## MATHEMATICAL AND COMPUTATIONAL SCIENCE

## Director: Bradley Efron

Associate Director: Susan Holmes
Committee in Charge: Takeshi Amemiya (Economics), Gunnar Carlsson (Mathematics), Richard Cottle (Management Science and Engineering), Thomas M. Cover (Electrical Engineering, Statistics), Bradley Efron (Statistics), Peter W. Glynn (Management Science and Engineering), Gene Golub (Computer Science), J. Michael Harrison (Graduate School of Business), Susan Holmes (Statistics), Doron Levy (Mathematics), Parviz Moin (Engineering), Art Owen (Statistics), George Papanicolaou (Mathematics), Eric Roberts (Computer Science), David Rogosa (Education), Tim Roughgarden (Computer Science), David Siegmund (Statistics), Arthur F. Veinott Jr. (Management Science and Engineering)
Program Administrator: Helen Tombropoulos
Program Offices: Sequoia Hall, 390 Serra Mall
Mail Code: 94305-4065
Phone: (650) 723-2620
Email: helen@stat.stanford.edu
Web Site: http://www.stanford.edu/group/mathcompsci
Courses given in Mathematical and Computational Science have the subject code MCS. For a complete list of subject codes, see Appendix.

This interdepartmental interschool undergraduate program provides a major for students interested in the mathematical and computational sciences, or in the use of mathematical ideas and analysis in problems in the social or management sciences. It provides a core of mathematics basic to all the mathematical sciences and an introduction to concepts and techniques of automatic computation, optimal decision making, probabilistic modeling, and statistical inference. It also provides an opportunity for elective work in any of Stanford's mathematical science disciplines.

The program uses the faculty and courses of the departments of Computer Science, Management Science and Engineering, Mathematics, and Statistics. It prepares students for graduate study or employment in the mathematical and computational sciences or in those areas of applied mathematics which center around the use of computers and are concerned with the problems of the social and management sciences.

A biology option is offered for students interested in applications of mathematics, statistics ,and computer science to the biological sciences (bioinformatics, computational biology, statistical genetics, neurosciences); and in a similar spirit, an engineering option.

## UNDERGRADUATE PROGRAMS BACHELOR OF SCIENCE

The requirement for the bachelor's degree, beyond the University's basic requirements, is an approved course program of 72-77 units, distributed as follows:
Mathematics (MATH): 29-31 units
Qtr. and Units
MATH 41. Calculus
and MATH 42. Calculus
MATH 51. Linear Algebra and Differential Calculus of Several Variables
or MATH 51H. Honors Advanced Calculus
MATH 52. Integral Calculus of Several Variables
$\begin{array}{rr}\mathrm{A} & 5 \\ \mathrm{~A}, \mathrm{~W} & 5\end{array}$ or MATH 52 H . Honors Advanced Calculus A,W,S A,W,S

ATH 53. Ordinary Differential Equations with Linear Algebra A,W,S or MATH 53H. Honors Advanced Calculus
MATH 109. Applied Group Theory (WIM)
or MATH 110. Applied Number Theory and Field Theory (WIM)
or MATH 120. Modern Algebra (WIM)
MATH 113. Linear Algebra and Matrix Theory

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\mathrm{A}, \mathrm{~W}
$$

Computer Science (CS): 16-18 units
CS 103X. Discrete Structures (Accelerated)

CS 106X. Programming Methodology and Abstractions (Accel.) A, W or CS 106A. Programming Methodology

A,W,S and CS 106B. Programming Abstractions W, S

And two of the following (CS or CME):

CME 108. Introduction to Scientific Computing
CS 107. Programming Paradigms
CS 154. Introduction to Automata and Complexity Theory CS 161. Design and Analysis of Algorithms

W
A,S
A,S $\quad 3-4$
A,W 3-4
Management Science and Engineering (MS\&E): 8-9 units Both:
MS\&E 111. Introduction to Optimization (same as ENGR 62) A,S 3-4
MS\&E 121. Introduction to Stochastic Modeling
W 4
or three of the following:
MS\&E 211. Linear and Nonlinear Optimization
A $3-4$
MS\&E 212. Mathematical Programming and
Combinatorial Optimization
MS\&E 221. Stochastic Modeling
MS\&E 251. Stochastic Decision Models
Statistics (STATS): (11 units)
STATS 116. Theory of Probability
STATS 191. Introduction to Applied Statistics or STATS 203. Introduction to Regression Models and Analysis of Variance
STATS 200. Introduction to Statistical Inference

## ELECTIVES (9 UNITS)

Three courses in mathematical and computational science, 100-level or above, at least 3 units each. At least one must be chosen from the following:

ECON 102C. Advanced Topics in Econometrics
ECON 140. Introduction to Financial Economics
ECON 160. Game Theory and Economic Applications $\begin{array}{cr}\text { