

THE GAMMA-RAY ALBEDO OF THE MOON

IGOR V. MOSKALENKO¹

Hansen Experimental Physics Laboratory, Stanford University, Stanford, CA 94305; imos@stanford.edu

AND

TROY A. PORTER

Santa Cruz Institute for Particle Physics, University of California, Santa Cruz, CA 95064; tporter@scipp.ucsc.edu

Received 2007 June 12; accepted 2007 August 20

ABSTRACT

We use the GEANT4 Monte Carlo framework to calculate the γ -ray albedo of the Moon due to interactions of cosmic-ray (CR) nuclei with moon rock. Our calculation of the albedo spectrum agrees with the EGRET data. We show that the spectrum of γ -rays from the Moon is very steep with an effective cutoff around 3–4 GeV (600 MeV for the inner part of the Moon disk) and exhibits a narrow pion-decay line at 67.5 MeV, perhaps unique in astrophysics. Apart from other astrophysical sources, the albedo spectrum of the Moon is well understood, including its absolute normalization; this makes it a useful “standard candle” for γ -ray telescopes. The steep albedo spectrum also provides a unique opportunity for energy calibration of γ -ray telescopes, such as the forthcoming *Gamma Ray Large Area Space Telescope (GLAST)*. Since the albedo flux depends on the incident CR spectrum, which changes over the solar cycle, it is possible to monitor the CR spectrum using the albedo γ -ray flux. Simultaneous measurements of CR proton and helium spectra by the Payload for Antimatter-Matter Exploration and Light-Nuclei Astrophysics (PAMELA), and observations of the albedo γ -rays by the *GLAST* Large Area Telescope (LAT), can be used to test the model predictions and will enable the LAT to monitor the CR spectrum near the Earth beyond the lifetime of the PAMELA.

Subject headings: cosmic rays — elementary particles — gamma rays: theory — line: formation — Moon — radiation mechanisms: nonthermal

Online material: color figures

1. INTRODUCTION

Interactions of Galactic CR nuclei with the atmospheres of the Earth and the Sun produce albedo γ -rays due to the decay of secondary neutral pions and kaons (e.g., Seckel et al. 1991; Orlando et al. 2007). Similarly, the Moon emits γ -rays due to CR interactions with its surface (Morris 1984; Thompson et al. 1997). However, contrary to the CR interaction with the gaseous atmospheres of the Earth and the Sun, the Moon surface is solid, consisting of rock, making its albedo spectrum unique.

Due to the kinematics of the collision, the secondary particle cascade from CR particles hitting the Moon surface at small zenith angles develops deep into the rock, making it difficult for γ -rays to get out. The spectrum of the albedo γ -rays is thus necessarily soft as it is produced by a small fraction of low-energy splash particles in the surface layer of the moon rock. The high-energy γ -rays can be produced by CR particles hitting the Moon surface with a more tangential trajectory. However, since it is a solid target, only the very thin limb contributes to the high-energy emission.

The γ -ray albedo of the Moon has been calculated by Morris (1984) using a Monte Carlo code for cascade development in the Earth’s atmosphere that was modified for the Moon conditions. However, the CR spectra used as input in the Morris calculation differ considerably from recent measurements by AMS (Alcaraz et al. 2000a, 2000b) and BESS (Sanuki et al. 2000) at both low and high energies. In particular, the CR proton spectrum used by Morris produces the correct intensity only around 10 GeV. In addition, due to the lack of accelerator data and models a number of approximations and ad hoc assumptions were required to cal-

culate the hadronic cascade development in the solid target of the Moon’s surface.

The Moon has been detected by the EGRET as a point source with integral flux $F(>100 \text{ MeV}) = (4.7 \pm 0.7) \times 10^{-7} \text{ cm}^{-2} \text{ s}^{-1}$ (Thompson et al. 1997), $\sim 24\%$ below the predictions by Morris (1984), although the spectral shape agrees with the data. The observed spectrum is steep and yields only the upper limit $\sim 5.7 \times 10^{-12} \text{ cm}^{-2} \text{ s}^{-1}$ above 1 GeV. At lower energies, γ -ray spectroscopy data acquired by the Lunar Prospector have been used to map the elemental composition of the Moon surface (Lawrence et al. 1998; Prettyman et al. 2006).

