8

Dispersive spin fluctuations in the nearly optimally doped superconductor $Ba(Fe_{1-x}Co_x)_2As_2$ (x=0.065)

C. Lester, ¹ Jiun-Haw Chu, ^{2,3} J. G. Analytis, ^{2,3} T. G. Perring, ⁴ I. R. Fisher, ^{2,3} and S. M. Hayden ¹ H.H. Wills Physics Laboratory, University of Bristol, Tyndall Avenue, Bristol BS8 1TL, United Kingdom ²Geballe Laboratory for Advanced Materials and Department of Applied Physics, Stanford University, Stanford, California 94305, USA ³Stanford Institute for Materials and Energy Sciences, SLAC National Accelerator Laboratory, 2575 Sand Hill Road, Menlo Park, California 94025, USA

⁴ISIS Facility, STFC Rutherford Appleton Laboratory, Chilton, Didcot OX11 0QX, United Kingdom (Received 20 December 2009; revised manuscript received 25 January 2010; published 16 February 2010)

Inelastic neutron scattering is used to probe the collective spin excitations of the near optimally doped superconductor $Ba(Fe_{1-x}Co_x)_2As_2$ (x=0.065). Previous measurements on the antiferromagnetically ordered parents of this material show a strongly anisotropic spin-wave velocity. Here we measure the magnetic excitations up to 80 meV and show that a similar anisotropy persists for superconducting compositions. The dispersive mode measured here connects directly with the spin resonance previously observed in this compound. When placed on an absolute scale, our measurements show that the local- or wave-vector-integrated susceptibility is larger in magnitude than that of the ordered parents over the energy range probed.

DOI: 10.1103/PhysRevB.81.064505 PACS number(s): 74.70.-b, 75.40.Gb, 75.30.Et, 78.70.Nx

I. INTRODUCTION

The recently discovered ferropnictide superconductors¹ show critical temperatures exceeding 50 K. They are interesting materials, both in their own right and because they provide valuable insights into other classes of superconductor. Theoretical calculations² suggest that the electronphonon coupling is too weak in the ferropnictides to produce the high transition temperatures which are observed experimentally. The ferropnictides have some similarities to the cuprates in that they are quasi-two-dimensional (2D) and have antiferromagnetic parent compounds. Superconductivity in the ferropnictides can be induced^{3,4} from their antiferromagnetic parents by various means: electron or hole doping via chemical substitution; isovalent substitution of the iron or arsenic or by the application of pressure. In the widely studied AFe_2As_2 (A=Ca,Sr,Ba) family (known as the "122" family), 3-7 this can be via chemical substitution at the Fe or As sites or the application of pressure. For example, in BaFe2As2, we obtain superconductivity through electron doping by Co or Ni substitution at the Fe site; by hole doping with K at the Ba site; or by isovalent substitution of Fe by Ru or As by P.

The proximity of superconductivity to antiferromagnetism suggests that the pairing mechanism in the doped ferropnictides is related to the spin degrees of freedom. Theories based on various models of the magnetic excitations have been proposed. In order to take such theories forward, the collective magnetic excitations in the superconducting region of the phase diagram need to be characterized and the underlying interactions understood. Thus, in this paper, we report an inelastic neutron-scattering (INS) study of the magnetic response, up to 80 meV, of a near optimally doped superconducting (T_c =23 K) composition Ba(Fe_{0.935}Co_{0.065})₂As₂. This composition appears not to be magnetically ordered. We compare our results with similar measurements on the antiferromagnetic parent compounds 14–17 of the 122 series and find that (i) the magnetic excitations are stronger than in the

parent compounds and (ii) the anisotropy in the spin-wave (SW) velocity observed in the parent compounds persists in this superconductor.

II. EXPERIMENTAL DETAILS

Single crystals of Ba(Fe_{0.935}Co_{0.065})₂As₂ were grown by a self-flux method.⁶ Fifteen crystals were coaligned on a thin Al plate using x-rays and neutron diffraction. Our neutron measurements were made on a mosaic of total mass of 0.3 g. Resistivity and magnetization measurements identified the superconducting transition temperature $T_c(\text{onset}) = 23 \text{ K}$. Elastic neutron scattering revealed no evidence of magnetic order at this doping level at temperatures down to 2 K. We used the MAPS instrument at the ISIS spallation source. MAPS is a low-background direct-geometry time-of-flight chopper spectrometer with position sensitive detectors. ¹⁸ A pulse of moderated spallation neutrons spread over a time of about 5–10 μ s (for the energies used in the present experiment) is produced when a pulse of protons hits a Ta target adjacent to a water moderator. Neutrons with the required energy (E_i =60, 80, or 140 meV in the present experiment) are then selected by an appropriately phased Fermi chopper (rotating at 100 Hz in the present experiment). The Fermi chopper is 10 m from the neutron source and opens for about 45 μ s. The neutrons then scatter from the sample (12 m from source) and are detected in position sensitive ³He detectors at 6 m from the sample. The detection time of the neutron is used to determine its energy transfer. Data are averaged of a range of energies to improve the experimental statistics. The energy ranges of integration are given when we quote neutron energy transfers in the text. Data were placed on an absolute scale (barn sr⁻¹ f.u.⁻¹) by comparing the count rate with that from a plate of vanadium.

