of the county. County area to the east is omitted because it comprises sparsely inhabited rural mountain terrain and the Anza-Borrego desert. Each dot in the map is a transaction, with the colormap reflecting price from light blue (cheap) to pink (expensive). The grey lines delineate zip codes. There is geographic clustering: in the rich suburbs along the Pacific, most traded houses are expensive, whereas in the poor areas around downtown most traded houses are cheaper. However, variation is also apparent within narrow geographic areas, and certainly at the level of delineated zipcodes.

The middle and right panels of Figure 3 illustrate the shift in the quality distribution from

2000 to 2005. In particular, the increase in the share of low quality houses in Figure 2 had two components. First, the share of volume in low quality neighborhoods increased at the expense of volume in high quality neighborhood. The middle panel colors census tracts by the change (between 2000 and 2005) in their share of total countywide volume. Grey areas are census tracts in which the share of total volume changed by less than .05% in absolute value. The warm colors (with a colormap going from red = +.05% to yellow = + 1%) represent census tracts for which the share of volume increased. In contrast, the cold colors (with a colormap going from blue = -1% to green = -.05%) indicates census tracts that lost share of volume. Comparing the left and middle panel, a number of relatively cheaper inland suburbs increased their contribution to overall volume, whereas most expensive coastal areas lost volume.

Second, the share of low quality volume increased within census tracts, and here the direction is less clearly tied to overall area quality. The right panel colors census tracts by the change (between 2000 and 2005) in the share of census tract volume that was contributed by houses in the lowest quintile of the overall county quality distribution. Here grey areas are census tracts in which the share of total volume changed by less than 5% in absolute value. Warm colors (with a colormap from red = 5% to yellow = 60%) represent census tracts in which the composition of volume changed towards more low quality housing. The cold colors (colormap from blue = -60% to green = -5%) show tracts where the composition changes away from low quality housing. Comparing the left and right panels, many of the inland neighborhoods that saw an overall increase in volume also experienced an increase in the share of low quality housing. At the same time, there is less low quality housing in the downtown area, which did not see unusual volume. Moreover, even some of the pricey oceanfront zipcodes saw an increase in the share of low quality houses.

2.3 Mover characteristics

Below we model the decisions by movers, so we are interested in the characteristics of movers in San Diego in 2000 and 2005. Table 2 shows summary statistics on the three dimensions of household heterogeneity in our model: age, income, and wealth (defined as net worth, including houses and all other assets). For comparison, we also report statistics for stayer households. The difference in mover versus stayer characteristics is particularly pronounced in the year 2005, at the peak of the housing boom. This finding underscores the importance of measuring the characteristics of movers, which are the households whose optimality conditions we want to evaluate.

Table 2 shows that movers tend to be younger than stayers. In San Diego, roughly 13% of stayer households are aged 35 years and younger. Among movers, this fraction is almost three times as large in the year 2000. It further increases to 46% in the year 2005. Table 2 also shows that the median income of younger households is roughly the same as the median income of older households.

However, younger households are poorer than older households; older households have about 2.5 times as much wealth as younger households. Finally, movers are somewhat poorer than stayers.

TABLE 2: CHARACTERISTICS OF SAN DIEGO MOVERS AND STAYERS

	Year 2000		Year 2005	
	Movers	Stayers	Movers	Stayers
Fraction of households				
aged \leq 35 years	0.34	0.13	0.46	0.14
aged $>$ 35 years	0.66	0.87	0.54	0.86
Median Income (in thousands)				
aged \leq 35 years	74.1	74.8	77.5	86.7
aged $>$ 35 years	82.3	74.4	88.7	78.5
Median Wealth (in thousands)				
aged \leq 35 years	145.0	161.2	222.3	257.0
aged $>$ 35 years	361.4	402.2	603.3	724.7

Note: This table reports summary statistics for stayer and mover households in San Diego County for the years 2000 and 2005. All dollar numbers are in 2005 dollars, and are thus comparable. The table has two age bins for household heads: aged 35 and younger, older than 35 years. For age and income, we use age of the household head and income reported in the 2000 Census and 2005 ACS. For wealth, we use imputed wealth with data from the Survey of Consumer Finances. The appendix explains the details.

The reported medians mask substantial heterogeneity within each characteristic. For example, the top 10 percent richest households tend to receive roughly 20 percent of the total income earned by their age group, which illustrates the fact that there is income inequality. This inequality is even more pronounced for total wealth, where the top 10 percent households own 50 percent of the total wealth in their age group. The amount of inequality stays roughly the same across the two years, 2000 and 2005.

3 Assigning houses to movers

We consider an assignment model of a city. A group of mover households faces an inventory of available houses. Houses are indivisible and come in different qualities indexed by $h \in [0, 1]$. The one-dimensional quality index h summarizes various aspects of housing that households care about (for example square footage, location, views or amenities such as schools.) The inventory of houses

is described by a strictly increasing cumulative distribution function $G(h)$. A house of quality h trades in a competitive market at the price $p(h)$.

Every mover household buys exactly one house. Let $h^*(p, i)$ denote the housing demand function of household i . It depends on the house price function p as well as on household i 's characteristics. In equilibrium, the markets for all house types clear. For every $h \in [0, 1]$, the number of households who demand houses of quality less than h must therefore be equal to the number of such houses in the inventory:

$$\Pr(h^*(p, i) \leq h) = G(h). \quad (4)$$

The price function $p(h)$ describes a set of house prices at which households are happy to be assigned to the available inventory of houses.

How hard it is to solve a model like this depends on (i) how housing demand h^* is derived and (ii) what the distribution of mover characteristics looks like. Our quantitative model derives housing demand from an intertemporal optimization program with uncertainty and frictions (borrowing constraints and transaction costs.) Moreover, households differ by age, wealth, and income so that the distribution of movers is three-dimensional. Both housing demand and equilibrium prices must then be determined numerically.

Before introducing the full model, we consider a simpler version. In particular, we assume that (i) the housing demand is derived from a frictionless, deterministic, one-period optimization problem and (ii) the distribution of mover characteristics is one-dimensional. While this version is not suitable for quantitative work, prices and assignments are available in closed form. We use this model to illustrate how changes in the house quality and mover distributions as well as shocks to a subpopulation (in the vein of a change in credit conditions for poor households) differentially affect prices at the high and low end of the quality spectrum. We also clarify how our setup differs from other models in which houses are priced linearly.

A simple model

Households care about two goods: housing and other (numeraire) consumption. Households start with wealth w and buy a house of quality h at the price $p(h)$. Households also choose their consumption of numeraire c . A household maximizes utility

$$u(c, h) \quad (5)$$

subject to the budget constraint

$$c + p(h) = w.$$

Let $F(w)$ denote the strictly increasing cumulative distribution function of wealth w defined on the nonnegative real line. An equilibrium consists of a consumption and house allocation together

with a price function such that households optimize and markets clear.

The first order condition for the household problem is

$$p'(h) = \frac{u_2(c, h)}{u_1(c, h)}. \quad (6)$$

It says that the marginal rate of substitution (MRS) of housing for numeraire consumption equals the *marginal* value of a house $p'(h)$ at the quality level h that the household chooses. Intratemporal Euler equations that equate MRS and house prices hold in many models of housing. What is special here is that house value does not need to be linear in quality. The MRS is thus equated to a marginal house value that may differ across quality levels. In this sense, houses of different quality are priced by different marginal investors.

Consider an equilibrium such that optimal house quality is unique and strictly increasing in wealth. The assignment of houses to wealth levels is then given by a strictly increasing function $h^* : \mathbb{R}_0^+ \rightarrow [0, 1]$. It is convenient to work with its inverse $w^*(h)$, which gives the wealth level of an agent who is assigned a house of quality h . The market clearing condition (4) now says that, for all h ,

$$F(w^*(h)) = G(h) \implies w^*(h) = F^{-1}(G(h)),$$

where w^* is well defined because F is strictly increasing. The assignment of wealth levels to house qualities depends only on the respective distributions, and is independent of preferences. Of course, prices will depend on preferences through the Euler equations.

The function w^* describes a QQ plot commonly used to compare probability distributions. Its graph is a curve in (h, w) -space that is parametrized by the common cdf value in $[0, 1]$. The shape of the graph w^* is determined by the *relative* dispersion of house quality and wealth. If the relative dispersion is similar, the graph of w^* is close to the 45 degree line. In the special case of identical quality and wealth distributions, the graph of w^* is exactly the 45 degree line. If the distribution of wealth F is more dispersed than the quality distribution G , the graph of w^* is steeper than the 45 degree line. For example, if all houses are essentially of the same quality, but there is some dispersion in wealth, then w^* must be close to a vertical line and is thus very steep. In contrast, if wealth is less dispersed than quality then w^* is flatter than the 45 degree line.

To characterize equilibrium prices in closed form, we specialize further and assume separable log utility, that is, $u(c, h) = \log c + \theta \log h$. From the Euler equations, the marginal house price at quality h must be equal to the MRS between housing and wealth spent on other goods:

$$p'(h) = \theta \frac{w^*(h) - p(h)}{h}. \quad (7)$$

An agent with wealth $w^*(h)$ must be indifferent between buying a house of quality h and spending

$w^*(h) - p(h)$ on other goods, or instead buying a slightly larger house and spending slightly less on other goods. An agent who already spends a lot on other goods is willing to pay more for a larger house (because of diminishing marginal utility of nonhousing consumption.) Therefore, if the house of quality h is assigned to an agent who spends more on nonhousing consumption per unit of house quality, then the slope of the house price function must be steeper at the point h .

To obtain closed form solutions for equilibrium prices, we further assume distributions G and F such that the assignment function is a polynomial of degree n

$$w^*(h) = \sum_{i=1}^n a_i h^i. \quad (8)$$

The lowest-quality house must have a zero price since it is purchased by the buyer who has zero wealth. The unique solution to the ordinary differential equation (7) that satisfies $p(0) = 0$ is given by

$$p(h) = \int_0^h \left(\frac{\tilde{h}}{h} \right)^\theta \frac{\theta w^*(\tilde{h})}{\tilde{h}} d\tilde{h} = \sum_{i=1}^n a_i \frac{\theta}{\theta + i} h^i. \quad (9)$$

If this solution is strictly increasing, then it is an equilibrium house price function. The price for a house of quality h is the weighted average of MRS for all agents who buy quality *less* than h , with the MRS evaluated at total wealth.

When is the price function linear?

In general, the equilibrium price (9) is a nonlinear function of quality. Higher powers of h matter for prices if they matter for the assignment (8). Linear pricing emerges in equilibrium, however, for particular pairs of distributions. Indeed, suppose the distributions F and G are scaled version of each other, that is, $F(w) = G(w/k)$ for some positive constant k . The assignment function is then $w^*(h) = kh$. Let $\bar{W} = \int w dF(w)$ and $\bar{H} = \int h dG(h) = \bar{W}/k$ denote average wealth and house quality, respectively. The price function can be written as $p(h) = \bar{p}h$ with

$$\bar{p} = \frac{\theta}{\theta + 1} \frac{\bar{W}}{\bar{H}}. \quad (10)$$

It depends on the distributions F and G only through their respective means. More generally, the segment-specific house price (9) can depend on details of the distributions through the parameters of the assignment (8).

The emergence of linear pricing as a knife-edge case is not limited to log utility. Indeed, given a utility function such that housing is a normal good, a cdf $F(w)$ for movers and an average housing quality $\bar{H} = \int h dG(h)$, we can find a cdf $\tilde{G}(h)$ with mean \bar{H} such that (i) the assignment can be represented by an increasing function $w^*(h) = F^{-1}(\tilde{G}(h))$ and (ii) the price function is linear

$p(h) = \bar{p}h$, where for all h we have

$$\bar{p} = \frac{u_2(c, h)}{u_1(c, h)}. \quad (11)$$

When pricing is linear, the per-unit house price \bar{p} enters the Euler equations of *all* households: The marginal (or, equivalently, the average, per unit) user cost can be read off the Euler equation of any household – in this sense *every* household is a marginal investor for *every* house $h \in [0, 1]$. In contrast, in the nonlinear pricing case, the marginal user cost at quality h can be read off only *one* Euler equation (6), that of the marginal investor with wealth $w^*(h)$.

The linear special case is *imposed* in macroeconomic models with divisible housing capital. In these models, there is a production technology that converts different houses into each other which is linear; the marginal rate of transformation between different houses is thus set equal to one. Moreover, the cdf $\tilde{G}(h)$ is assumed to adjust so as to ensure linear pricing. As a result, the per unit price of housing \bar{p} changes if and only if the marginal rate of substitution of *all* investors changes. In our quantitative approach below, we do not take a stance on the production technology or the house quality distribution $G(h)$. Instead, we measure the cdf $G(h)$ directly from the data – in other words, we let the data tell us whether the pricing is linear or nonlinear.

Graphical example

Figure 4 illustrates equilibria with separable log utility. The top left panel shows a wealth density $f(w) = F'(w)$. The top right panel shows a uniform house density $g(h) = G'(h)$. In both panels, the second and fourth quintile have been shaded for easier comparison. The bottom left panel shows house prices. The solid line is the house price function $p(h)$. Its nonlinearity reflects the different shapes of F and G that lead to a nonlinear assignment w^* . The dotted line is the price function for a comparison economy with the same mean house quality but linear pricing. In the comparison economy, at least one of the distributions must be different so w^* is linear. For example, we could have the uniform house quality distribution G together with a uniform wealth distribution \tilde{F} . Alternatively, we could have the wealth distribution could be F together with a house quality distribution \tilde{G} adjusted so quality is a scaled version of wealth. The latter would emerge in equilibrium in a model with divisible housing.