In this paper we calculate the γ -ray albedo from the Moon using the GEANT4 software framework and discuss the consequences of its measurement by the upcoming *GLAST* mission (Michelson 2007; Ritz 2007). Our preliminary results are presented in Moskalenko & Porter (2007).

2. MONTE CARLO SIMULATIONS

Since the first calculation of the Moon albedo (Morris 1984), computers and Monte Carlo codes have advanced considerably, while more data on particle interactions and CR fluxes have become available. The modern GEANT4 toolkit² (Agostinelli et al. 2003) is widely used across particle physics, medical science, and space physics to simulate the passage of particles through matter. It provides extensive functionality including physics models, tracking, geometry, and visualization. A full range of electromagnetic and hadronic physics processes over a wide energy range are available including long-lived particles. A large set of materials and elements are also included. Together with the extensive documentation and examples, it is straightforward to describe and simulate complicated detectors and interactions.

¹ Also Kavli Institute for Particle Astrophysics and Cosmology, Stanford University, Stanford, CA 94309.

² Available from <http://cern.ch/geant4>.

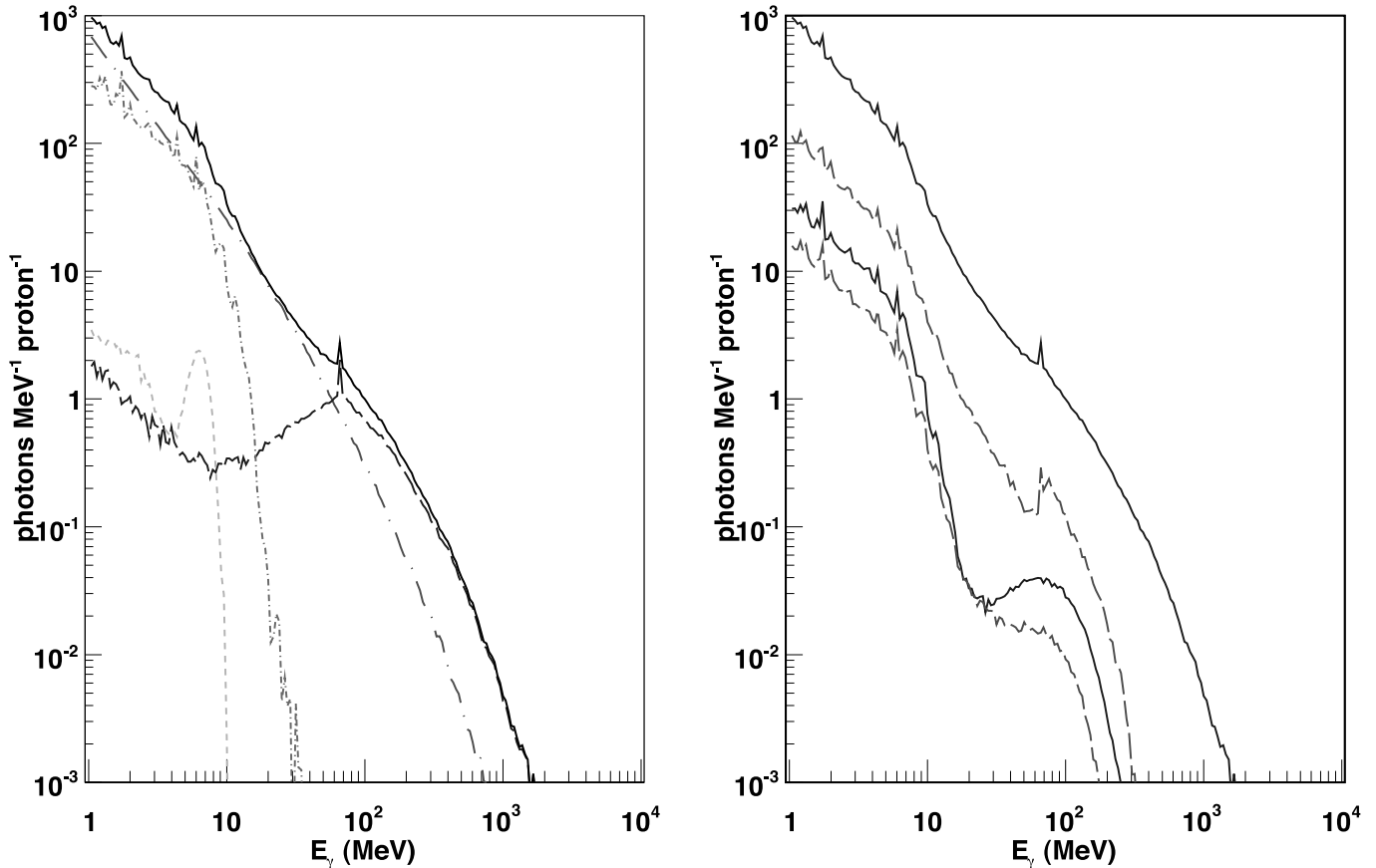


FIG. 2.—Integration of the γ -ray yield per proton interaction over all emission angles from the Moon surface. *Left*: Yield calculated for $E_p = 10,000$ MeV and $\cos \theta_p = 0.1$ with components shown, *Line styles*: Decay, blue-dashed; bremsstrahlung, red long-dash-dotted; nonelastic scattering and de-excitation, magenta short-dash-dotted; low-energy neutron capture, cyan dotted; and total, black solid. For each component, the initial process responsible for the production of the γ -ray secondary is given by the line style, but the yield distribution includes also processes such as Compton scattering. *Right*: Yield calculated for two different energies and incident angles. *Line styles*: $\cos \theta_p = 0.1$, blue solid; $\cos \theta_p = 1$, red dashed. *Line sets*: $E_p = 500$ MeV, lower; $E_p = 10,000$ MeV, upper. [See the electronic edition of the Journal for a color version of this figure.]

incident angles are very similar to each other for the case of low-energy protons where the secondary particles (pions, kaons, neutrons, etc.) are produced nearly at rest. In the high-energy case, the secondary distribution for protons incident near zenith has a cutoff above ~ 500 MeV. Further away from zenith, higher yields of secondary γ -rays are produced while the spectrum of γ -rays becomes progressively harder. This is a result of the cascade developing mostly in the forward direction: for near zenith primaries, most high-energy secondary γ -rays will be absorbed in the target, while a small fraction of splash albedo particles, mostly low-energy ones, produce the soft spectrum γ -rays; further from zenith, the high-energy secondary γ -rays will shower out of the Moon surface.