The magnetic cross section of an isotropic paramagnet is given by

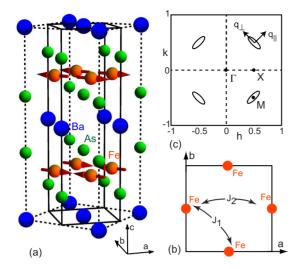


FIG. 1. (Color online) (a) The antiferromagnetic structure of the parent compound BaFe₂As₂. Axes refer to the tetragonal notation used throughout the paper. Solid lines denote the tetragonal unit cell. (b) Exchange couplings between Fe atoms referred to in the text. (c) Schematic illustration of reciprocal space (of a 2D square lattice). The ellipses represent the anisotropic excitations reported in this paper. The wave vectors are used to define the spin-wave velocities.

$$\frac{d^2\sigma}{d\Omega dE} = \frac{2(\gamma r_{\rm e})^2}{\pi g^2 \mu_{\rm B}^2} \frac{k_f}{k_i} |F(\mathbf{Q})|^2 \frac{\chi''(\mathbf{q}, \omega)}{1 - \exp(-\hbar\omega/kT)},$$
 (1)

where $(\gamma r_{\rm e})^2$ =0.2905 barn sr⁻¹, ${\bf k}_i$ and ${\bf k}_f$ are the incident and final neutron wave vectors and $|F({\bf Q})|^2$ is the isotropic magnetic form factor for a Fe²⁺ orbital. We use Eq. (1) to convert the measured cross section to the energy- and momentum-dependent susceptibility¹⁹ $\chi''({\bf q},\omega)$. Ba(Fe_{0.935}Co_{0.065})₂As₂ has the tetragonal crystal structure

shown in Fig. 1(a) with lattice parameters a=3.955 Å and c=12.95 Å. We use the reciprocal space notation to label wave vectors $\mathbf{Q}=h\mathbf{a}^*+k\mathbf{b}^*+l\mathbf{c}^*$. In this notation, the antiferromagnetic ordering wave vector of BaFe₂As₂ is (1/2,1/2,1). The data reported in this paper were collected with \mathbf{c}^* parallel to \mathbf{k}_i . Under these conditions, there is a coupling of l and the ω . We give the l value corresponding to each ω in the figures and captions.

III. RESULTS

Figure 2 shows typical ${\bf q}$ -dependent images of $S({\bf q},\omega)=(k_i/k_f)d^2\sigma/d\Omega dE$ in the (h,k) plane for various energy transfers obtained from the MAPS spectrometer. At first sight, the data look similar to those obtained over the same energy range on the related antiferromagnetic parent compound CaFe₂As₂. ^{16,17} At low energies, $E=9.5\pm1.5$ meV [Fig. 2(a)], the magnetic response is strongest at the (1/2,1/2) position. The excitations disperse with increasing energy with the pattern broadening most rapidly along the $(1/2-\xi,\ 1/2+\xi)$ rather than the $(1/2+\xi,\ 1/2+\xi)$ direction, leading to an elliptically shaped response as shown schematically in Fig. 1(b). Figure 3 shows cuts through the data shown in Fig. 2, again illustrating the anisotropic dispersion and broadening of the response with increasing energy transfer.

Although $Ba(Fe_{0.935}Co_{0.065})_2As_2$ is not magnetically ordered, its response is reminiscent of the magnetically ordered 122 parent compounds. In order to make a more quantitative analysis of our data we fitted a phenomenological spin-wave cross section with a damped-harmonic-oscillator (DHO) line shape in energy. The DHO cross section is specified by Eqs. (2) and (3),

$$\chi''(\mathbf{q},\omega) = \chi'(\mathbf{q},0) \frac{2\omega_0^2 \Gamma \omega}{(\omega_0^2 - \omega^2)^2 + (2\omega\Gamma)^2},$$
 (2)