To understand in more detail how the shape of the price function depends on F and G , consider first the assignment function $w^*(h) = F^{-1}(G(h))$, plotted in the bottom right panel. It is relatively steep for low and high house qualities, and relatively flat in between. Locally, the slope of w^* is higher at a point h if house quality near that point is less dispersed than wealth. Indeed, if there are many houses of quality close to h , but few movers have wealth close to $w^*(h)$, then some houses close to h must be assigned to movers who are much richer or poorer than $w^*(h)$, so the function w^* is steep around h . The overall effect can be seen in the figure by focusing on relative dispersion of wealth and house quality within quintiles. The dispersion of house quality is the same in each

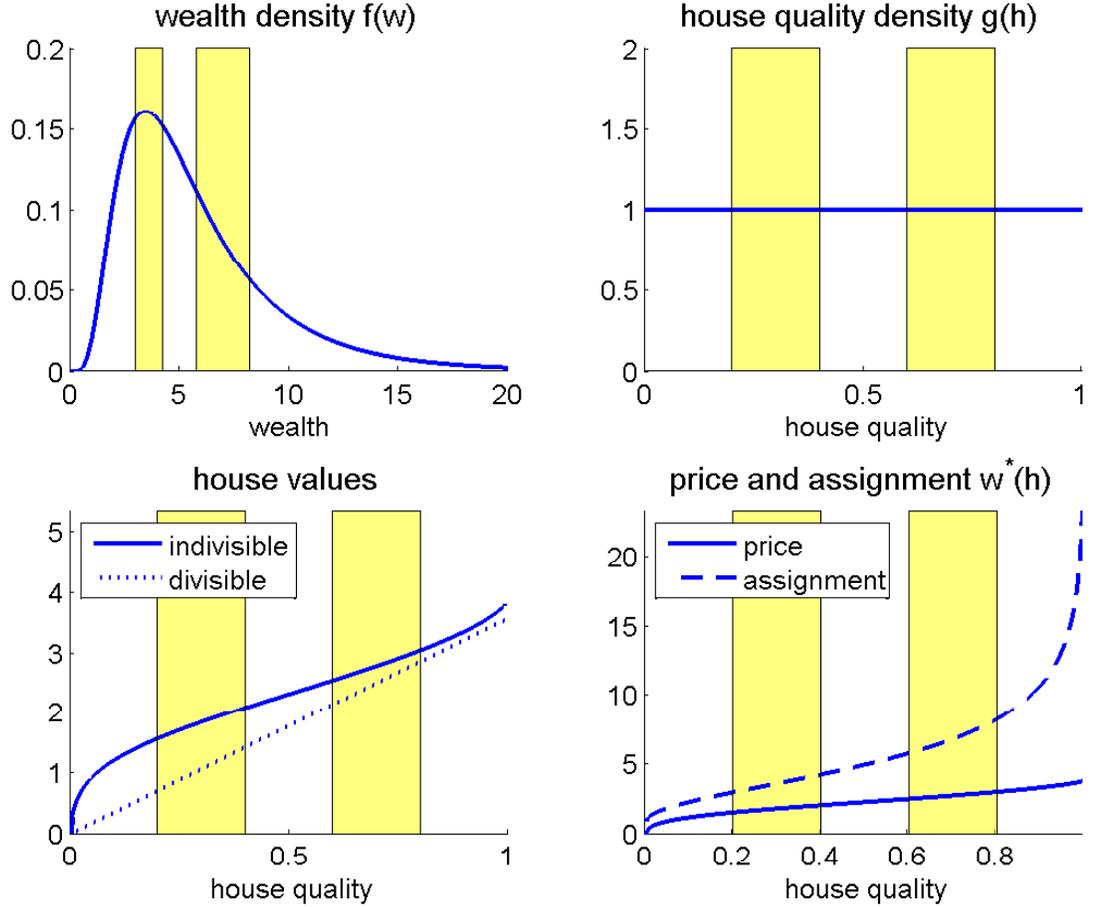


Figure 4: Equilibrium prices and assignment with lognormal wealth density $f(w)$ and uniform house quality density $g(h)$. Top left: wealth density $f(w)$. Top right: house quality density $g(h)$. Bottom left: the equilibrium house price function $p(h)$ in the indivisible model (solid line) and the divisible model (dotted line). Bottom right: assignment $w^*(h)$ and house prices. Shaded areas indicate the quintiles of the distribution.

quintile due to the uniform distribution. The dispersion of wealth is relatively high in the first and fifth quintile (where w^* is therefore steep), but relatively low in the second and third quintile (where w^* is flatter).

The house price function is determined by the segment-specific Euler equation (7). For a given quality h , the price function is steeper if the marginal investor spends more on nonhousing consumption per unit of house quality. In particular, for a given $p(h)$, the house price must rise more if the marginal investor is richer. The house price function thus inherits from the assignment w^* the property that it steepens for very high and very low qualities. There is less steepening at high qualities where wealth per unit of quality responds less to w^* . In addition, the house price function must be consistent with pricing by all marginal investors at qualities less than h . More dispersion in wealth relative to house quality in lower quintiles thus leads to higher prices in higher quintiles.

For the very smallest houses, the closed form solution for price (9) analytically illustrates the role of relative dispersion. First order expansion of p at $h = 0$ delivers⁹

$$p(h) \approx \frac{\theta}{\theta + 1} a_1 h \quad (12)$$

In general, the slope of the price function at $h = 0$ thus depends not only on θ , but also on the slope of the assignment function w^* and thus the relative shape of the cdfs near zero. For example, if the densities f and g are defined for positive w and h , respectively, then a_1 is the limit, as h goes to zero, of the density ratio $g(h)/f(w^*(h))$. If, say, the house density is higher than the wealth density near zero then the price function has to slope up steeply. This is because many similar small houses have to be assigned to movers of different wealth. In contrast, with linear pricing, $a_1 = 1$ and the slope $p'(0)$ depends only on preferences.

Comparative statics

Figure 5 shows what happens if the house quality distribution has fatter tails: there is more mass at both the low and high end. The new density – the green line in the top right panel – is U-shaped and symmetric around one half. The mean house quality is thus the same as under the original uniform density. While the densities here are stylized, a move from the blue to the green density qualitatively mimics the move from the 2000 to the 2005 quality distribution displayed in Figure 2 and studied quantitatively in Section 5 below. The green line in the bottom left panel is the new price function, $\hat{p}(h)$ say. Prices change to reflect the new relative shapes of the distributions. In contrast, if pricing was linear, then prices would not change since the means have not changed.

The bottom right panel shows capital gains by house value. It plots the log house value in the “blue economy” ($\log p(h)$, or the log of the blue line in the bottom left panel) on the horizontal axis against the capital gain from blue to green ($\log \hat{p}(h) - \log p(h)$ or the log difference between the green and blue lines in the bottom left panel) on the vertical axis. Capital gains are positive and higher at the low end than at the high end. Indivisibility of housing is crucial for this result – in a model with divisible housing and hence linear pricing, capital gains would be zero.

To understand the intuition, it is again helpful to consider the relative dispersion of wealth and quality within quintiles. In the bottom quintile, the dispersion of house qualities has now decreased, making wealth even more dispersed relative to quality. The assignment w^* must become steeper in this region as richer agents must buy lower quality houses. A steeper assignment in turn implies a steeper house price function.¹⁰ Starting from the smallest house, prices rise faster to keep richer

⁹In particular we have $a_1 = g(0)/f(0)$ if the densities are defined at zero, but this is not necessary for a polynomial w^* .

¹⁰For example, for the smallest houses, the increase in the house quality density at zero induces an increase in a_1 , to \hat{a}_1 say. The capital gain satisfies

$$\lim_{h \rightarrow 0} (\log \hat{p}(h) - \log p(h)) = \log \frac{\hat{a}_1}{a_1}$$

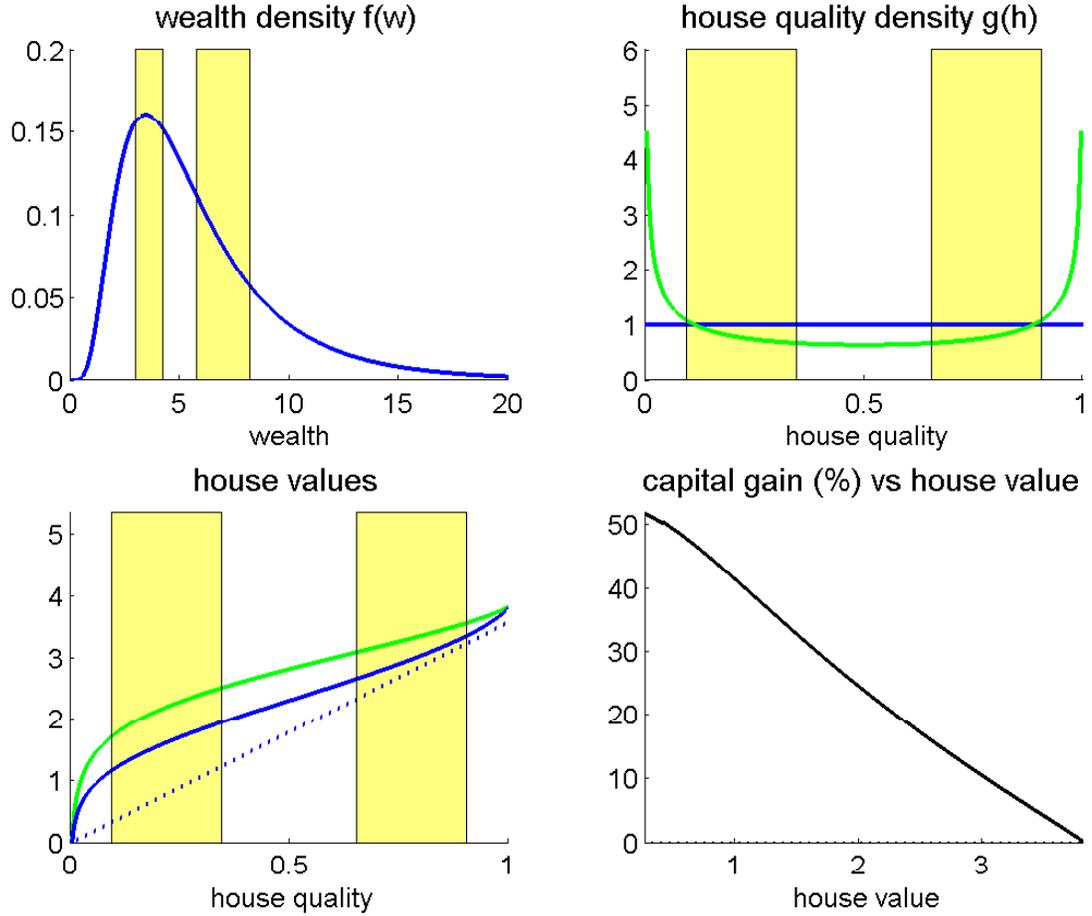


Figure 5: Changing the distribution of house qualities. Top left: wealth density $f(w)$. Top right: quality density $g(h)$ under uniform (blue) and beta (green). Bottom left: blue equilibrium price function $p(h)$ for uniform distribution, green function for beta quality density. Bottom right: capital gain from blue prices to green prices.

marginal investors indifferent. For higher qualities, for example in the third quintile, the effect is reversed: as the house distribution is more dispersed than the wealth distribution, poorer marginal investors imply a flatter price function.