The clear narrow line at 67.5 MeV in Figure 2 (*left and right panels*) is due to neutral pions decaying near rest. To ensure that it is not an artifact of the simulation, we made an extensive analysis of the hadronic interaction models employed in GEANT4 and various geometries of the beam/target/detector configuration. Independently of the hadronic interaction model used, the line is always present, but its intensity may vary slightly. However, dependent on the beam/target/detector configuration, the line may appear or disappear. The most feasible explanation of this effect is the following. The line is always present since there is always some small fraction of pions decaying at rest, but in the most common configurations, such as thin target, gaseous target, and/or detector position in the forward hemisphere, the line is hidden under the strong continuum background. In our case of a

solid thick target and the detector location in the backward hemisphere, a considerable part of the continuum background is cut off and the line becomes visible.

There are several reasons why the continuum background is cut off. The interaction length of a GeV proton in oxygen (the most abundant element in the moon rock) is ~ 80 g cm $^{-2}$, which corresponds to ~ 44 cm for the moon rock (density ~ 1.8 g cm $^{-3}$). As the cascade develops, energetic particles penetrate deep into the rock, too deep for γ -rays to come out. The γ -ray albedo is produced by relatively low-energy particles at the depth of about one radiation length, ~ 34 g cm $^{-2}$, which corresponds to ~ 20 cm for the moon rock. The pions decaying in the upper layer of the moon rock are necessarily low-energy (splash) particles while the high-energy part of the cascade producing the continuum spectrum is cut off because of the kinematics of the interaction and the forward cascade development. Since many photons are coming from a large depth, this explains the large contribution of the Compton scattered γ -rays below ~ 60 MeV (Fig. 2). For lower energy protons, this also explains why the 67.5 MeV line is not prominent, since the development of the cascade then occurs relatively close to the surface producing a continuum that essentially washes out any line feature.