where

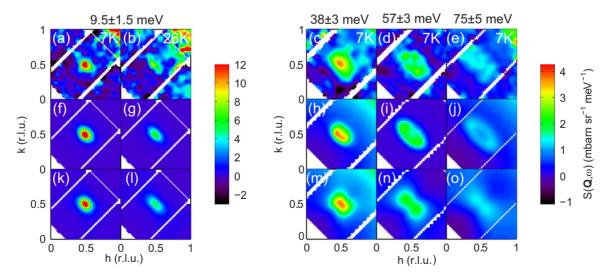


FIG. 2. (Color online) (a)–(e) Constant-energy slices through the magnetic excitations in Ba(Fe_{0.935}Co_{0.065})₂As₂ as observed on MAPS. (f)–(j) Fits to a phenomenological spin-wave cross section [Eqs. (2) and (3)]. (k)–(o) Fits to a phenomenological Sato-Maki cross sections [Eq. (6)] [e.g., for (n) κ =0.21 \pm 0.09, δ =0.6 \pm 0.2, and λ =5 \pm 2]. The incident energies used were (a) and (b) 60 and 140 meV (c)–(e) and the corresponding l values were (a) and (b) l=1, (c) 2.5, (d) 4, and (e) 5.5. The E_i =140 meV data were collected using a proton beam current of 175 μ A for 80 h. A constant background has been subtracted from each plot.

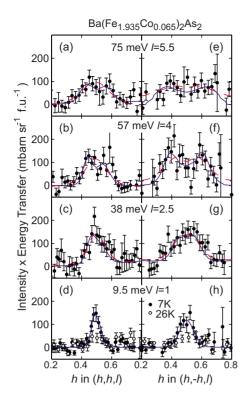


FIG. 3. (Color online) Constant $\hbar\omega$ and l cuts along $(1/2-h,\ 1/2+h,l)$ and $(1/2-h,\ 1/2+h,l)$ (see Fig. 1) for various values of $\hbar\omega$. The blue solid line is a fit to the SW cross section [Eqs. (2) and (3)] and the red dotted line to the Sato-Maki model [Eq. (6)]. Where only one line is drawn, the fits are indistinguishable.

$$\omega_0 = \left[(v_{\parallel} q_{\parallel})^2 + (v_{\perp} q_{\perp})^2 + \Delta^2 \right]^{1/2}. \tag{3}$$

In these equations, v_{\parallel} and v_{\perp} describe the dispersion along $(1/2+\xi,\ 1/2+\xi)$ -type and $(1/2-\xi,\ 1/2+\xi)$ -type directions, respectively (or q_{\parallel} and q_{\perp} in Fig. 1), Γ is the damping parameter and Δ is a gap (see later). Equations (2) and (3) give a good description of the data at all energies. The **q**-averaged or local susceptibility $\chi''(\omega)$ is defined as

$$\chi''(\omega) = \frac{\int \chi''(\mathbf{q}, \omega) d\mathbf{q}}{\int d\mathbf{q}},\tag{4}$$

where the average is over sufficient Brillouin zones in the extended zone scheme to sample representative wave vectors of $\chi''(\mathbf{q},\omega)$. The local quantity gives an indication of the overall strength of the excitations and can be used to compute the corresponding fluctuating moment

$$\langle \mathbf{m}^2 \rangle = \frac{3\hbar}{\pi} \int_{-\infty}^{\infty} \frac{\chi''(\omega) d\omega}{1 - \exp(-\hbar \omega/kT)}.$$
 (5)

Figures 4 and 5 show the dispersion and the energy dependence of $\chi''(\omega)$ determined from fits to the data. The different symbols in Figs. 4 and 5 represent different l values for the c-axis momentum. In the present experiment we average $\chi''(\mathbf{Q},\omega)$ over 0 < h < 1 and 0 < k < 1 and l over approximately ± 0.25 to compute the values in Fig. 5. All points appear to follow the same trend and thus we are unable to discern any evidence for magnetic coupling in the c

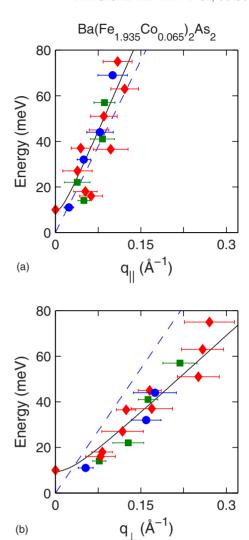


FIG. 4. (Color online) The dispersion of the magnetic excitations in Ba(Fe_{0.935}Co_{0.065})₂As₂ for T=7 K as determined from fitting the damped spin-wave cross section [Eqs. (3) and (2)] along q_{\parallel} (a) and q_{\perp} (b) compared to that found in CaFe₂As₂ (Ref. 17) (blue dashed line) in each case. Symbols denote l values: \blacksquare (l even); \blacksquare (l odd); and \blacklozenge (l noninteger).

for the energy scale of the present experiment $E \gtrsim 10$ meV.