Figure 6 provides an example of a shock to a subpopulation. We assume that all agents with wealth less than 4 develop a higher taste for housing, as measured by the parameter θ . Over that range, we choose the increase in θ to be linearly declining in wealth, with a slope small enough such that the assignment is still monotonic in wealth. The wealth and quality distributions are the same as before. The bottom panels show prices and capital gains. The Euler equation predicts that the slope of the price function becomes steeper for low house qualities that poor households buy and capital gains are higher there. With linear pricing, prices also rise to reflect higher demand for housing but capital gains must be the same everywhere. It follows that in our model, a shock that

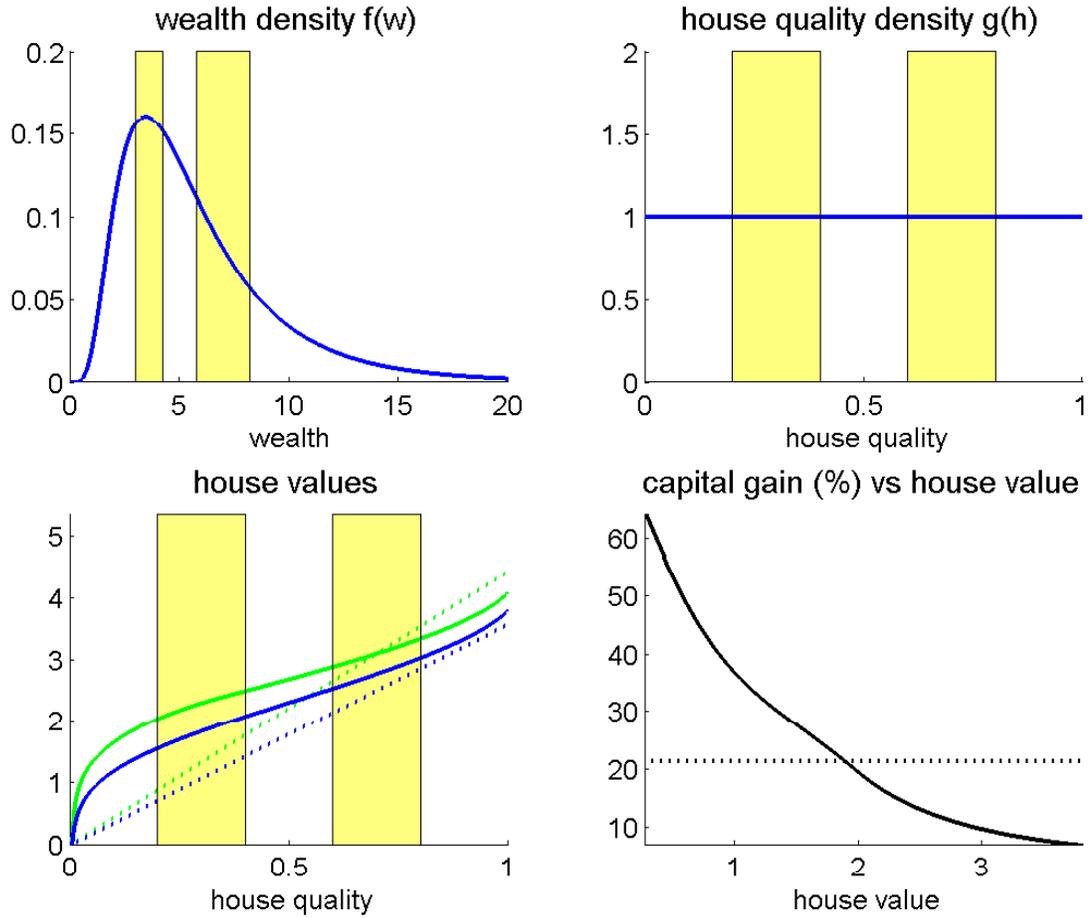


Figure 6: Changing poor households' preferences for housing.

affects only poor agents has larger effects on prices at the low end than in a model with divisible housing.

4 A Quantitative Model

For the stylized model in the previous section, housing demand was derived from a frictionless, deterministic, static optimization problem and households differed only in wealth. In this section, we describe a more general intertemporal problem for household savings and portfolio choice. This problem accommodates many features that have been found important in existing studies with micro data, and thus lends itself better to quantitative analysis. It differs from most existing models because there is a continuum of (indivisible) assets that agents can invest in.

The problem is solved for a distribution of households that differ in age, income, and cash on hand (that is, liquid resources). The distribution is chosen to capture the set of movers in San Diego County in a given year. An equilibrium is defined by equating the distribution of movers' housing

demand derived from the dynamic problem to the distribution of transacted houses. Appendix D contains a detailed description of our computations.

4.1 Setup

Households live for at most T periods and die at random. Let D_t denote a death indicator that equals one if the household dies in period t or earlier. This indicator is independent over time but has an age-dependent probability. Preferences are defined over streams of housing services s and other (numeraire) consumption c during lifetime, as well as the amount of numeraire consumption w left as bequest in the period of death. Conditional on period τ , utility for an agent aged a_τ in period τ is

$$E_\tau \left[\sum_{t=\tau}^{\tau+T-a_\tau} \beta^t [(1 - D_t) u(c_t, s_t(h_t)) + (D_t - D_{t-1}) v^b(w_t)] \right] \quad (13)$$

Households have access to two types of assets. First they can buy houses of different qualities $h \in [0, 1]$ that trade at prices $p_t(h)$. Owning a house is the only way to obtain housing services for consumption. A house of size h_t owned at the end of period t produces a period t service flow $s_t(h_t)$ where the function s_t is strictly increasing. It may depend on time to accommodate growth.

Households also participate in the credit market. Between period t and $t + 1$, the household can either lend at the rate R_t or borrow at the rate $R_t + \rho_t$. The spread ρ_t is strictly positive so the household never simultaneously borrows and lends.¹¹ We denote net borrowing by b_t so $b_t < 0$ represents bond purchases. We assume that a household can only borrow up to a fraction $1 - \delta_t$ of the value of his house. In other words, the amount b_t must satisfy

$$b_t \leq (1 - \delta_t)p_t(h_t). \quad (14)$$

The fraction δ_t is the downpayment requirement on a house.

We introduce three further features that distinguish housing from bonds. First, selling houses is costly: the seller pays a transaction cost ν that is proportional to the value the house. Second, every period an owner pays a maintenance cost ψ , also proportional to the value of the house. Finally, a household can be hit by a moving shock $m_t \in \{0, 1\}$, where $m_t = 1$ means that they must sell their current house. Formally, the moving shock may be thought of as a shock to the housing services production function $s_t(\cdot)$ that permanently leads to zero production unless a new house is bought. Of course, households may also choose to move when they do not receive a moving shock,

¹¹The spread here accounts for screening costs on the part of lenders. It does not incorporate expected costs of default since the number of mortgage defaults during the boom period we study was negligible. For an application to the bust period, it would be important to include these mortgage defaults explicitly in to the model (as in Chatterjee and Eyigungor 2009, Corbae and Quintin 2010, Campbell and Cocco 2010.)

for example because their income has increased sufficiently relative to the size of their current home.

Households receive stochastic income

$$y_t = f(a_t) y_t^p y_t^{tr} \quad (15)$$

every period, where $f(a_t)$ is a deterministic age profile, y_t^p is a permanent stochastic component, and y_t^{tr} is a transitory component.

Our approach to incorporating the tax system is simple. We assume that income is taxed at a rate τ . So the aftertax income $(1 - \tau) y_t$ enters cash on hand and the budget constraint. Mortgage interest can be deducted at the same rate τ . Interest on bond holdings is also taxed at rate τ . Therefore, the aftertax interest rate $(1 - \tau) R_t$ enters cash on hand and the budget constraint. We assume that housing capital gains are sheltered from tax.

To write the budget constraint, it is helpful to define cash on hand net of transaction costs. The cash w_t are the resources available if the household sells:

$$w_t = (1 - \tau) y_t + p_t(h_{t-1})(1 - \nu) - (1 - \tau) (R_{t-1} + \rho_{t-1} \mathbf{1}_{\{b_{t-1} > 0\}}) b_{t-1} \quad (16)$$

The budget constraint is then

$$c_t + (1 + \psi) p_t(h_t) = w_t + \mathbf{1}_{[h_t = h_{t-1} \& m_t = 0]} \nu p_t(h_{t-1}) + b_t \quad (17)$$

Households can spend resources on numeraire consumption and houses, which also need to be maintained. If a household does not change houses, resources are larger than w_t since the household does not pay a transaction cost. The household can also borrow additional resources.

Consider a population of movers at date t . A mover comes into the period with cash w_t , including perhaps the proceeds from selling a previous home. Given his age a_t , current house prices p_t as well as stochastic processes for future income y_τ , future house prices p_τ , the interest rate R_τ , the spread ρ_τ , and the moving shock m_τ , the mover maximizes utility (13) subject to the budget and borrowing constraints. We assume that the only *individual-specific* variables needed to forecast the future are age and the permanent component of income y_t^p . The optimal housing demand at date t can then be written as $h_t^*(p_t; a_t, y_t^p, w_t)$.

As in the previous section, the distribution of available houses is summarized by a cdf $G_t(h)$. The distribution of movers is described by the joint distribution of the mover characteristics (a_t, y_t^p, w_t) . An equilibrium for date t is a price function p_t and an assignment of movers to houses such that households optimize and market clear, that is, for all h ,

$$\Pr(h_t^*(p_t; a_t, y_t^p, w_t) \leq h) \leq G_t(h).$$

This equation involves the optimality conditions of movers. We do not explore the optimality conditions of non-movers as well as developers or other sellers. These conditions impose additional restrictions on equilibrium prices.

The dynamic programming problem for movers does not offer them the option to rent a house in the future. There are certain states of the world (with extremely low income or cash), in which such a rental option might be attractive. However, transitions from owning to renting happen rarely in the data. For example, Bajari, Chan, Krueger, and Miller (2012) estimate this transition probability to be 5% for all age cohorts. Moreover, our continuous distribution of house qualities includes some extremely small homes for households who want to downscale. The absence of a rental option will thus not matter much for our quantitative results below.

4.2 Numbers

We now explain how we quantify the model. In this section, we describe our benchmark specification. Section 5 discusses results based on several alternatives. It is helpful to group the model inputs into four categories

1. Preferences and Technology

(Parameters fixed throughout all experiments.)

- (a) Felicity u , bequest function v , discount factor β
- (b) conditional distributions of death and moving shocks
- (c) conditional distribution of income
- (d) maintenance costs ψ , transaction costs ν
- (e) service flow function (relative to trend)

2. Distributions of house qualities and mover characteristics

3. Credit market conditions

- (a) current and expected future values for the interest rate R and the spread ρ
- (b) current and expected future values for the downpayment constraint δ

4. House price expectations

Our goal is to explain house price changes during the boom. We thus implement the model for two different trading periods: once before the boom, in the year 2000, and then again at the peak

of the boom, the year $t = 2005$. Preferences and technology are held fixed across trading periods. In contrast, the distributions of house qualities and mover characteristics, credit conditions as well as expectations about prices and credit conditions change across dates. To select numbers use data on distributions and market conditions together with survey expectations.

For the pre-boom implementation (labeled $t = 2000$), distributions are measured using the 2000 Census cross section. Credit market conditions are based on 2000 market data and are expected to remain unchanged in the future. Moreover, households expect all house prices to grow at trend together with income, so relative prices remain unchanged. The service flow function is chosen to match 2000 house prices at these expectations. At the same time, preference parameters are fixed to match moments of the wealth distribution.

For the peak-of-the-boom implementation (labeled $t = 2005$), distributions are measured using the 2005 ACS. For the baseline exercise, we assume that (i) credit market conditions are based on 2005 market data, (ii) interest rates are expected to mean revert, while other borrowing conditions are expected to remain unchanged and (iii) all house prices grow at trend together with income. We then compare predictions for 2005 equilibrium house prices with 2005 data. Other exercises varying (i) – (iii) are described below. In particular, Appendix E considers a scenario in which households anticipate the Great Recession, expecting tighter credit and lower house prices. We now describe all elements of the quantitative strategy in detail.

Preferences and technology

The period length for the household problem is three years. Households enter the economy at age 22 and live at most 23 periods until age 91. Survival probabilities are taken from the 2004 Life Table (U.S. population) published by the National Center of Health Statistics. Felicity is given by CRRA utility over a Cobb-Douglas aggregator of housing services and other consumption:

$$u(c, s) = \frac{[c^{1-\rho} s^\rho]^{1-\gamma}}{1-\gamma}, \quad (18)$$

where ρ is the weight on housing services consumption, and γ governs the willingness to substitute consumption *bundles* across both time period and states of the world. We work with a Cobb-Douglas aggregator of the two goods, with $\rho = .2$. If divisible housing services are sold in a perfect rental market, the expenditure share on housing services should be constant at 20%. This magnitude is consistent with evidence on the cross section of renters' expenditure shares (see for example, Piazzesi, Schneider, and Tuzel 2007.) We also assume $\gamma = 5$, which implies an elasticity of substitution for consumption bundles across periods and states of 1/5.

Utility from bequests takes the form $v^b(w) = \bar{v}^b w^{1-\gamma} / (1-\gamma)$ with $\gamma = 5$. We choose the constant \bar{v}^b as well as the discount factor to match average household wealth as well as average wealth of households older than 81, both in 2000. The resulting constant \bar{v}^b is 0.54 and the discount

factor is $\beta = .95$.

The moving shocks are computed based on two sources. First, we compute the fraction of households who move by age, which is about a third per year on average. The fraction is higher for younger households. To obtain the fraction of movers who move for exogenous reasons, we use the 2002 American Housing Survey which asks households in San Diego about their reasons for moving. A third of movers provides reasons that are exogenous to our model (e.g., disaster loss (fire, flood etc.), married, widower, divorced or separated.)

We estimate the deterministic life-cycle component $f(a_t)$ in equation (15) from the income data by movers. The permanent component of income is a random walk with drift

$$y_t^p = y_{t-1}^p \exp(\mu + \eta_t), \quad (19)$$

where μ is a constant growth factor of 2% and η_t is iid normal with mean $-\sigma^2/2$. The transitory component y_t^{tr} of income is iid. The standard deviation of permanent shocks η_t is 11% and the standard deviation of the transitory component is 14% per year, consistent with estimates in Cocco, Gomes, and Maenhout (2005).

We assume that maintenance expenses cover the depreciation of the house. Based on evidence from the 2002 American Housing Survey, maintenance ψ is roughly 1% of the house value per year. The transaction costs ν are 6% of the value of the house, which corresponds to real estate fees in California.

The housing services produced by a house of quality h grow at the same rate μ as income. Starting from an initial service flow function $s_t(h)$, households expect

$$s_{t+1}(h) = \exp(\mu) s_t(h). \quad (20)$$

As discussed above, the initial service flow function s_0 is backed out so that the model exactly fits the 2000 price distribution. Constant growth of service flow over time is consistent with evidence on improvements in the cross section of houses discussed in Appendix C.