3. CALCULATIONS

The CR spectrum above the geomagnetic cutoff near Earth (at 1 AU) can be directly measured by balloon-borne instruments or spacecraft. However, it has been done during short flights at

TABLE 1
 FITS TO LOCAL INTERSTELLAR CR SPECTRA

Particle	J_0	a_1	b_1	c_1	a_2	b_2	c_2	a_3	b_3	c_3
Proton.....	1.6×10^4	1	0.458	2.75	-3.567	0.936	4.90	4.777×10^5	14.4	6.88
Helium.....	1.6×10^3	1	1.116	3.75	2.611	4.325	3.611	0.219	0.923	2.58

NOTE.—Intensity units: $\text{m}^{-2} \text{s}^{-1} \text{sr}^{-1} (\text{GeV nucleon}^{-1})^{-1}$.

different phases of solar activity. To calculate the Moon albedo at an arbitrary modulation level, we use the local interstellar (LIS) spectra of CR protons and helium as fitted to the numerical results of the GALPROP propagation model (reacceleration and plain diffusion models; Table 1 in Ptuskin et al. 2006); the CR particle flux at an arbitrary phase of solar activity at 1 AU can then be estimated using the force-field approximation (Gleeson & Axford 1968):

$$\frac{dJ_p(E_k)}{dE_k} = \frac{dJ_p^\infty(E_k + \Phi Z/A)}{dE_k} \frac{E^2 - M^2}{(E + \Phi Z/A)^2 - M^2}, \quad (1)$$

where dJ_p^∞/dE_k is the LIS spectrum of CR species, E_k is the kinetic energy per nucleon, E is the total energy per nucleon, Φ is the modulation potential, Z and A are the nucleus charge and atomic number correspondingly, and M is the nucleon mass.

To fit the LIS CR spectra we choose a function of the form

$$\frac{dJ^\infty}{dE_k} = J_0 \sum_{i=1}^3 a_i (E_k + b_i)^{-c_i}, \quad (2)$$

where the flux units are $\text{m}^{-2} \text{s}^{-1} \text{sr}^{-1} (\text{GeV nucleon}^{-1})^{-1}$ and the parameter values are given in Table 1. The latter are not unique and other sets could produce similar quality fits, but this does not affect the final results. Figure 3 shows the LIS CR proton spectrum and modulated one compared with the BESS (Sanuki et al. 2000) and AMS (Alcaraz et al. 2000a) data taken during the period of moderate solar activity. The parameters given in Table 1 yield a LIS proton spectrum that is somewhat *higher* than the GALPROP LIS below ~ 2 GeV (plain diffusion model 44_999726,

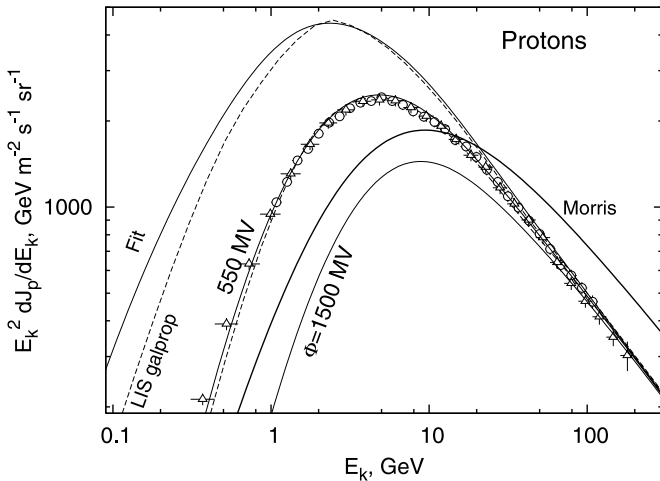


FIG. 3.—CR proton spectrum. The dashed lines are the LIS spectrum (*upper*) and modulated one ($\Phi = 550$ MV, *lower*) as calculated by GALPROP in the plain diffusion model 44_999726 (Ptuskin et al. 2006). The thin solid lines are the fit to the LIS spectrum (*upper*) and modulated spectra ($\Phi = 550$ MV, *middle*; $\Phi = 1500$ MV, *lower*). The thick solid line is the CR proton spectrum used by Morris (1984). Data: BESS (Sanuki et al. 2000, *circles*), AMS (Alcaraz et al. 2000a, *triangles*).