A second function which has been used to describe the magnetic response in nested Fermi liquids is the modified Lorentzian or Sato-Maki (SM) function.²¹ This function has been successfully used to model chromium,^{21,22} La_{2-x}Sr_xCuO₄,²³ and more recently FeTe_{1-x}Se_x.²⁴ The Sato-Maki cross section is of the form

$$\chi''(\mathbf{q},\omega) = \chi_{\delta}(\omega) \frac{\kappa^4(\omega)}{\left[\kappa^2(\omega) + R(\mathbf{q})\right]^2}$$
 (6)

with

$$R(\mathbf{q}) = \frac{1}{4\delta^2} \left\{ \left[(h - h_0)^2 + (k - k_0)^2 - \delta^2 \right]^2 + \frac{\lambda}{4} \left[(h - h_0)^2 - (k - k_0)^2 \right]^2 \right\},$$

where $\mathbf{Q}_0 = (h_0, k_0)$ is the nearest reciprocal-lattice point to \mathbf{Q}

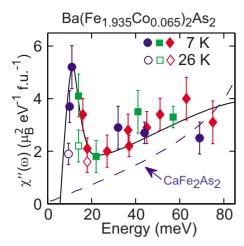


FIG. 5. (Color online) The local susceptibility $\chi''(\omega)$ at 7 (closed symbols) and 26 K (open symbols). Symbols denote l values: \blacksquare (l even); \bullet (l odd); and \bullet (l noninteger). Dashed line shows the local susceptibility for CaFe₂As₂ (Refs. 17 and 20).

with odd (h+k). The location of the peaks in the response is controlled by δ , and its shape by κ and λ . For example, to obtain a peak centered at $\mathbf{Q} = (1/2, 1/2)$, $\delta = 1/\sqrt{2}$. We found that the Sato-Maki function could give a good description of our data except at the highest energies $E \approx 80$ meV. Fits of the SM function are shown in Figs. 2 and 3. The values of $\chi''(\omega)$ computed from the SM fits are statistically indistinguishable from those obtained using the SW cross section.

IV. DISCUSSION

The magnetic response has been studied by neutron scattering in a number of superconducting ferropnictides^{24–29} including Ba(Fe_{1-x}Co_x)₂As₂. ^{26,29} Previous experiments on the superconducting 122 systems have either been on powder samples²⁵ or performed over a smaller energy range^{26,29} than the present experiment. One of the early results from INS on the iron-based superconductors was the observation of a "spin resonance." ^{25-27,29} The spin resonance is most easily interpreted in terms of a sign difference in the superconducting gap $\Delta(\mathbf{k})$ between different parts of the Fermi surface^{8–13} and is consistent with a s^{\pm} gap function. At the lowest energies probed by the present experiment we are able to observe the spin resonance. Figure 5 shows this most directly: there is a peak in the local susceptibility $\chi''(\omega)$ near 10 meV at T=7 K which is suppressed on raising the temperature to 26 K. The resonance is strongest near q = (1/2, 1/2) as shown in Figs. 2(a), 3(d), and 3(h). As the energy is increased above the resonance energy, magnetic excitations disperse in an anisotropic manner (see Fig. 4). Thus our results are consistent with an upwardly dispersing mode which is strongest near q = (1/2, 1/2). This is at least qualitatively consistent with theoretical predictions for a s^{\pm} state. ¹⁰ Interestingly, this contrasts with the behavior in YBa₂Cu₃O_{6+x}, where the resonance mode disperses downwards in energy.^{30–32}

An important result from our experiment is the observation of dispersive anisotropic spin fluctuations up to 80 meV. Neutron scattering studies on the antiferromagnetic parents of the 122 series, BaFe2As2 (Refs. 14 and 15) and CaFe₂As₂, ^{16,17} have observed spin-wave excitations up to about 200 meV. Unfortunately, single-crystal measurements up to 80 meV only exist for CaFe₂As₂. The magnetic excitations have been analyzed using a spin-wave model based on localized moments. Ba(Fe_{0.935}Co_{0.065})₂As₂ is close to magnetic order at low temperature. In order to parameterize our data we use a damped spin-wave cross section with an energy gap. In our case, the gap Δ in Eq. (3) is due to the superconductivity (and the formation of the resonance described above). We find that Eqs. (2) and (3) provide a good description of the data (as illustrated by Figs. 2 and 3) with $\Gamma/E=0.15$ (as per Ref. 17). This method of analysis produces spin-wave velocities of $v_{\parallel} = 580 \pm 60 \text{ meV Å}, v_{\perp}$ $=230\pm30$ meV Å, and $\Delta=10\pm0.5$ meV. Using the published exchange constants, we obtain spin-wave velocities for the parent compound CaFe₂As₂ of v_{\parallel} =513 (Ref. 16) or 494 meV Å (Ref. 17) and $v_{\perp} = 370$ (Ref. 16) or 348 meV Å.17 If the magnetic interactions are described using a Heisenberg Hamiltonian