Distributions of house qualities and mover characteristics

House quality is expressed in terms of 2000 prices as described in Subsection 2.2; the relevant 2000 and 2005 quality cdfs are shown in Figure 2. The problem of an individual household depends on characteristics (a_t, y_t^p, w_t) . For age and income, we use age of the household head and income reported in the 2000 Census (for $t = 2000$) and 2005 ACS (for $t = 2005$). The Census data does not contain wealth information. We impute wealth using data from the Survey of Consumer Finances. The appendix contains the details of this procedure.

Credit market conditions

Current lending and borrowing rates are set to their corresponding values in the data. For the lending rates R_t , the data counterpart is the three-year interest rate on Treasury Inflation-Protected Securities (TIPS), since the model period is three years. We thus set the lending rate to 3% for 2000 and to 1% for 2005. For the spread ρ_t between borrowing and lending rates, we use the difference between mortgage and Treasury rates. The spread is thus 2% in 2000 and 1.3% in 2005.

Expectations about future (real) lending rates and spreads are set according to consensus long range forecasts on nominal interest rates and inflation from Bluechip Surveys. Survey forecasts suggest a belief in mean reversion for lending rates at the peak of the boom. Indeed, in both 2000 and 2005, long-run forecasts for nominal Treasury rates were about 5.5% and long forecasts for inflation were about 2.5%, pointing to the same expected real rate of 3%. We thus assume that, in 2000, real rates in 2000 were expected to remain at 3%, whereas in 2005, real rates were expected to increase from 1% to 3%.

Survey forecasts further suggest a belief that future spreads between lending and borrowing rates would persist. Indeed, long run consensus forecasts for nominal mortgage rates in 2000 and 2005 were 7.5% and 6.7%, respectively. Together with the nominal Treasury rate forecasts above, we obtain spread forecasts that are close to the current values of 2% and 1.3%, respectively. We thus assume that spreads are expected to remain at their respective current values in both 2000 and 2005.

For the current downpayment constraint δ_t , we use 20% to describe conditions before the housing boom in 2000, and 5% for the peak of the boom in 2005. These assumptions are in line with recent evidence that credit became looser, although there is some uncertainty about the magnitude of the shift. Geanakoplos (2010) shows that average CLTV ratios for securitized subprime and Alt-A loans among the top 50% leveraged homeowners increased from 86.4% to 97.3%. Lee, Mayer and Tracy (2012) look at coastal areas of the US; they show average combined loan-to-value ratios at origination of 94% in 2001 and 96% in 2006 as well as significant increase in the fraction of high LTV mortgages. Keys, Piskorski, Seru and Vig (2014) show that average CLTV ratios increased from 83% in 2000 to 95% in 2005. Similar to the case of spread forecasts, households expect the current downpayment constraints to remain in place in the future.

House price expectations

Under our baseline scenario, households believe that capital gains on houses of quality h are given by

$$p_{t+1}(h) = p_t(h) \exp(\mu + u_{t+1}(h)). \quad (21)$$

where $u_{t+1}(h)$ is an idiosyncratic property-level shock that is realized only when the house is sold. Expected capital gains on all houses are given by the trend growth rate of labor income μ which is

the same in both 2000 and 2005. This approach is motivated by two considerations. On the one hand, it is consistent with evidence that homebuyers during recent housing booms in California did not anticipate subsequent price declines.¹² On the other hand, it implies that return expectations are not assumed to be special at the peak of the boom, but instead allows us to focus on the role of credit market conditions.¹³

We set the volatility of the property-level shock equal to 9% per year over the three year model period. We have also investigated adding an aggregate risk component that shifts the price function for all houses. We have found that the results are not very sensitive to adding the modest amounts of aggregate risk that are commonly measured from regional house prices (e.g., Flavin and Yamashita 2002.) We thus omit aggregate regional risk, and model agents' views about the San Diego market as a whole only through different scenarios for the conditional mean (as described below).

5 Quantitative Results

In this section we compare pricing by quality segment in our base year 2000 to pricing at the peak of the boom in 2005. The 2005 environment differs from the base year environment in three respects: the house quality and mover distributions (in particular, the 2005 house quality distribution has fatter tails), credit conditions (in particular, interest rates and downpayment constraints are lower in 2005) and house price growth expectations (in particular, 2005 households expect prices to revert to 2000 levels). Below we also report on experiments that consider each feature in isolation.

5.1 Prices and service flow in the base year 2000

The first step in our quantitative analysis considers the base year 2000. Here we take as given *(i)* the distributions of house quality and mover characteristics, *(ii)* credit conditions that were prevalent in the year 2000, and *(iii)* constant capital gains in price expectations. We then determine a service flow function $s_0(h)$ such that the model exactly fits the cross section of observed house prices in the year 2000.

Figure 7 shows the resulting service flow function. It is strictly increasing in house quality. It is also concave over almost all of the quality range (except for the lowest qualities.). Since our quality

¹²It is difficult to come up with sharp measures of return expectations for houses in San Diego. Case, Quigley and Shiller (2004) performed mail surveys of homebuyers in Orange and Alameda county during the California boom years of 1988 and 2002. Their point estimates suggest high capital gains expectations – above 10% per year over 10 years – in both years, although they are rather imprecise.

¹³In contrast, some recent literature has attributed features of the housing boom to exceptionally high capital gain expectations, for example because of higher expected growth rates to the local cost of housing (Himmelberg, Mayer and Sinai, 2005) or extrapolation of past capital gains by a small subset of investors in a search market (Piazzesi and Schneider, 2009). Such effects are shut down here.

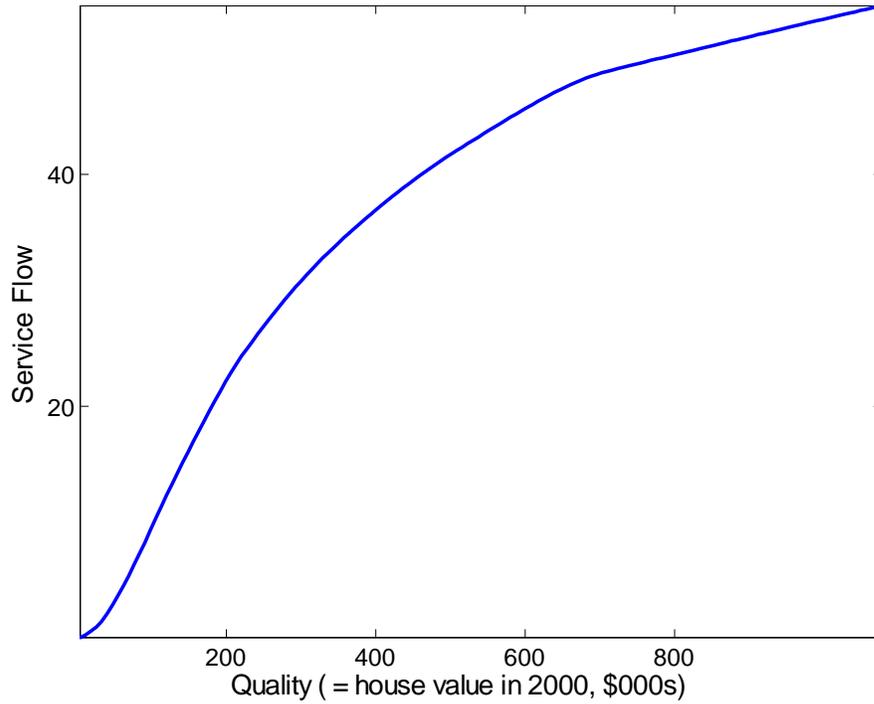


Figure 7: Service flow as a function of house quality (= 2000 house value)

index is the 2000 house price, the figure says that the price of a house is convex in the amount of housing services it provides. Some intuition for this result can be obtained from our analysis of the stylized model in Section 3. In that model, the price function is linear in the service flow if the distribution of service flow across houses is a scaled version of the wealth distribution. In contrast, if the dispersion of the wealth distribution relative to the service flow distribution is larger over a particular quantile range, say the top quintile, than elsewhere, then we would expect the price function to be steeper over that range.

This logic rationalizes the shape of the backed out service flow function. The key pattern in the data is that the wealth distribution has a longer upper tail than the house price distribution and hence, given our convention for the 2000 experiment, than the house quality distribution. For example, the top 10 percent of households own 50 percent of the total wealth but only 15 percent of the total housing wealth in their age group. This difference in tail behavior induces a concave service flow function. Indeed, if the service flow function were linear then rich households in the upper tail would demand houses in the upper tail, which are not available. For markets to clear, some rich households must be induced to choose lower quality houses. This requires a steep increase in the price per unit of service flow at higher house qualities.

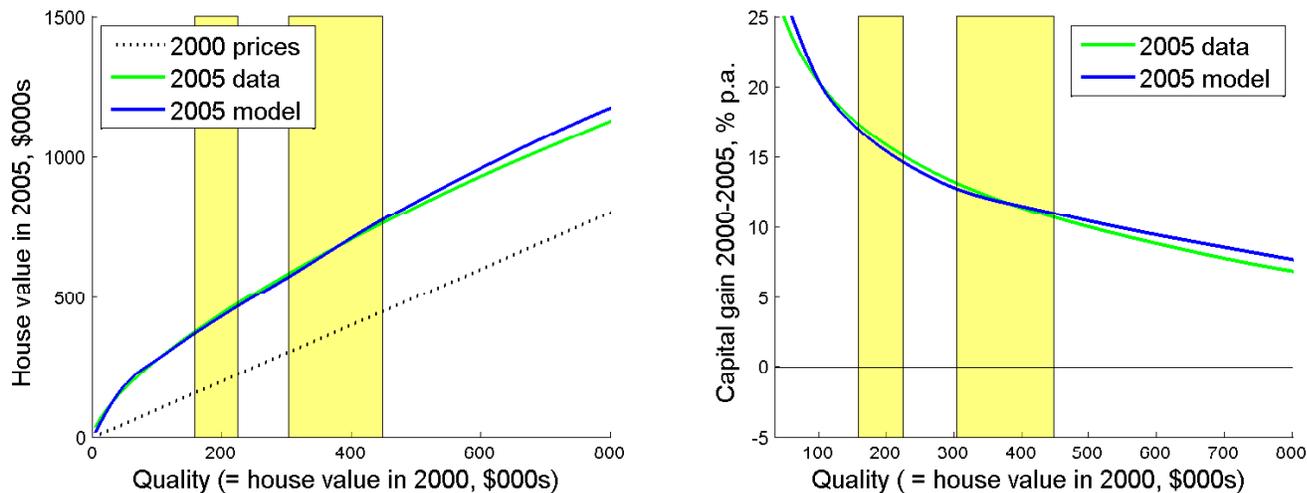


Figure 8: Model results for the year 2005. The left panel shows house prices for 2005. The dashed 45 degree line are 2000 prices. The green line are prices in the data. The blue line are equilibrium prices in the model. The right panel shows capital gains in the data (green) and the model (blue). The shaded areas indicate quintiles of the house quality distribution. The house quality on the horizontal axis is measured in 2005 Dollars.

5.2 Changes in house prices from 2000 to 2005

Figure 8 compares model implied 2005 house prices to those in the data. In both panels, the horizontal axis measures house quality. The left panel shows the 2005 price as a function of quality. The green line is the price function in the data, constructed above in equation (3) from the response of prices to common shocks that affect houses of the same quality. The blue line is the equilibrium price function from the model. The dashed line indicates 2000 prices. It is linear with slope one since our quality index is equal to the 2000 price and all prices are reported in 2005 dollars. In both the data and the model, equilibrium prices of lower quality houses increased more than the prices of high quality houses from the year 2000 to the year 2005, the peak of the boom.

The right panel shows annualized capital gains between 2000 and 2005. For both the model and the data, capital gains are computed as one fifth of the log difference between the 2005 price function and the 2000 price line shown in the left panel. The green line is also equal to the regression line from Figure 1. Capital gains are monotonically declining in quality: they are higher at the low end of the quality spectrum than at the high end. The shaded areas indicate quintiles of the 2005 house quality distribution: in particular, the yellow regions correspond to the second and fourth quintiles.

Overall, the figure shows that the model fits the 2005 price distribution well. For all but the highest quality quantile, capital gains are within one percentage point of the data. For the highest quality houses, the model overpredicts capital gains, although the discrepancy remains below 2

percentage points over the entire range. Changes in the distributions of movers and house qualities, as well as in credit market conditions can thus jointly account for the cross section of capital gains over the boom.

5.3 Properties of the assignment

To understand how the model works, we now consider the assignment of movers to houses. In the stylized model of Section 3, cash on hand was the only dimension of heterogeneity and the assignment could be represented as a line in the plane. In the model considered here, movers differ not only in cash (asset wealth plus income), but also in income and age. Age matters for housing demand if movers' savings and portfolio choice depends on their planning horizon. Income matters (other than through its effect on cash) because it helps forecast future income and thus human wealth.

Figure 9 provides a first impression for how all three dimensions of heterogeneity affect the equilibrium assignment. In both panels, the horizontal axis measures house quality, the vertical axis measures cash and every dot is a mover household in the 2005 ACS. The panels differ only in the color of the dots, which illustrate a second dimension of heterogeneity. In the top panel, color represents age, whereas in the bottom panel color represents the ratio of income to cash.

