

MAE 180A: Spacecraft Guidance I, Summer 2009

Homework 1

Due Tuesday, July 6, in class.

Guidelines: Please turn in a *neat* and *clean* homework that gives all the formulae that you have used as well as details that are required for the grader to understand your solution. Show all work. Required plots should be generated using computer software such as Matlab or Excel. Answers should be written in the blank spaces provided in these homework sheets. Use the back of the page in case you need additional space (not recommended to use more space than provided), for which a clear indication should be written to warn the reader of the presence of text there. Vector quantities are denoted in **bold** letters in what follows.

Student's Name:..... **Student's ID:**.....

Question 1 (10 pts)

a) State briefly in words the physical meaning of the three Newton's laws of motion, and put a physical or mechanical example for each of them.

b) State in words the definitions of an inertial reference system and a non-inertial reference system. Newton formulated his laws with respect to a reference system fixed relative to the *stars*; is the system used by Newton a truly inertial reference system? Is the Earth an inertial or a non-inertial reference system?

Question 3 (10 pts)

Select the true answer (only one) out of the choices from the list provided for each question. A complementary and *brief* mathematical proof of your answer on the available space would be welcome, but it is **not** needed in order to get full credit.

3.1 The orbital period of a planet in a circular orbit of radius r_1 around the Sun is P_1 . The orbital period of another planet in a circular heliocentric orbit of radius $3r_1$ is

- a) $P_1/3$
- b) $-3P_1$
- c) 3^3P_1
- d) $3^{3/2}P_1$

3.2 The angular momentum in a central motion is

- a) constant and parallel to the orbit plane.
- b) constant and normal to the orbit plane.
- c) not constant, and it is parallel to the orbit plane.
- d) not constant, and it is normal to the orbit plane.

3.3 The specific mechanical energy of a satellite orbiting around the Earth

- a) is not constant and varies sinusoidally with time.
- b) is constant but only for US-manufactured satellites.
- c) is constant if the satellite is not subject to any dissipative forces or external forces other than gravitational interactions.
- d) is always constant.

3.4 The burnout velocity of a space probe intended to leave the Earth is $1.0 \cdot v_{ESC}$, where v_{ESC} is the escape speed at the burnout point. Then the hyperbolic excess speed of the space probe is

- a) $2.0 \cdot v_{ESC}$
- b) $0.5 \cdot v_{ESC}$
- c) zero.
- d) infinity.

3.5 If a hyperbolic, parabolic, elliptic and circular orbits intersect at one point P in the space, a satellite at point P would have a higher orbital speed if it is orbiting on the

- a) hyperbolic orbit.
- b) parabolic orbit.
- c) elliptic orbit.
- d) circular orbit.

Problem 1 (20 pts)

The Molniya 3-3 satellite was launched in 1975 by the Soviet Union for communication, surveillance and military purposes, and it was inserted into a high-inclination Earth orbit of perigee altitude 2,646.5 km and apogee altitude 37,715.4 km. *Give all your results in both canonical units and dimensional units.* Find:



Figure 1: The Molniya 3-3 satellite.

a) the orbit eccentricity,

b) the specific angular momentum of the satellite,

c) the perigee velocity,

d) the apogee velocity,

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e) the specific mechanical energy of the satellite,

f) the orbit period,

g) the satellite velocity when its altitude is 10,000 km,

h) the flight-path angle at altitude 10,000 km,

i) and the zenith angle at altitude 10,000 km.

Problem 2 (25 pts)

The Ballistic Missile Early Warning System (BMEWS) detects an unidentified object with the following parameters:

- altitude: 0.5 DU_{\oplus} ,
- speed: $0.8 \text{ DU}_{\oplus}/\text{TU}_{\oplus}$,
- flight-path angle: 40° .

Is it possible that this object is a space probe intended to escape the Earth, an Earth satellite, or a ballistic missile? Justify your answer.

Problem 3 (25 pts)

A spacecraft is launched from the Vanderberg Air Force base (VAF) to a circular equatorial parking orbit of altitude 300 nmi above Earth. The spacecraft remains circulating in this orbit until the mission center gives permission for an escape maneuver, during which the spacecraft ignites its main engines tangentially to the circular orbit during a short time, by which it is transferred to a hyperbolic orbit about the equator as the one depicted in the figure. The burnout and orbit transfer point corresponds to the perigee of the hyperbolic orbit. Thus, the spacecraft leaves the Earth at a velocity $\mathbf{v}_d = v_\infty \mathbf{I}$ parallel to the vernal-equinox direction Υ (i.e. the x axis), with $v_\infty = 10$ km/s the spacecraft velocity at a radial distance $r_d = 10r_\oplus$, where r_\oplus is the radius of the Earth. In this formulation, \mathbf{I} , \mathbf{J} and \mathbf{K} are unit vectors in the x , y and z directions respectively. Notice that v_∞ is close to the hyperbolic excess velocity since the spacecraft is far from the Earth, $r_d \gg r_\oplus$. A radar station R is located at VAF base, which latitude is $L = 28.5^\circ$. At a particular tracking time, the longitude of VAF is $\theta = 30^\circ$ in a westerly direction with respect to the vernal equinox direction Υ . Note that the system of coordinates $\{x, y, z\}$ (i.e. the geocentric-equatorial coordinate system) does not rotate with the Earth, but the radar site does rotate with the Earth.