$$H = J_1 \sum_{\langle jk \rangle} \mathbf{S}_j \cdot \mathbf{S}_k + J_2 \sum_{\langle \langle jk \rangle \rangle} \mathbf{S}_j \cdot \mathbf{S}_k, \tag{7}$$

where the sums are over nearest-neighbor and next-nearest-neighbor pairs (see Fig. 1), we can convert the spin-wave velocities to effective exchange constants based on spin-wave theory in the ordered parent antiferromagnets. Using the relations $v_{\parallel} = S\sqrt{2}a(J_1+2J_2)$ and $v_{\perp} = S\sqrt{2}a\sqrt{(2J_2+J_1)(2J_2-J_1)}$ (see Refs. 14, 16, 17, and 33), we obtain $J_1 = 43 \pm 7$ and $J_2 = 30 \pm 3$ meV. It should be noted that this is not the only possible analysis, but it is the simplest. It may also be possible to interpret the data in terms of the J_{1a} - J_{1b} - J_2 model 17,34 which has been used to describe the ordered parent CaFe₂As₂. However $|J_{1a}$ - $J_{1b}|$ is certainly less for Ba(Fe_{0.935}Co_{0.065})₂As₂.

In addition to comparing the spin-wave velocities with the parent compounds, we can also compare the strength of the magnetic response. Figure 5 shows the wave-vectoraveraged or local susceptibility $\chi''(\omega)$ defined by Eq. (4). In the case of Ba(Fe_{0.935}Co_{0.065})₂As₂, we have averaged over $0 \le h < 1$ and $0 \le k < 1$, and ± 0.25 around various odd, even, and noninteger l values (see caption to Fig. 5). As mentioned above, points with different l appear to follow the same trend, suggesting that there is no l dependence to this partially averaged quantity. Thus, the graph represents the true $\chi''(\omega)$. For comparison, we have computed $\chi''(\omega)$ for $CaFe_2As_2$ using the exchange constants and S_{eff} from Ref. 17. This result is shown as the dashed line²⁰ in Fig. 5. We that the response is slightly note larger Ba(Fe_{0.935}Co_{0.065})₂As₂ over the energy range investigated here. The same phenomenon occurs in the cuprates where, for example, the spin fluctuations are stronger in optimally doped La_{2-x}Sr_xCuO₄ than in La₂CuO₄.^{23,35} One might understand this increase at lower energies as being due to a shift in spectral weight from higher energies (above the window of the present experiment) and the loss of the peak due to magnetic order present in the ordered compounds.

It is interesting to compare the present results with those obtained on the cuprates. First, we note that the magnitude of the local susceptibility is similar in optimally doped La_{2-x}Sr_xCuO₄ (Refs. 23 and 35) and Ba(Fe_{0.935}Co_{0.065})₂As₂. Both the cuprates and Ba(Fe_{0.935}Co_{0.065})₂As₂ show a strong response near the \mathbf{Q} =(1/2,1/2). In La_{2-x}Sr_xCuO₄ and YBa₂Cu₃O_{6+x}, various dispersive modes and "resonance" features^{23,30–32} are observed below $E \lesssim 50$ meV. At higher energies, $50 \lesssim E \lesssim 100$ meV, the response in YBa₂Cu₃O_{6+x} and La_{2-x}Sr_xCuO₄ is quasi-isotropic or has fourfold symmetry about the (1/2,1/2) position.^{23,36–38} In contrast, the response in Ba(Fe_{0.935}Co_{0.065})₂As₂ is more anisotropic being broader along (1/2- ξ ,1/2+ ξ) than the (1/2+ ξ ,1/2+ ξ). We discuss possible origins of this anisotropy below.

Discussion about the best way to describe the magnetic interactions in the ferropnictides continues. 33,34,39,40 These materials are not Mott insulators with localized spins which can be described purely by near-neighbor superexchange. Neither are the ferropnictides weakly correlated metallic systems. It appears that Hund's rule coupling is responsible for producing the atomic moments and there is also strong magnetoelastic coupling. Keeping this is mind, we discuss our results in terms of an effective Heisenberg coupling and a weakly correlated metallic picture.