Ptuskin et al. 2006). However, the fit to the AMS and BESS data after modulation ($\Phi = 550$ MV) is good. The spectrum labeled $\Phi = 1500$ MV corresponds to the period of high solar activity. The proton spectrum used by Morris (1984) is shown by the thick solid line. The disagreement with the modern CR proton data is considerable. For the helium spectrum, the parameters given in Table 1 provide a good fit to the GALPROP LIS, and agree with the AMS (Alcaraz et al. 2000b) data after modulation ($\Phi = 550$ MV); at high energies the fit also passes through JACEE (Asakimori et al. 1998) and Sokol (Ivanenko et al. 1993) data.

The γ -ray albedo flux at the Earth is calculated as

$$\frac{dF_\gamma}{dE_\gamma d \cos \psi} = 1/\cos \theta \int dE_k \frac{dJ_p}{dE_k} \frac{d\tilde{Y}_\gamma(E_k, \cos \psi)}{dE_\gamma d \cos \theta}, \quad (3)$$

where ψ is the angular distance from the geometrical center of the Moon disk as seen from the Earth, $1/\cos \theta$ is the Jacobian,

$$\cos \theta = \sqrt{1 - \frac{R^2}{r^2} \sin^2 \psi}, \quad (4)$$

$$\frac{d\tilde{Y}_\gamma(E_k)}{dE_\gamma d \cos \theta} = 2\pi \int_0^1 d(\cos \theta_p) \cos \theta_p \frac{dY_\gamma(E_k, \cos \theta_p)}{dE_\gamma d \cos \theta}, \quad (5)$$

$R = 1738.2$ km is the Moon radius, and $r = 384,401$ km is the distance to the Moon.

Figure 4 shows the calculated total γ -ray albedo spectrum for CR protons and helium compared to the EGRET data for periods of lower (*upper solid line*: $\Phi = 500$ MV) and higher (*lower solid line*: $\Phi = 1500$ MV) solar activity. Taking into account that the exact CR spectra during the EGRET observations are unknown, the agreement with the data is remarkable. The broken lines show the spectra from the limb (outer 5') and the central part of the disk (20' across) for the case of higher solar activity. As expected, the spectra from the limb and the central part are similar at lower energies (< 10 MeV); at high energies the central part exhibits a softer spectrum so that virtually all photons above ~ 600 MeV are emitted by the limb.

Interestingly, the pion-decay line is still significant even when the γ -ray yields are integrated over the spectrum of CR, although, its intensity is small relative to the *total* albedo flux. The line perhaps always exists due to the splash albedo pions, but in case of a thin and/or gaseous target (usual in astrophysics) it is indistinguishable from the background γ -rays (see § 2 for more discussion).

4. DISCUSSION

The *GLAST* LAT is scheduled for launch by NASA in early 2008. It will have superior angular resolution and effective area, and its field of view (FOV) will far exceed that of its predecessor, the EGRET (McEnery et al. 2004). The LAT will scan the sky continuously providing complete sky coverage every two orbits (approximately 3 hr). The on-axis effective area of the LAT