The cloud of points extends from southwest to northeast: not surprisingly, the model assigns houses of higher quality to households with more cash. If cash were the only relevant dimension of heterogeneity, all dots would be on a line, as for the stylized model of Section 3 (for example, in the bottom left panel of Figure 4). Since the cloud looks very different from this benchmark, we can conclude that cash is not the only dimension that matters in the assignment. Indeed, the figure displays many pairs of movers such that one mover has twice the house quality but the same cash level as the other mover. At the same time, houses of the same quality are frequently bought by pairs of movers such that one has more than twice as much cash as the other.

In the top panel of Figure 9, light blue dots represent the youngest households. For a given quality range, most young households have little cash and thus cluster at the bottom of the cloud. In contrast, pink and violet dots representing the older households scatter towards the top of the cloud – those households have more cash. Comparison of similarly colored dots shows that the assigned quality is more sensitive to cash for younger households. Indeed, for the cloud of light blue dots, the orientation from southwest to northeast is less pronounced than for the cloud of pink and violet dots. Put differently, young households increase house quality more quickly with cash than older households.

In the bottom panel of Figure 9, light blue dots correspond to a higher ratio of income to cash. The light blue dots at the bottom of the cloud represent households with income-cash ratios close

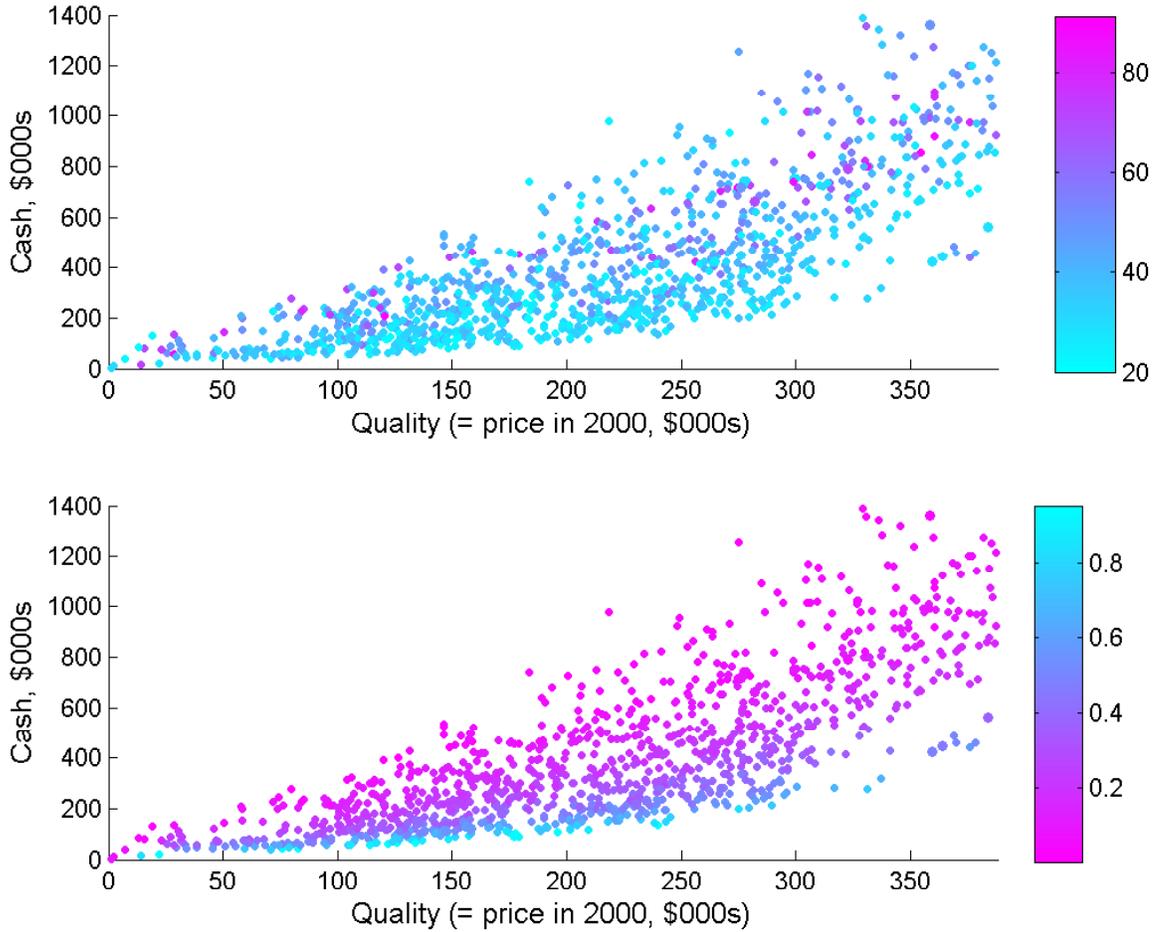


Figure 9: Equilibrium assignment. Both panels are scatter plots of 2005 San Diego ACS observations and their equilibrium assignments. The horizontal axis measures house quality. The vertical axis measures cash (wealth plus income.) The top panel shades dots according to age. The age coloring is indicated on the right bar. The bottom panel shades dots according to income-to-cash ratios. The coloring of income/cash is indicated on the right bar. The size of the dots correspond to their sampling weights.

to one. Those households have virtually no funds other than their current income. In contrast, the pink dots at the top of the cloud represent households with cash worth several times income. Comparison of the colored clouds shows that the assigned quality is more sensitive to cash when the ratio of income to cash is larger. Put differently, households increase house quality more quickly with cash if a larger share of their cash comes out of current income.

The key principle underlying the assignment rule is that households with relatively more human capital optimally hold more housing in their portfolios. To see where it comes from, consider a frictionless portfolio choice problem with two risky assets, housing and human capital. If markets are complete, the solution to such a problem removes exposure to idiosyncratic endowment risk by shorting claims to labor income. If markets are incomplete and claims on labor income cannot be

traded, it still makes sense to remove exposure to endowment risk by shorting a tradable portfolio that mimics labor income. In our model, this mimicking portfolio essentially consists of bonds. At the same time, the collateral constraint implies that shorting bonds requires borrowing against housing.

Optimal portfolio choice thus suggests that households who have more human wealth relative to total wealth buy houses of higher quality. The facts shown in both panels follow directly. On the one hand, labor income is persistent and hence serves a proxy for human wealth, holding fixed age. House quality should thus increase more quickly with cash if the share of labor income in cash is higher. On the other hand, younger households have a longer working life ahead of them and thus larger human wealth, holding fixed labor income. House quality should thus increase more quickly with cash for younger households.

Assignment by age and wealth – comparing model and data

We now investigate whether the data are consistent with the assignment predicted by the model. Table 3 compares the assignment of house quality by cash, income and age in the data and the model. Panels A and B contain numbers for the years 2000 and 2005, respectively. In both panels, the columns labeled I, II, III and IV correspond to four house quality bins: houses worth less than \$150K, between \$150-200K, \$200-400K, and above \$400K, all expressed in terms of prices in the base year 2000. For each quality bin, the rows of the table report key moments of the distribution of movers who buy houses in that bin, namely, median income and cash for young (≤ 35 years) and older movers as well as the top and bottom deciles the cash distribution for the bin.

Higher quality houses are bought by richer households, whether "rich" is measured by income or cash. Over the quality range covered by the first three bins, both measures of wealth actually grow roughly linearly in quality once we condition on broad age groups. Indeed, the first three bins are approximately equally spaced at 75K, 175K and 300K. At the same time, for both young (≤ 35 years) and old (≥ 35 years) households, income and cash increase by similar amounts between bins I and II and between bins II and III. In contrast, there is typically a sharp increase between bin III and bin IV – the top bin that has no upper bound.

The model also predicts that income and cash increase with quality, and that the relationship is close to linear over the first three bins. As a measure of "slope" over that range, consider the average increase from moving up one bin from bin I or bin II. For median income, this slope measure is essentially independent of age: in the data for the year 2000 (2005) it is 19K (20K) for the young and 23K (23K) for the old. The model exhibits the same pattern: slopes for the year 2000 (2005) are 31K (32K) for the young and 31K (40K) for the old. The model is also close to the level of median income for bin II and thus captures the linear relationship quite well.

In contrast to the case of income, the relationship between quality and median cash strongly

depends on age, both for the data and – as expected from Figure 9 – for the model. Indeed, in the data for the year 2000 (2005), the slope is 58K (55K) for the young, but 113K (208K) for the old, a substantial steepening. The model predicts slopes for the year 2000 (2005) of 65K (102K) for the young as well as steeper slopes of 118K (165K) for the old. In addition, the model is again close to the data for bin II. As a result, it also captures the fact that the old have substantially higher levels of cash than the young in all bins.

The dispersion of the cash distributions can be described by the ratio of the bottom decile to the top decile. In the data, this ratio is smallest for bin IV and largest for bin II in both years. Moreover, it decreases for bins I and II between 2000 and 2005, as those low quality bins become more dispersed during the boom. The same patterns are predicted by the model. Quantitatively, the average ratio in 2000 (2005) for the data is 10% (11%) whereas for the model it is 22% (22%).

Standard errors of data moments are reported in Table 3 in parentheses. They are computed without taking into account sampling uncertainty and thus overstate our confidence in the estimated moments.¹⁴ In other words, a check on whether the model predictions fall within two standard error bounds of the estimates is "too tough" on the model. Nevertheless, the model is within two standard error bounds for five medians in Panel A and seven medians in Panel B, out of the sixteen total medians. We conclude that the model performs reasonably well in matching the cross-sectional assignment of quality by measures of wealth.

Optimal portfolios and changes in credit conditions

As discussed above, the model captures key features of the assignment function in the data because younger agents who have more human wealth choose more housing in equilibrium. To illustrate the magnitudes of heterogeneity in portfolios and how it has changed over time, Table 4 reports the ratio of housing wealth to cash by age. This ratio is highest for households under 35 and remains relatively high for households between 35 and 50. Moreover, it increased substantially between 2000 and 2005 for households younger than 50, whereas it changed little for older households.

The model matches closely the level and change in the housing weights of households younger than 50. The change in credit conditions across years is critical for this result. Indeed, when we recompute the model with the same distributions of mover characteristics and houses, but with the interest rate and downpayment constraints set to their 2000 values, the housing weight falls to 74% for households younger than 35 and to 48% for households between 35 and 50. In other words, we

¹⁴Addressing sampling uncertainty via replication weights provided by the Census would have two effects for our exercise. On the one hand, errors around data medians would increase. On the other hand, we would also obtain standard errors around medians predicted by the model. This is because computation of the equilibrium of the takes the distribution of mover characteristics as an input. Each set of replication weights would thus lead to a different mover distribution and hence a different set of model predictions. This second effect makes a more accurate treatment of uncertainty computationally very costly in our context and is therefore omitted.

are almost back to the 2000 numbers (61% and 43%, respectively).

TABLE 3: ASSIGNMENT OF HOUSE QUALITIES IN DATA AND MODEL

House quality bins	Data				Model			
	I	II	III	IV	I	II	III	IV
PANEL A: YEAR 2000								
Median Income (in thousands)								
aged \leq 35 years	48.5 (1.8)	68.7 (2.5)	88.1 (4.0)	128.5 (7.1)	38.3	67.6	100.3	206.3
aged $>$ 35 years	44.0 (2.2)	63.4 (2.3)	90.3 (4.5)	152.3 (8.5)	33.4	67.4	95.9	182.2
Median Cash (wealth plus income, in thousands)								
aged \leq 35 years	112.0 (5.4)	169.7 (7.8)	284.6 (15.3)	646.8 (39.7)	93.2	158.5	361.9	1,551.4
aged $>$ 35 years	172.3 (9.2)	284.8 (15.4)	496.4 (27.6)	1,141.8 (71.5)	122.9	241.1	547.1	1,721.0
Percentiles of the Cash Distribution (in thousands)								
bottom 10%	60.2	94.9	146.0	310.9	59.6	114.5	221.0	763.0
top 10%	471.1	721.8	1,443.9	3,941.9	205.6	362.5	1,007.1	4,378.9
PANEL B: YEAR 2005								
Median Income (in thousands)								
aged \leq 35 years	61.3 (4.0)	73.6 (3.5)	101.9 (8.1)	132.5 (7.1)	51.0	82.0	115.7	137.4
aged $>$ 35 years	45.9 (4.3)	78.5 (4.9)	91.7 (5.7)	144.7 (12.5)	35.7	76.4	96.8	244.6
Median Cash (wealth plus income, in thousands)								
aged \leq 35 years	203.4 (18.0)	258.5 (22.5)	421.3 (43.8)	735.2 (76.4)	136.7	238.6	526.0	1,689.8
aged $>$ 35 years	251.6 (29.5)	459.7 (45.2)	712.2 (70.9)	1,645.6 (187.7)	196.3	360.6	749.3	2,601.8
Percentiles of the Cash Distribution (in thousands)								
bottom 10%	79.1	125.3	180.4	391.3	67.0	146.5	314.9	1,093.0
top 10%	714.4	1,099.0	1,733.7	5,582.6	324.8	553.8	1,244.4	6,262.4

Note: This table reports moments of the assignment of house quality to income and cash (wealth plus

current income) in the data and in the benchmark model. Panel A contains results for the year 2000, while Panel B reports results for the year 2005. Across both panels, house quality is measured in four bins. Bin I contains houses worth less than \$150K in the 2000 base year. Bin II contains houses worth between \$150-200K. Bin III contains houses worth \$200-400K. Bin IV contains houses above \$400K. All dollar amounts are reported in 2005 Dollars. The medians are computed for the households who bought a house in the indicated bin. The row "aged \leq 35 years" ("aged $>$ 35 years") reports the medians of households aged 35 years or younger (above 35 years). The row "bottom 10%" ("top 10%") reports the 10th (90th) percentile of the cash distribution. The left columns show the assignment in the data computed from the 2000 Census and the 2005 American Community Survey. The right columns show the assignment in our benchmark model.