There is evidence that the ferropnictides develop an underlying electron nematic phase^{33,41,42} as they approach the magnetic ordering temperature. That is, they show fluctuating magnetic stripes based on the ordering shown in Fig. 1(a). While $Ba(Fe_{0.935}Co_{0.065})_2As_2$ does not appear to order magnetically, it is close to the antiferromagnetic quantum critical point;^{5–7} therefore, similar considerations should apply. It has been known for some time⁴³ that 2D square-lattice systems described by the Hamiltonian in Eq. (7) develop a stripelike order of the type observed in the ferropnictides for $J_2/J_1 > 1/2$ which is the condition here (our measurements give $J_2/J_1=0.70\pm0.09$). Although the Hamiltonian in Eq. (7) has a C_4 lattice symmetry, we expect low-frequency correlations to develop at low temperature through the so-called "order out of disorder" mechanism. 33,43,44 This means instantaneous collinear order described by two interpenetrating Néel sublattices as shown in Fig. 1(a). The higher-energy magnetic excitations of such a state with long-lived correlations of this type might be expected to be similar to the excitations of the corresponding ordered antiferromagnet. This could explain the similarities between the magnetic exin citations the 10 < E < 80 meVrange $Ba(Fe_{0.935}Co_{0.065})_2As_2$ and $CaFe_2As_2$. ^{16,17}

The second approach which has been used to describe the ferropnictides is that based on nesting between the electron and hole pockets. 10,12,13,39,45 In such a picture, the magnetic excitations are correlated electron-hole pairs. The canonical example of an itinerant antiferromagnet which is described by such a picture is elemental chromium. 46 Model Lindhard calculations of the wave-vector-dependent susceptibility $\chi(\mathbf{q},\omega)$ (Refs. 13 and 45) based on the band structure appear to reproduce the q anisotropy in $\chi''(\mathbf{q},\omega)$ observed here at higher energies. In particular, the response is broader along $(1/2-\xi, 1/2+\xi)$ rather than the $(1/2+\xi, 1/2+\xi)$ for a given energy. It is interesting to note that highly structured magnetic excitations, characteristic of nesting, have recently been observed in $FeTe_{1-x}Se_x$. ^{24,47,48} For $FeTe_{0.51}Se_{0.49}$, an anisotropic response similar to the one reported here is observed. The authors of Ref. 24 found that the Sato-Maki cross section [Eq. (6)] provides a good description of their data over a 10-120 meV energy range. Motivated by this we also fitted our data to the Sato-Maki form (see Fig. 2). While the Sato-Maki function provides a reasonable description of the data, the phenological spin-wave cross section provides a better description at higher energies.

V. CONCLUSIONS

In summary, we have used inelastic neutron scattering to probe the collective spin excitations of near optimally doped Ba(Fe_{1-x}Co_x)₂As₂ (x=0.065). Strongly dispersive spin fluctuations are observed up to 80 meV. In the superconducting state, our measurements are consistent with a mode dispersing from the spin resonance near Q=(1/2,1/2) to high energy. At higher energies, we observe excitations which are anisotropic as a function of in-plane wave vector. The response is centered on the M or (1/2,1/2) position of the Brillouin zone and is broader along $(1/2-\xi,1/2+\xi)$ rather than the $(1/2+\xi,1/2+\xi)$ direction. This anisotropy may be understood in terms of multiple J_1 - J_2 exchange interactions or response functions derived from the band structure. When placed on an absolute scale, our measurements show that the local- or wave-vector-integrated susceptibility is generally larger in magnitude than that of the ordered parent antiferromagnets over the energy range probed here.

Note added. Diallo *et al.*⁴⁹ recently reported magnetic fluctuations in the paramagnetic state of CaFe₂As₂ which are similar to those presented here.

ACKNOWLEDGMENTS

We acknowledge useful discussions with J. P. Rodriguez, Pengcheng Dai, and Jun Zhao.

¹Y. Kamihara, T. Watanabe, M. Hirano, and H. Hosono, J. Am. Chem. Soc. **130**, 3296 (2008).

²L. Boeri, O. V. Dolgov, and A. A. Golubov, Phys. Rev. Lett. 101, 026403 (2008).

³M. Rotter, M. Tegel, D. Johrendt, I. Schellenberg, W. Hermes, and R. Pottgen, Phys. Rev. B **78**, 020503(R) (2008).

⁴A. S. Sefat, R. Jin, M. A. McGuire, B. C. Sales, D. J. Singh, and

D. Mandrus, Phys. Rev. Lett. 101, 117004 (2008).

⁵N. Ni, M. E. Tillman, J. Q. Yan, A. Kracher, S. T. Hannahs, S. L. Bud'ko, and P. C. Canfield, Phys. Rev. B **78**, 214515 (2008).

⁶J.-H. Chu, J. G. Analytis, C. Kucharczyk, and I. R. Fisher, Phys. Rev. B **79**, 014506 (2009).