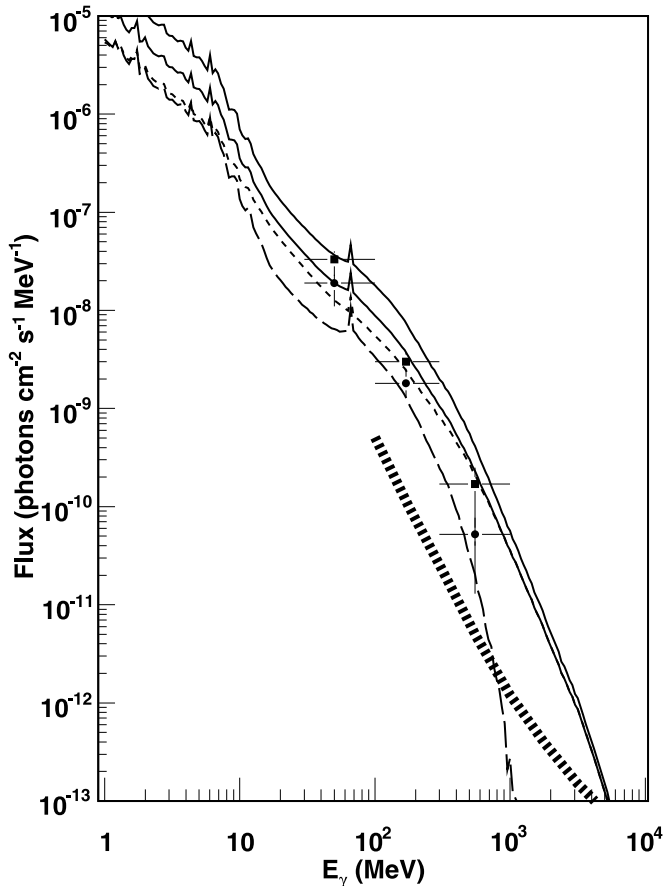


FIG. 4.— Calculated γ -ray albedo spectrum of the Moon. Line-styles: total, black solid; limb (outer 5'), blue dotted; center (inner 20'), red dashed. Upper solid line: $\Phi = 500$ MV; lower solid line: $\Phi = 1500$ MV. Limb and center components are only shown for $\Phi = 1500$ MV. Data points from the EGRET (Thompson et al. 1997) with upper and lower symbols corresponding to periods of lower and higher solar activity, respectively. The differential 1 yr sensitivity of the LAT is shown as the shaded region. [See the electronic edition of the *Journal* for a color version of this figure.]

increases from ~ 3000 cm^2 at 100 MeV to ~ 8500 – 9000 cm^2 at 1 GeV and higher.⁴ In this case, the point-spread function (PSF) of the instrument has a 68% containment radius $\sim 4.3^\circ$ at 100 MeV reducing dramatically at higher energies: $\sim 0.8^\circ$ at 1 GeV, $\sim 0.5^\circ$ at 2 GeV, and $\sim 0.2^\circ$ at 10 GeV. Using only events from the front section of the LAT, the PSF improves to a 68% containment radius of $\sim 3^\circ$ at 100 MeV, $\sim 0.5^\circ$ at 1 GeV, $\sim 0.25^\circ$ at 2 GeV, and $\sim 0.1^\circ$ at 10 GeV, but the on-axis effective area is essentially halved.

About 20% of the time the Moon will be in the FOV at different viewing angles. The photon flux expected from the Moon for $\Phi = 500$ MV above 100 MeV, 1 GeV, and 4 GeV is $\sim 5 \times 10^{-7}$, $\sim 2 \times 10^{-8}$, and $\lesssim 1.6 \times 10^{-10}$ photons $\text{cm}^{-2} \text{s}^{-1}$, respectively. For $\Phi = 1500$ MV, the expected flux is reduced by a factor of 2 at 100 MeV only. With these fluxes and the above values for the effective area, and allowing for an additional factor of 2 reduction to take into account time off-axis, instrumental dead time, and South Atlantic Anomaly traversals, we estimate the LAT will collect $\sim 5 \times 10^3$, $\sim 6 \times 10^2$, and $\lesssim 5$ photons, respectively, in the above energy ranges in 1 year. These numbers are reduced by a factor of 2 if only events from the front section of the LAT are used. Interestingly, the albedo flux at low energies is high enough that the impact of the broader PSF is significantly reduced.

Measuring γ -rays from the Moon presents several interesting possibilities for the LAT. Apart from other astrophysical sources, the albedo spectrum of the Moon is well understood, including its absolute normalization, while the Moon itself is a “moving target” passing through high Galactic latitudes and the Galactic center region. This makes it a useful “standard candle” for the *GLAST* LAT at energies where the PSF is comparable to the Moon size 0.5° , i.e., at ~ 1 GeV and higher. At these energies the albedo flux is essentially independent of the solar modulation. At lower energies the γ -ray flux depends on the level of the solar modulation and thus can be used to infer the incident CR spectrum. A simultaneous presence of the PAMELA on-orbit capable of measuring protons and light nuclei with high precision (Picozza et al. 2007) provides a necessary input for accurate prediction of the albedo flux and a possible independent calibration of the *GLAST* LAT. An additional bonus of such a calibration is the possibility to use the *GLAST* observations of the Moon to monitor the CR spectra near the Earth beyond the projected lifetime of the PAMELA (currently 3 years).

The line feature at 67.5 MeV from π^0 -decay produced by CR particles in the solid rock target is interesting. There is no other astrophysical object predicted to produce such a narrow line and there is no other line expected except, perhaps, from dark matter annihilation. The lower energy limit of the LAT instrument is below 20 MeV, while the energy resolution is $\sim 15\%$ at 100 MeV and improves at higher energies. With a suitable event selection it may be possible to observe the line; if so, it will provide a possibility of in-orbit energy calibration. Another possibility for energy calibration at higher energy is provided by the steep albedo spectrum above 100 MeV: a small error in the energy determination will result in a large error in the intensity.

