

Stanford University Mathematical Organization (SUMO) Speaker Series

# Pseudo-polynomials

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3–4 PM @ 380-382T

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## Abstract

Every polynomial  $f$  with integer coefficients has the following useful property: for every integers  $n$  and  $k$ ,  $f(n+k)$  is congruent to  $f(k)$  mod  $n$ . To say this a different way,  $f$  is well-defined mod  $n$  for every  $n$ . This talk will be about pseudo-polynomials, which are arbitrary functions on the integers that satisfy this same property. All polynomials are pseudo-polynomials, but it turns out there are many more: for example,  $\lfloor e \cdot n! \rfloor$  is a pseudo-polynomial. We'll discuss the history of pseudo-polynomials and certain outstanding open questions about them!