⁷C. Lester, J.-H. Chu, J. G. Analytis, S. C. Capelli, A. S. Erickson, C. L. Condron, M. F. Toney, I. R. Fisher, and S. M. Hayden,

- Phys. Rev. B 79, 144523 (2009).
- ⁸I. I. Mazin, D. J. Singh, M. D. Johannes, and M. H. Du, Phys. Rev. Lett. **101**, 057003 (2008).
- ⁹V. Barzykin and L. P. Gorkov, JETP Lett. **88**, 131 (2008).
- ¹⁰M. M. Korshunov and I. Eremin, Phys. Rev. B **78**, 140509(R) (2008).
- ¹¹ V. Cvetkovic and Z. Tesanovic, EPL **85**, 37002 (2009).
- ¹² A. V. Chubukov, D. V. Efremov, and I. Eremin, Phys. Rev. B 78, 134512 (2008).
- ¹³ S. Graser, T. A. Maier, P. J. Hirschfeld, and D. J. Scalapino, New J. Phys. **11**, 025016 (2009).
- ¹⁴R. A. Ewings, T. G. Perring, R. I. Bewley, T. Guidi, M. J. Pitcher, D. R. Parker, S. J. Clarke, and A. T. Boothroyd, Phys. Rev. B 78, 220501(R) (2008).
- ¹⁵ K. Matan, R. Morinaga, K. Iida, and T. J. Sato, Phys. Rev. B 79, 054526 (2009).
- ¹⁶S. O. Diallo, V. P. Antropov, T. G. Perring, C. Broholm, J. J. Pulikkotil, N. Ni, S. L. Bud'ko, P. C. Canfield, A. Kreyssig, A. I. Goldman, and R. J. McQueeney, Phys. Rev. Lett. **102**, 187206 (2009).
- ¹⁷ J. Zhao, D. T. Adroja, D.-X. Yao, R. Bewley, S. Li, X. F. Wang, G. Wu, X. H. Chen, J. Hu, and P. Dai, Nat. Phys. 5, 555 (2009).
- ¹⁸Further details of the MAPS spectrometer are given on the ISIS website. (www.isis.rl.ac.uk).
- ¹⁹In the present experiment we assume that $\chi''_{\alpha\alpha}(\mathbf{q},\omega)$ is isotropic with respect to field direction. Thus the susceptibilities quoted correspond to $\chi'' = (1/3)(\chi''_{xx} + \chi''_{yy} + \chi''_{zz})$.
- ²⁰The local susceptibility shown in Fig. 4 of Ref. 17 is defined by Eq. (4) but averaged over one Brillouin zone (0.5 < h < 1.5, -0.5 < k < 0.5, 0.5 < l < 1.5) of the extended zone scheme in orthorhomic notation. The average shown in Fig. 5 of the present paper corresponds to averaging wave vectors over several orthorhomic Brillouin zones (0 < h < 2, -1 < k < 1, 0 < l < 2). It is necessary to sample all representative wave vectors of $\chi''(\mathbf{q}, \omega)$ which varies between zones in this case. The authors of Ref. 17 obtain a larger value for $\chi''(\omega)$ because they average over the Brillouin zone where the response is strongest.
- ²¹ H. Sato and K. Maki, Int. J. Magn. 6, 183 (1974).
- ²²D. R. Noakes, T. M. Holden, E. Fawcett, and P. C. de Camargo, Phys. Rev. Lett. **65**, 369 (1990).
- ²³B. Vignolle, S. M. Hayden, D. F. McMorrow, H. M. Ronnow, B. Lake, C. D. Frost, and T. G. Perring, Nat. Phys. 3, 163 (2007).
- ²⁴M. Lumsden, A. Christianson, E. Goremychkin, S. Nagler, H. Mook, M. Stone, D. Abernathy, T. Guidi, G. MacDougall, C. de la Cruz, A. Sefat, M. McGuire, B. Sales, and D. Mandrus, arXiv:0907.2417, Nat. Phys. (to be published).
- ²⁵ A. D. Christianson, E. A. Goremychkin, R. Osborn, S. Rosen-kranz, M. D. Lumsden, C. D. Malliakas, I. S. Todorov, H. Claus, D. Y. Chung, M. G. Kanatzidis, R. I. Bewley, and T. Guidi, Nature (London) 456, 930 (2008).
- ²⁶M. D. Lumsden, A. D. Christianson, D. Parshall, M. B. Stone, S. E. Nagler, G. J. MacDougall, H. A. Mook, K. Lokshin, T. Egami, D. L. Abernathy, E. A. Goremychkin, R. Osborn, M. A. McGuire, A. S. Sefat, R. Jin, B. C. Sales, and D. Mandrus, Phys.