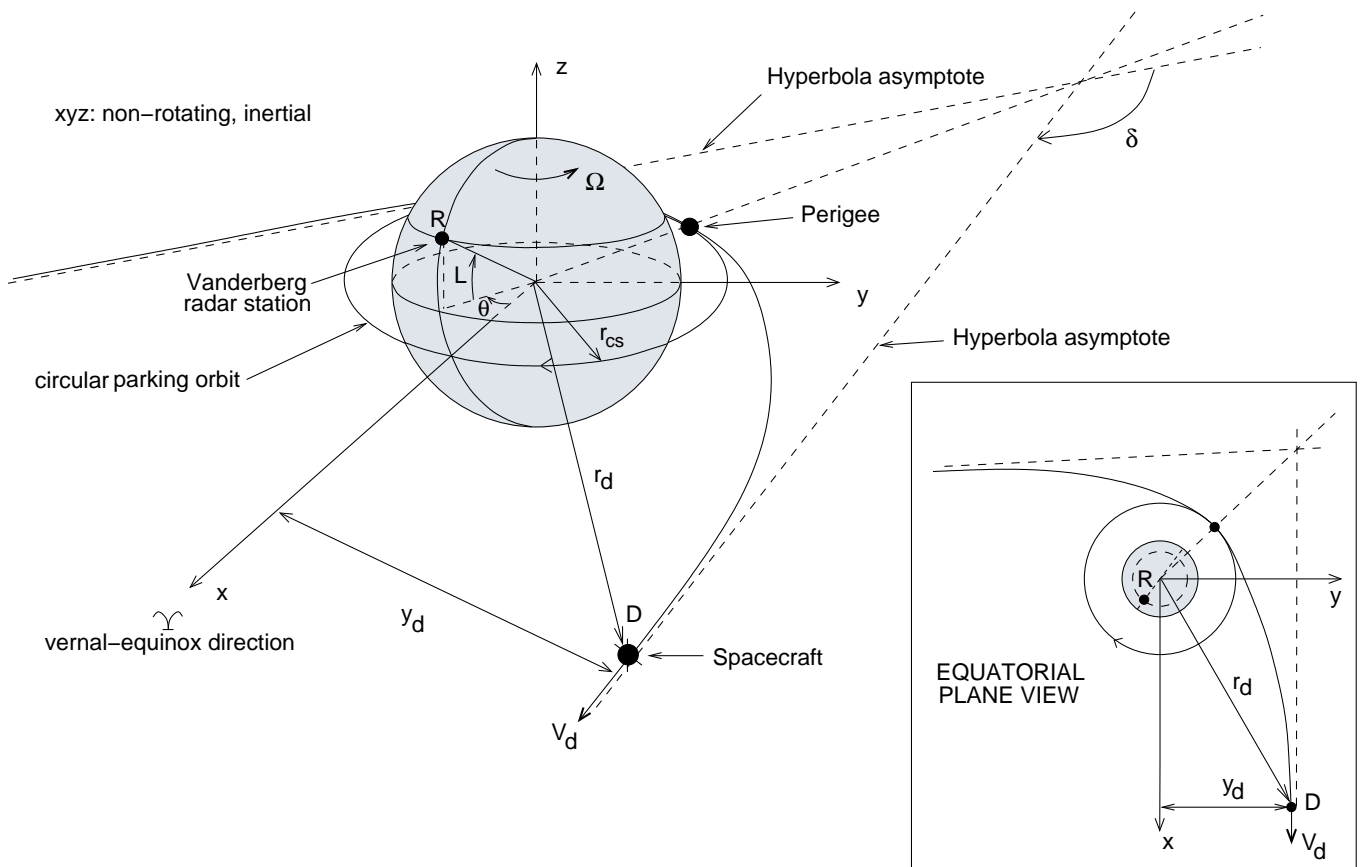


Figure 2: Departure mission sketch.

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h) Obtain the $\{I, J, K\}$ components of the relative position vector of the spacecraft at D with respect to the radar site R .

i) Obtain the $\{I, J, K\}$ components of the relative velocity vector of the spacecraft at D with respect to the radar site R ,