TABLE 4: HOUSING WEALTH RELATIVE TO CASH (WEALTH PLUS INCOME)

	Age			
	below 35	35-50 years	50-65 years	above 65
Panel A: Year 2000				
Data	0.632	0.459	0.369	0.317
Model	0.613	0.435	0.385	0.403
Panel B: Year 2005				
Data	0.968	0.677	0.317	0.387
Model	0.959	0.627	0.423	0.522

5.4 Understanding the cross section of capital gains

Figure 10 presents results for two hypothetical scenarios in order to illustrate the different forces shaping the cross section of capital gains. For both exercises, we start from the 2000 distributions of houses and mover characteristics as well as 2000 credit conditions. The left hand panel changes only the distribution of houses to its shape in 2005. It is thus analogous to the experiment reported in Figure 5 for our simple illustrative model. The results are qualitatively similar to that earlier experiment: a shift towards more low quality houses increases capital gains at the low end. It is clear however, that the distributional shift by itself would not be sufficient to explain the cross section of capital gains quantitatively. In particular, gains for the top quintile of houses are close to zero.¹⁵

The right hand panel of Figure 10 changes only credit conditions, again starting from the 2000

¹⁵The exercise shifts only the distribution of houses, leaving mover characteristics unchanged. An exercise that shifts only the distribution of mover characteristics has very small effects on equilibrium capital gains and is not reported here.

environment. It is thus similar in spirit to the experiment reported in Figure 6. The analogy is not as clean as for a distributional change, however, because downpayment constraints and interest rates have partly offsetting effects on households. On the one hand, lower downpayment constraints are more relevant for poor households who are close to their collateral constraint. They account for the sharp increase in capital gains at the low end. On the other hand, a given percentage drop in interest rates has strong effects on present values computed with the lending rate which is lower already in 2000. This effect helps prop up capital gains also at the higher end.

The appendix presents a number of other exercises that explore the sensitivity of the results to our assumptions. First, we consider what happens when households in 2005 are able to perfectly foresee future house prices and credit conditions. This means that households in 2005 anticipate that after one model period (three years) house prices, downpayment constraints and mortgage spreads revert to their 2000 levels. The results show that if households had perfectly foreseen conditions during the housing bust of the Great Recession, the house price boom would have been substantially smaller. However, the boom would have generated the same cross sectional patterns in capital gains, with capital gains being roughly 10% per year for low quality houses and 0% at the upper end of the quality distribution.

We also investigate the role of our assumption that the service flow function remains the same over time, up to a growth factor. Formally, we compute a new service flow function that exactly matches 2005 observed house prices. This computation also uses *(i)* 2005 distributions for house qualities and mover characteristics, *(ii)* 2005 credit conditions, and *(iii)* constant capital gain expectations. The new service flow function is steeper for qualities below 400K, which makes the price function less steep in that region compared to the benchmark in Figure 8. We also show that even if differential home improvement is allowed, credit conditions play an important role in explaining the cross section of capital gains.

6 Conclusion

The extraordinary housing boom experienced by the United States in the early 2000s has generated an active literature trying to understand its roots. Financial innovation, changes in relative housing supply, shifts in the income distribution and exuberant expectations have all been discussed as candidate explanations. An exciting feature of this research is that it employs detailed cross sectional data to compare implications of different hypotheses. A natural starting point for the analysis of cross sectional data is a model of a homogenous housing market. Comparative static predictions from such a model are easily compared to data on house prices and trading across geographical areas, for example.

The approach taken by this paper is slightly different: we view a narrow geographical area as a

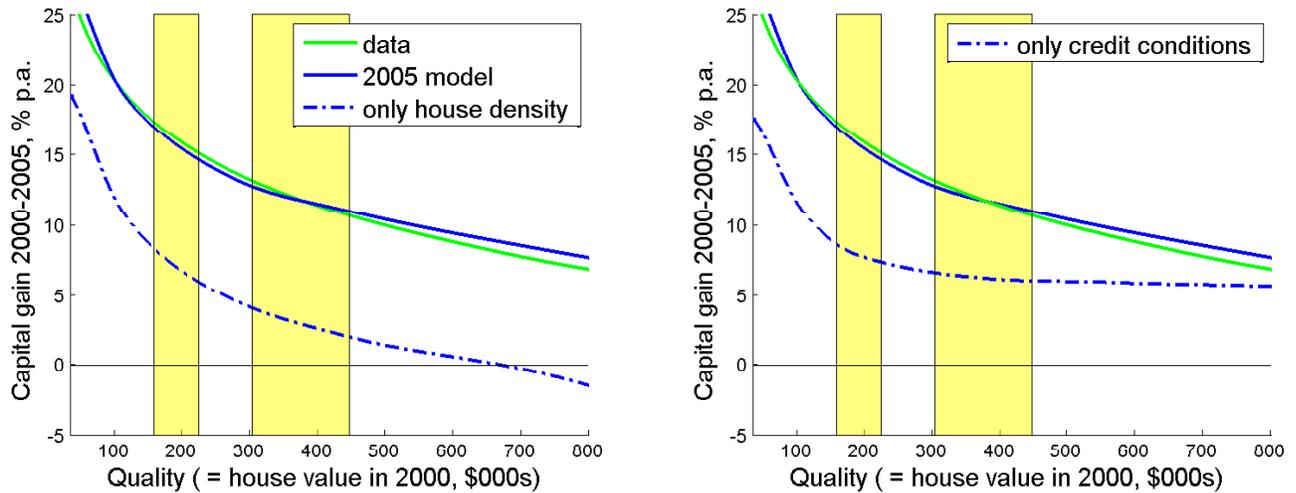


Figure 10: Equilibrium capital gains 2000-2005 in the data (green line) and the model (solid blue line) together with two hypothetical scenarios (dotted blue line in the two graphs). Both scenarios start with model inputs from the year 2000 and compute equilibrium prices for the year 2005. The left panel adds a 2005 house quality distribution. The right panel adds 2005 credit conditions.

set of quite diverse but nevertheless interconnected housing markets. From this perspective, we can learn about candidate explanations for the boom by assessing their simultaneous effect on the entire distribution of capital gains. For example, if cheap credit matters, then we should see stronger price increases at the low end, as would be true if markets were fully segmented. However, within a metro area, stronger demand by low quality buyers is likely to “spill over” to medium qualities and from there in turn to high qualities. Using a model that allows for spillover effects thus provides a more complete assessment of what a given candidate explanation entails.

Quantitative assignment models should help understand housing market dynamics in other contexts. One interesting episode is the bust that immediately followed the boom studied in this paper. As Table 1 showed, higher capital gains at the low end during the boom were reversed by higher capital losses during the bust. It is natural to ask to what extent more stringent credit conditions – especially for low income borrowers – interacted with changes in the income and house distribution during the recession. Even more recently, the dramatic recovery of the housing market in the San Francisco Bay Area was concentrated in the high end market segments of Silicon Valley, begging the question of how a sectoral shock to the IT sector is transmitted to the entire cross section of markets.

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Appendix for online publication

A San Diego County Transactions Data

In this appendix we describe our selection of sales and repeat sales. We begin by describing our sample of sales which not only forms the basis for selecting repeat sales but is also used to illustrate the shift in distributions in Section 2. Our goal is to compile a dataset of households' market purchases of single-family dwellings. We start from a record of all deeds in San Diego County, 1999-2008 and then screen out deeds according to three criteria.

First, we look at qualitative information in the deed record on what the deed is used for. We drop deed types that are not typically used in arms length transfers of homes to households in California. In particular, we keep only grant deeds, condo deeds, corporate deeds and individual deeds. The most important types eliminated are intrafamily deeds and deeds used in foreclosures. Even for the types of deeds we keep, the deed record sometimes indicates that the transaction is not "arms length" or that the sale is only for a share of a house – we drop those cases as well.

Second, we drop some deeds based on characteristics of the house or the buyer. We use only deeds for which a geocode allows us to precisely identify latitude and longitude. We eliminate deeds that transfer multiple parcels (as identified by APN number.) Information about property use allow us to eliminate second homes and trailers. To further zero in on household buyers, we eliminate deeds where the buyer is not a couple or a single person (thus dropping transaction where the buyer is a corporation, a trust or the beneficiary of a trust.)

Third, we drop some deeds based on the recorded price or transaction dates. We drop deeds with prices below \$15,000 or with loan-to-value ratios (first plus second mortgage) above 120%. We also consolidate deeds that have the same sales price for the same contract date. We drop deeds that have the same contract date but different prices.

Our repeat sales sample is used to estimate our statistical model of price changes in Section 2.2. A repeat sale is a pair of consecutive sales of the same property within the above sales sample. Since we are interested in long term price changes, we want to avoid undue influence of house flipping on our estimates. We thus drop all pairs of sales that are less than 180 days apart. To guard against outliers, we drop repeat sales with annualized capital gains or losses above 50%.

B Robustness of facts on capital gains

Table B.1 reports additional results for the repeat sales model that incorporate zip code and census tract level information. Regression (i) reports the basic regression of capital gains on the own

initial 2000 price p_t^i in logs from Figure 1. The regression has a slope coefficient of -0.060 with a standard error 0.0014 and an R^2 of 57.1% . Regression (ii) adds the initial zip code median (again, in logs) p_t^{zip} as regressor. The point estimate of the coefficient on the initial own price is basically unchanged (-0.057 versus -0.060); the difference is not statistically significant. The estimated coefficient on the zip-code median is statistically significant, but -0.011 is economically small. The added explanatory power of the zip code median is tiny, the R^2 goes from 57.1% to 57.5% . The regression (iii) on the zip-code median alone (iii) gives an R^2 of 20.6% . Regressions (iv) and (v) are analogous to (ii) and (iii), but they use census tract rather than zipcode as the geographical area. The results are quite similar. Regression (v) uses only the census-tract medians with an R^2 of 28.5% .

TABLE B.1 GEOGRAPHIC PATTERNS IN REPEAT SALES MODEL

		const.	$\log p_{2000}^i$	$\log p_{2000}^{zip}$	$\log p_{2000}^{census}$	R^2
(i)	$\log p_{2005}^i - \log p_{2000}^i$	0.899 (0.018)	-0.060 (0.002)			0.571
(ii)	$\log p_{2005}^i - \log p_{2000}^i$	1.000 (0.035)	-0.057 (0.002)	-0.011 (0.003)		0.575
(iii)	$\log p_{2005}^i - \log p_{2000}^i$	1.016 (0.048)		-0.069 (0.004)		0.206
(iv)	$\log p_{2005}^i - \log p_{2000}^i$	0.879 (0.024)	-0.062 (0.002)		0.004 (0.003)	0.572
(v)	$\log p_{2005}^i - \log p_{2000}^i$	0.837 (0.031)			-0.056 (0.003)	0.285
(vi)	$\log p_{2005}^{zip} - \log p_{2000}^{zip}$	1.014 (0.068)		-0.070 (0.006)		0.672
(vii)	$\log p_{2005}^{census} - \log p_{2000}^{census}$	1.038 (0.034)			-0.071 (0.003)	0.606

Note: This table reports results from regressions of the capital gain from 2000 to 2005 in the price series indicated on the left-hand side on the regressors indicated on the headers of the columns. These cross sectional regressions involve

individual house prices p_t^i from houses that were repeat sales in the two years 2000 and 2005, zip code medians p_t^{zip} , and census tract medians p_t^{census} in San Diego County.

Regression (vi) runs the capital gains in the zip-code medians on the initial zip-code medians. The results are comparable to row (i) with a slope coefficient of -0.070 , a somewhat higher standard error of 0.0055 , and a higher R^2 of 67.2% . Regression (vii) does the same exercise for census tracts, again with similar slope as row (i).

Figure 11 plots the repeat sales observations from Figure 1 with the 2005 log price on the y-axis. The black line is the predicted value from a linear regression of 2005 log prices on 2000 log prices. The green line is the predicted value from a nonparametric regression, using a Nadaraya-Watson estimator with a Gaussian kernel and a bandwidth of 0.15 . The nonparametric regression line is strictly increasing in the initial 2000 price. This monotonicity property implies that the relative ranking of houses by quality according to the nonparametric regression is the same as the relative ranking according to the linear regression.

The nonparametric regression line is close to linear for a large range of house values, with the largest deviation at the low end. This deviation does not matter for our approach, because we use the pricing model only to derive an ordinal index. The absolute amount of service flow due to a house of a certain ordinal quality is backed out using the structural model. Section 5.1 uses 2000 house prices to back out a service flow function for that year and assumes a constant rate between 2000 and 2005 to derive the 2005 service flow function. Section E uses 2000 house prices and 2005 house prices to back out service flow functions for the two years, respectively.