- Rev. Lett. 102, 107005 (2009).
- ²⁷ S. Chi, A. Schneidewind, J. Zhao, L. W. Harriger, L. Li, Y. Luo, G. Cao, Z. Xu, M. Loewenhaupt, J. Hu, and P. Dai, Phys. Rev. Lett. **102**, 107006 (2009).
- ²⁸S. Li, Y. Chen, S. Chang, J. W. Lynn, L. Li, Y. Luo, G. Cao, Z. Xu, and P. Dai, Phys. Rev. B **79**, 174527 (2009).
- ²⁹D. Inosov, J. Park, P. Bourges, D. Sun, Y. Sidis, A. Schneidewind, K. Hradil, D. Haug, C. Lin, B. Keimer, and V. Hinkov, arXiv:0907.3632, Nat. Phys. (to be published).
- ³⁰H. A. Mook, P. C. Dai, S. M. Hayden, G. Aeppli, T. G. Perring, and F. Dogan, Nature (London) 395, 580 (1998).
- ³¹ M. Arai, T. Nishijima, Y. Endoh, T. Egami, S. Tajima, K. Tomimoto, Y. Shiohara, M. Takahashi, A. Garrett, and S. M. Bennington, Phys. Rev. Lett. 83, 608 (1999).
- ³²P. Bourges, Y. Sidis, H. F. Fong, L. P. Regnault, J. Bossy, A. Ivanov, and B. Keimer, Science 288, 1234 (2000).
- ³³C. Fang, H. Yao, W.-F. Tsai, J. P. Hu, and S. A. Kivelson, Phys. Rev. B **77**, 224509 (2008).
- ³⁴T. Yildirim, Phys. Rev. Lett. **101**, 057010 (2008).
- ³⁵S. M. Hayden, G. Aeppli, H. A. Mook, T. G. Perring, T. E. Mason, S. W. Cheong, and Z. Fisk, Phys. Rev. Lett. **76**, 1344 (1996).
- ³⁶S. M. Hayden, H. A. Mook, P. C. Dai, T. G. Perring, and F. Dogan, Nature (London) 429, 531 (2004).
- ³⁷C. Stock, W. J. L. Buyers, R. A. Cowley, P. S. Clegg, R. Coldea, C. D. Frost, R. Liang, D. Peets, D. Bonn, W. N. Hardy, and R. J. Birgeneau, Phys. Rev. B 71, 024522 (2005).
- ³⁸ V. Hinkov, P. Bourges, S. Pailhes, Y. Sidis, A. Ivanov, C. D. Frost, T. G. Perring, C. T. Lin, D. P. Chen, and B. Keimer, Nat. Phys. 3, 780 (2007).
- ³⁹ D. J. Singh, M. H. Du, L. Zhang, A. Subedi, and J. An, Physica C 469, 886 (2009).
- ⁴⁰M. D. Johannes and I. I. Mazin, Phys. Rev. B **79**, 220510(R) (2009).
- ⁴¹C. Xu, M. Muller, and S. Sachdev, Phys. Rev. B **78**, 020501(R) (2008).
- ⁴²I. I. Mazin and M. D. Johannes, Nat. Phys. **5**, 141 (2009).
- ⁴³ P. Chandra, P. Coleman, and A. I. Larkin, Phys. Rev. Lett. **64**, 88 (1990).
- ⁴⁴C. Xu, Y. Qi, and S. Sachdev, Phys. Rev. B **78**, 134507 (2008).
- ⁴⁵ A. N. Yaresko, G. Q. Liu, V. N. Antonov, and O. K. Andersen, Phys. Rev. B **79**, 144421 (2009).
- ⁴⁶E. Fawcett, Rev. Mod. Phys. **60**, 209 (1988).
- ⁴⁷Y. Qiu, W. Bao, Y. Zhao, C. Broholm, V. Stanev, Z. Tesanovic, Y. C. Gasparovic, S. Chang, J. Hu, B. Qian, M. Fang, and Z. Mao, Phys. Rev. Lett. **103**, 067008 (2009).
- ⁴⁸S. Li, C. Zhang, M. Wang, H. Luo, E. Faulhaber, A. Schneidewind, J. Hu, T. Xiang, and P. Dai, arXiv:1001.1505 (unpublished).
- ⁴⁹S. Diallo, D. Pratt, R. Fernandes, W. Tian, J. Zarestky, M. Lumsden, T. Perring, C. Broholm, N. Ni, S. Bud'ko, P. Canfield, H. Li, D. Vaknin, A. Kreyssig, A. Goldman, and R. McQueeney, arXiv:1001.2804 (unpublished).