Because of the steep albedo spectrum, very few photons will be detected above ~ 3 – 4 GeV. The central part of the Moon has an even steeper spectrum with an effective cutoff at ~ 600 MeV. Above a few GeV, the Moon presents almost a black spot on the γ -ray sky, providing an opportunity to screen out a piece of the sky. In addition, the expected irreducible background rate⁵ at these energies within the solid angle subtended by the Moon is ~ 0.1 photons yr^{-1} (S. Digel 2007, private communication). The absence of any significant excess over the predicted rate will be a useful cross check on the expected irreducible background.

5. CONCLUSIONS

The γ -ray albedo of the Moon makes it a unique calibration target for γ -ray telescopes. Apart from other astrophysical sources the albedo spectrum is well understood, including its absolute normalization. The albedo of the Moon is dim, especially its central part at high energies. Its lower energy part exhibits a narrow pion-decay line at 67.5 MeV, perhaps unique in astrophysics and never before observed, while its continuum intensity depends on the phase of the solar cycle and allows one to monitor the ambient spectrum of CR particles. The *GLAST* LAT instrument is well suited for such observations.

We thank Bill Atwood, Seth Digel, Robert Johnson, and Dennis Wright for many useful discussions. I. V. M. acknowledges partial support from NASA Astronomy and Physics Research and Analysis Program (APRA) grant. T. A. P. acknowledges partial support from the US Department of Energy.

⁴ See <http://glast.stanford.edu>.

⁵ Gamma-rays produced in the FOV by CR interactions in the inert material surrounding the LAT.

REFERENCES

- Agostinelli, S., et al. 2003, Nucl. Instrum. Methods Phys. Res. A, 506, 250
- Alcaraz, J., et al. 2000a, Phys. Lett. B, 490, 27
- . 2000b, Phys. Lett. B, 494, 193
- Anand, M., et al. 2003, Meteor. Planet. Sci., 38, 485
- Asakimori, K., et al. 1998, ApJ, 502, 278
- Ersmark, T., et al. 2004, IEEE Trans. Nucl. Sci., 51, 1378
- Gleeson, L. J., & Axford, W. I. 1968, ApJ, 154, 1011
- Ivanenko, I. P., et al. 1993, Proc. 23rd Int. Cosmic-Ray Conf. (Calgary), 17
- Lawrence, D. J., et al. 1998, Science, 281, 1484
- McEnery, J. E., Moskalenko, I. V., & Ormes, J. F. 2004, in Cosmic Gamma-Ray Sources, ed. Cheng, K. S., & Romero, G. E. (Dordrecht: Kluwer), 361
- Michelson, P. F. 2007, in AIP Conf. Proc. 921, First Int. *GLAST* Symp., ed. Ritz, S., et al. (Melville: AIP), 8
- Morris, D. J. 1984, J. Geophys. Res. A, 89, 10685
- Moskalenko, I. V., & Porter, T. A. 2007, in Proc. 30th Int. Cosmic-Ray Conf. (Merida), in press (arXiv:0705.3856)
- Orlando, E., Petry, D., & Strong, A. W. 2007, in AIP Conf. Proc. 921, First Int. *GLAST* Symp., ed. S. Ritz et al. (Melville: AIP), 502
- Picozza, P., et al. 2007, Astropart. Phys., 27, 296
- Prettyman, T. H., et al. 2006, J. Geophys. Res., 111, 12007
- Ptuskin, V. S., Moskalenko, I. V., Jones, F. C., Strong, A. W., & Zirakashvili, V. N. 2006, ApJ, 642, 902
- Ritz, S. 2007, in AIP Conf. Proc. 921, First Int. *GLAST* Symp., ed. S. Ritz et al. (Melville: AIP), 3
- Sanuki, T., et al. 2000, ApJ, 545, 1135
- Seckel, D., Stanev, T., & Gaisser, T. K. 1991, ApJ, 382, 652
- Thompson, D. J., Bertsch, D. L., Morris, D. J., & Mukherjee, R. J. 1997, Geophys. Res. A, 120, 14735
- Wellisch, J. P. 2003, Nucl. Instrum. Methods Phys. Res. A, 502, 669