C Details on quantitative implementation

This appendix provides details on the calculations of home improvements, house quality and wealth reported in the text.

Improvements

The 2002 American Housing Survey contains data on home improvements in San Diego County. Table C.1 shows the means and medians of annual improvement expenses in San Diego as a percent of house values. We find that San Diego homeowners spend an amount equal to roughly 1% of their house value on improvements each year. The mean percentage spent on improvements is 2% for homes in the lowest bin, worth less than $\$50,000$. However, this higher mean is estimated imprecisely. A test that the mean improvement percentage in the lowest bin and homes in the next bin (worth between $\$50,000$ and $\$100,000$) are identical cannot be rejected at the 10% level. A joint test whether mean improvements across all bins are equal can also not be rejected. We also test whether the data are drawn from populations that have the same median and cannot reject.

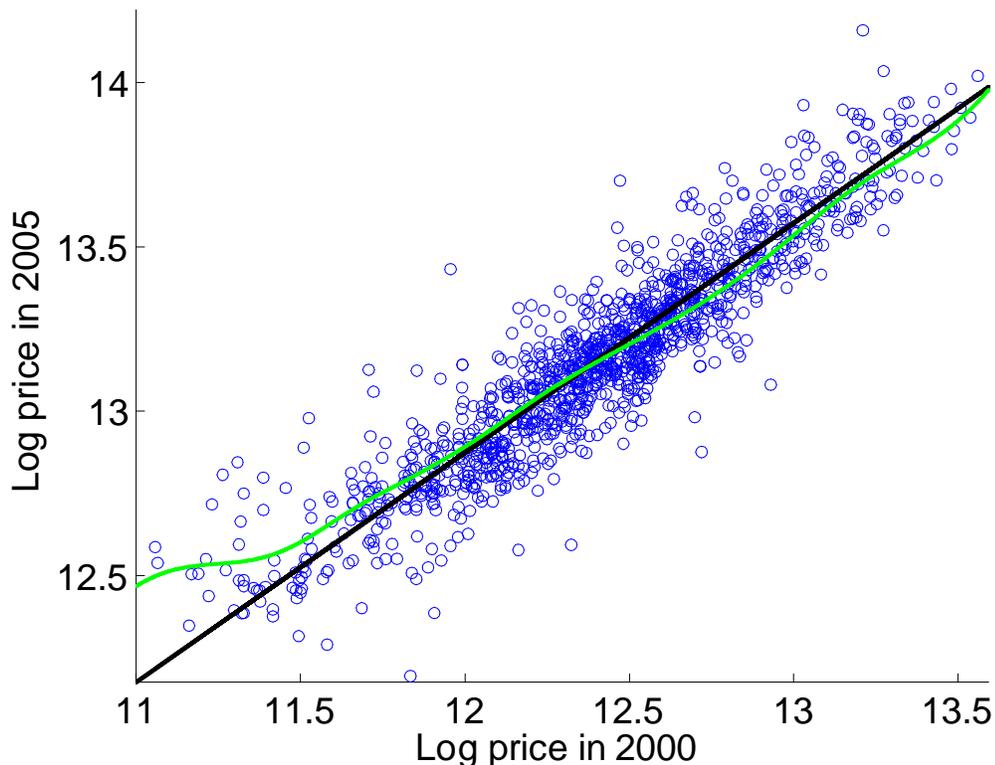


Figure 11: Repeat sales in San Diego County, CA, during the years 2000-2005.

TABLE C.1: HOME IMPROVEMENTS IN SAN DIEGO

House Value (in thousands)

	<50	50-100	100-150	150-200	200-300	300-500	500-1,000	>1,000
Improvements (in percent)								
mean	2.11	1.05	0.73	0.75	0.95	0.96	0.8	1.1
	(0.54)	(0.32)	(0.11)	(0.09)	(0.13)	(0.12)	(0.13)	(0.30)
median	0	0.07	0.08	0.10	0.14	0.19	0.13	0.13

Note: This table contains the estimated means of home improvement measured as percent of house value. These statistics are computed for observations within the house price bins indicated on the top of the table. The data are the San Diego County observations of the 2002 American Housing Survey on ‘rac’ which measures the cost of replacements/additions to the unit. The ‘rac’ amount is divided by two, because the survey asks about expenses within the last two years. Standard errors (in brackets) are computed using Jackknife replications.

Census house values

The Census data does not contain actual prices but rather price ranges, including a top range for houses worth more than one million dollars. The topcoded range contains 9.6% of houses in 2005 and 1.8% of houses in 2000. To obtain cross sectional distributions of houses sold in a given year, we fit splines through the bounds of the Census house binds. Let p^c a vector that contains those bounds, as well as a lower bound of zero and an upper bound. We can obtain a continuous distribution for every upper bound by fitting a shape-preserving cubic spline through $(p^c, G_0(p^c))$. We choose the upper bound such that the median house value in the topcoded range equals the median in that range in our transaction data. To prepare the imputation of wealth (described below) we set a household's housing wealth to the midpoint of its bin, and we use the median of the topcoded range for the top bin.

Imputation of wealth

For age and income, we use age of the household head and income reported in the 2000 Census (for $t = 2000$) and 2005 ACS (for $t = 2005$). We are thus given age and income, as well as a survey weight, for every survey household. However, Census data do not contain wealth. We construct a conditional distribution of wealth using data from the Survey of Consumer Finances (SCF). We use the 1998 and 2004 SCF to build the conditional distributions for 2000 and 2005, respectively.

We use a chained equations approach to perform imputations. The estimation is in two steps. In the first step, we use SCF data to run regressions of log net worth on log housing wealth, a dummy for whether the household has a mortgage and if yes, the log mortgage value, and log income for each age decade separately. In the second step, we use a regression switching approach described in Schenker and Taylor (1996), and implemented in the Stata commands 'mi' or 'ice'. The procedure draws simulated regression coefficients from the posterior distribution of the coefficients estimated using the SCF data. Using these simulated coefficients and the observed covariates in the census data, a predicted value for log networth is calculated for each census household. The imputed log networth for each census household is then randomly drawn from a set of SCF households whose actual log networth is close to the predicted log networth of the missing observation.

By repeating this second step multiple times (i.e. drawing multiple sets of simulated coefficients), we can generate multiple imputed observations for each original census observation. We choose to create three different imputations, following the recommended quantity for this kind of procedure. A survey weight for each new household is obtained by dividing the original survey weight by three.

D Computation

This section describes the computational methods used to solve the quantitative model in Section 4. We need to (i) solve a household problem with a continuum of housing assets with different service flows and prices and (ii) solve for the equilibrium objects (service flow for 2000, and price for 2005) given the three-dimensional distribution of household characteristics and the one-dimensional distribution of house qualities.

Both the price and service flow functions are defined on the interval of available house qualities $[\underline{h}, \bar{h}]$. Both functions are parametrized as shape-preserving cubic splines, defined by a set $\{h_i, s_i, p_i\}_{i=1}^I$, where $h_i \in [\underline{h}, \bar{h}]$ are the break points, $p_i \in [0, \infty)$ is the price p_i at h_i and s_i is the service flow at h_i . We impose strict monotonicity on both functions, that is, $h_j > h_i$ implies $p_j > p_i$ and $s_j > s_i$. Denote the approximating price and service flow functions by $\hat{p}(h)$ and $\hat{s}(h)$, respectively. The intertemporal household problem is tractable even with a continuum of assets because agents expect permanent shocks to not alter relative prices across houses. The price function expected in the future equals the cumulative permanent innovation to house prices plus the price function $\hat{p}(h)$.

To accurately capture the covariation in the three mover characteristics (age, income and wealth), we use the distribution derived from the Census and SCF using the imputation procedure in Appendix C. For every survey household i at date t , we have a tuple (a_{it}, y_{it}, w_{it}) as well as a survey weight. We solve the household problem for every survey household i and obtain his preferred house quality. We then use the survey weights to construct a cumulative distribution function for house quality. In equilibrium, this cdf must be equal to the house quality cdf from the data, shown in Figure 2. The equilibrium object (price or service flow) is found by minimizing a distance between those cdfs.

Household problem

The solution to the household problem is calculated using finite-horizon dynamic programming. Value and policy functions are approximated by discretizing the state space on a fine grid. Consider the optimization problem faced by a household of age a , with cash w as defined in equation (16), income y , and house of quality h . Each period, the household receives an exogenous mobility shock: $m = 1$ indicates that the household must move and $m = 0$ otherwise. The vector of state variables at time t is

$$x_t = [a_t, y_t, w_t, m_t, h_t].$$

The value function at time t is denoted $v(x_t)$. Income is a separate state variable even though the only shocks to income are permanent. This is because house prices are hit by shocks other than income shocks – the common approach of working with the wealth/income ratio and house/income ratio as state variables does not apply.

It is helpful to separate the household's moving decision from the other choices he makes conditional on moving or staying. Consider first a household who is moving within the period. He decides how to allocate cash on hand (which could come from a prior sale of a house) to consumption, housing or bonds, subject to the budget and collateral constraints. Denote the "mover value function" for this problem by v^m ; it depends on the state as well as the approximating price and service flow functions. Consider next a household who is staying in a house of quality h . He decides how to allocate cash on hand to consumption or bonds, again subject to budget and collateral constraints. A stayer household is thus allowed to change his mortgage – this assumption is appropriate for the boom period where refinancing and home equity loans were common. Denote the stayer value function by v^s .

A homeowner who lives in a house of quality h and who does not have to move ($m = 0$) has the option of either selling the house and incurring the transaction cost for selling, or staying in the same house. The selling household faces the same optimization problem as a moving household, with cash adjusted for the sales transaction costs. The optimization problem of the staying household is characterized by the stayer value function we defined above. Thus the value function of the owner household v^o is the maximum of both options

$$v^o(a, y, w, h; \hat{p}, \hat{s}) = \max \{v^s(a, y, w, h; \hat{p}, \hat{s}), v^m(a, y, w, h; \hat{p}, \hat{s})\}.$$

The beginning-of-period value function v takes into account both forced moves ($m = 1$) and endogenous moves:

$$v(x) = m v^m(a, y, w; \hat{p}, \hat{s}) + (1 - m) v^o(a, y, w, h; \hat{p}, \hat{s})$$

We specify separate approximating functions for $v^m(\cdot)$, $v^o(\cdot)$, as well as the housing policy function $h^m(a, y, w; \hat{p}, \hat{s})$ associated with $v^m(\cdot)$. Since the downpayment constraint may induce kinks in the cash dimension w , we perform a discrete approximation of both functions separately for each age. In particular, for each age a , we specify a two-dimensional grid in (y, w) -space for the mover function $v^m(\cdot)$, and a three-dimensional grid in (h, y, w) -space for the stayer function $v^s(\cdot)$. We then maximize the value function at each grid point by searching over the set of all feasible choices at that point. To capture the effect of the downpayment constraint as precisely as possible, the grid in the cash dimension has a higher density of points for low levels of cash.

Specifically, we use 25 grid points each for cash and income dimensions, and 175 grid points for the housing dimension of the owner value function. For income and cash, 15 equally spaced points are used to cover the interval between \$0 and \$600K, and the remaining 10 points are equally spaced between \$600K and the upper bounds of the grids. The upper bounds are set to the 98th percentile of the respective distribution in the data. Policy functions are linearly extrapolated for those observations above the upper bounds.

The discrete choice of moving in combination with the transaction cost of selling introduces a “region of inaction” for the owner households. In absence of the transaction cost, the mover and owner value functions would be identical, since we have defined cash to include the sales price of the house. Thus, without selling frictions, there is a unique optimal house quality choice $h^m(a, y, w; \hat{p}, \hat{s})$ for each level of cash and income. In the presence of transaction costs, however, the homeowner may decide to stay in a house of quality different from the frictionless optimum $h^m(a, y, w; \hat{p}, \hat{s})$. This is the case if the endowed house h is not too far from $h^m(a, y, w; \hat{p}, \hat{s})$ given the size of the transaction cost. More precisely, for a given level of transaction cost ν , there exists an interval $[\underline{h}(a, y, w; \hat{p}, \hat{s}, \nu), \bar{h}(a, y, w; \hat{p}, \hat{s}, \nu)]$ around the optimal mover choice $h^m(a, y, w; \hat{p}, \hat{s})$, such that – if the endowed quality h is located within this interval – the owner will optimally stay in the current house. Intuitively, if the endowed quality h is close to the frictionless optimum, then saving the transaction cost outweighs the benefit of adjusting the consumption bundle over housing and other goods.

We use this structure of the problem to efficiently compute the owner function $v^o(a, y, w, h; \hat{p}, \hat{s})$. We first solve the mover problem by searching over all feasible choices for each combination of age a , income y and cash w to obtain $h^m(a, y, w; \hat{p}, \hat{s})$. We then find the bounds of the inaction interval $[\underline{h}(a, y, w; \hat{p}, \hat{s}, \nu), \bar{h}(a, y, w; \hat{p}, \hat{s}, \nu)]$ for each combination of age a , income y , and cash w . We do this by checking for different house quality levels whether a household with characteristics (a, y, w) who is endowed with quality h would prefer to stay in house h instead of selling the current house and buying the mover optimum $h^m(a, y, w; \hat{p}, \hat{s})$. We start this search at the mover optimum $h^m(a, y, w; \hat{p}, \hat{s})$, and then search on a fine grid upwards and downwards from this point in the house quality space. In either direction, once we have found a house quality level at which selling and moving is preferred over staying, we know that we have found the bound of the inaction region. This procedure minimizes the number of optimization problems we need to solve to compute the owner value function.

Figure 12 plots the policy function for a young mover (aged 28 years). Since age a is fixed, the policy function depends on the income-cash ratio y/w and cash w . Higher y/w ratios mean a larger share of human wealth out of total wealth. Movers with higher y/w ratios choose a riskier portfolio with more housing. Housing demand is also increasing in cash w . In a dynamic programming problem with collateral constraints and linear pricing, we expect the policy function to be convex in the constrained region and then to become linear for higher income-cash ratios and cash levels. Figure 12 shows more curvature throughout the state space, because the price of house quality is nonlinear.

Older movers have policy functions that look qualitatively similar to Figure 12. The older movers choose lower house qualities, especially at low income-cash levels and overall cash levels. Moreover, their policy function reaches the unconstrained region sooner, i.e. at lower values of the two state

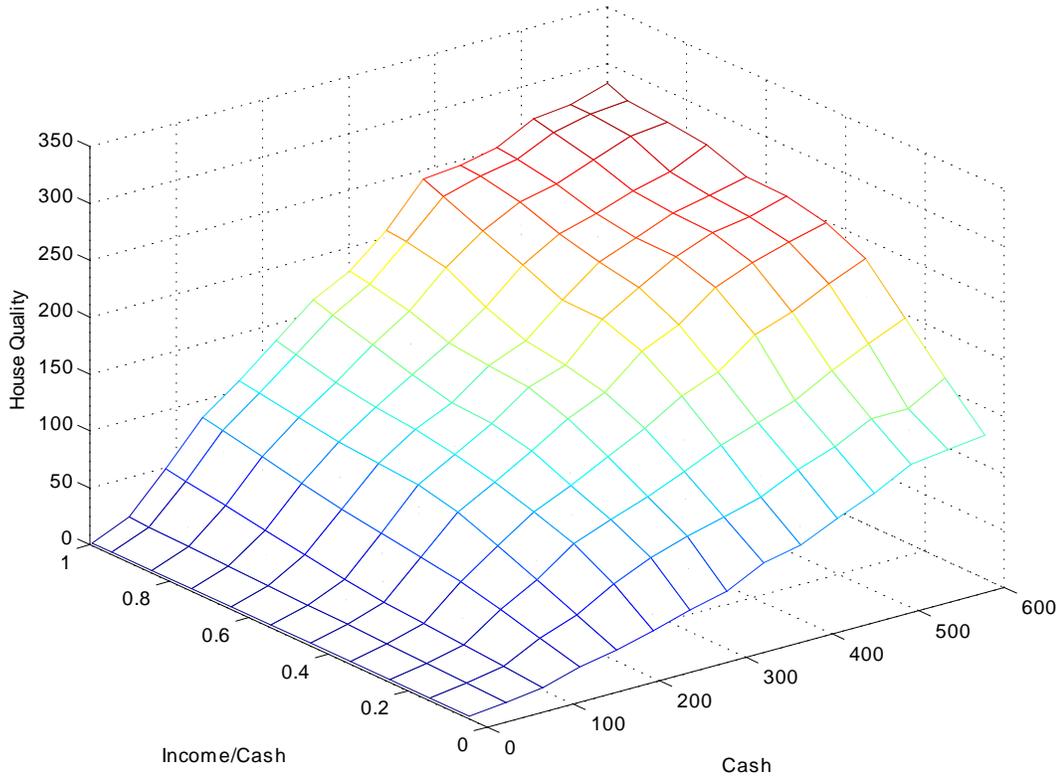


Figure 12: Policy function for young mover

variables.

Market clearing

Given a sample of movers with characteristics $\{a_{it}, y_{it}, w_{it}\}_i$ as well as approximating price and service flow function \hat{p} and \hat{s} , we calculate the model-implied optimal house qualities as

$$\hat{h}_{it} = h^m(a_{it}, y_{it}, w_{it}; \hat{p}, \hat{s}).$$

We thus obtain a sample of optimal house quality choices $\{\hat{h}_{it}\}_i$. We then use the survey weights for the movers to compute an empirical cdf of house quality. We smooth this cdf using a cubic spline. We call the resulting cdf $\hat{G}^{dem}(h; \hat{p}, \hat{s})$ the demand cdf as it represents optimal housing demands at the given price and service flow functions.

In equilibrium, the demand cdf must equal the quality cdf from the data. The latter is also given as a cubic spline, \hat{G} say, as explained in Appendix C. To get a measure of distance between the demand cdf and the data quality cdf, we define a set of test quantiles $\{g_j\}_{j=1}^{N_G}$, $g_j \in (0, 1)$ and compute

$$\sum_{j=1}^{N_G} \left\{ \hat{G} \left(\left[\hat{G}^{dem} \right]^{-1} (g_j; \hat{p}, \hat{s}) \right) - g_j \right\}^2. \quad (\text{D-1})$$

For our exercises we need to find the equilibrium object (price or service flow), taking as given

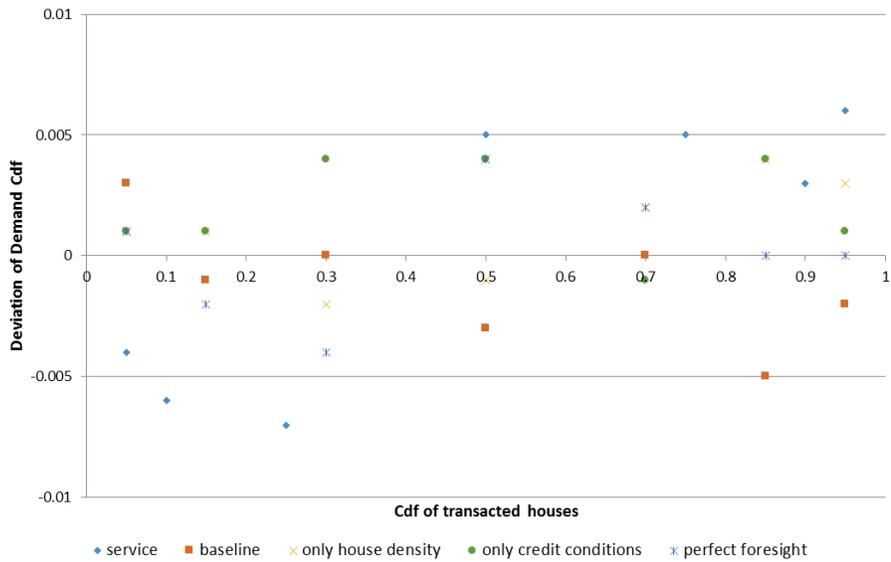


Figure 13: Errors in market clearing conditions

the respective other function (service or price). In each case, our algorithm chooses the spline coefficients of the equilibrium function to minimize the distance (D-1). For the reported results we use 7 break points and the test quantiles are the nine deciles between 10% and 90% as well as the 5-th and 95-th percentiles.

Figure 13 shows that the errors are within one percentage point at every test quantile. The errors labeled "service" are for the results in Figure 15. The "2005 model" errors are for the results in Figure 8. The "only house density" and "only credit conditions" errors are for the two models in Figure 10, respectively. The "const. exp. cap gains" errors are for Figure 14.

E Sensitivity to assumptions on expectations and service flow

This appendix checks the sensitivity of our results with respect to our assumptions on expectations and the service flow function. Our model assumes that households expect favorable credit market conditions (in particular, low downpayments and spreads) to remain in place and house prices to grow at trend. While such expectations are consistent with survey evidence for the peak of the boom in 2005, they were of course disappointed during the Great Recession. To examine the sensitivity of our results to expectations of future market conditions, we thus consider a "perfect foresight" scenario designed to capture recent developments in housing and financial markets.

The perfect foresight scenario retains 2005 mover and house distributions. However, households now expect that, after three years (or one model period), *(i)* downpayment constraints and mortgage spreads to return to their 2000 benchmarks after three years, *(ii)* house prices return to 2000 prices plus trend after three years, *(iii)* the volatility of idiosyncratic shocks to housing returns increases to 11.8% from 9%. Households also expect that *(iv)* interest rates remain permanently low at 1%. Figure 14 displays equilibrium capital gains under perfect foresight.

The results show that if households had perfectly foreseen conditions of the housing bust in the Great Recession, the house price boom would have been substantially smaller. However, the boom would have generated the same cross sectional patterns in capital gains: for low quality houses, 2000-5 capital gains rise above 10% per year, about 40% of the total observed gain. This happens even though capital gain expectations under perfect foresight are actually worse for low quality houses. For low quality buyers, current favorable credit conditions thus outweigh pessimistic expectations of future market developments.

Our model also assumes that the service flow function remains the same over time, up to a growth factor. To check the importance of credit conditions under alternative assumptions on this function, we compute a new service flow function that exactly matches 2005 observed house prices. This computation also uses *(i)* 2005 distributions for house qualities and mover characteristics, *(ii)* 2005 credit conditions, and *(iii)* constant capital gain expectations. The left panel of Figure 15 compares the benchmark (blue) and the service flow function that exactly matches 2005 house prices (green.) The new service flow function grows faster for qualities below 400K, which helps match 2005 prices. The right panel of Figure 15 shows the resulting capital gains. By definition, the model-implied capital gains are identical to those in the data.

To again isolate the importance of credit conditions, we now recompute the model with the new service flow function but under 2000 credit conditions. The result is the dashed line in the right panel of Figure 15. It can be compared to the right hand panel in Figure 10 which also displays a change in credit conditions alone. In both cases cheaper credit increases capital gains by similar

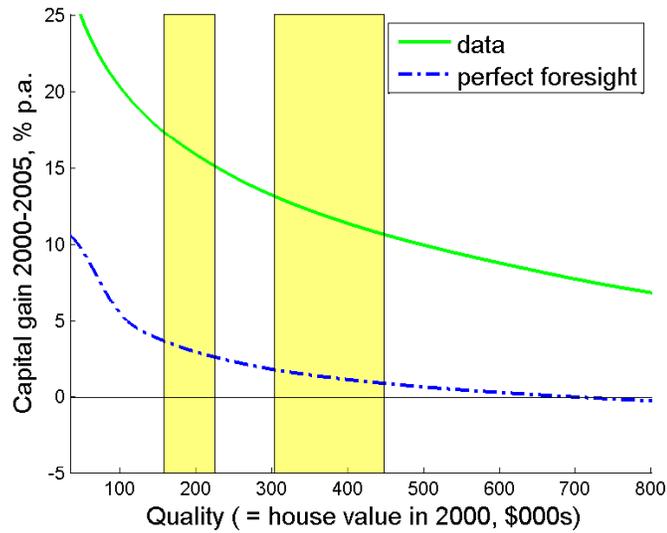


Figure 14: Model Results for 2005 under perfect foresight scenario. The green line represents capital gains in the data, while the dotted blue line shows the model counterpart.

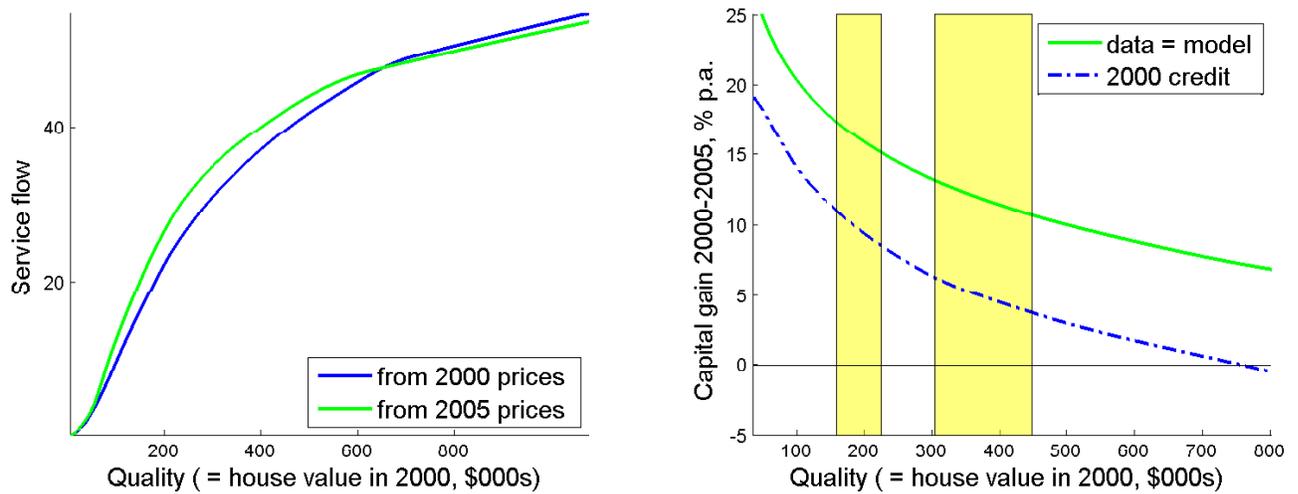


Figure 15: The left panel plots two service flow functions. The blue line matches 2000 house prices as in the benchmark. The green line is a new service flow function that matches 2005 house prices. The right panel shows capital gains under the new service flow function, which are identical to the data. The dashed line computes equilibrium prices with the new service flow function and 2000 credit conditions.

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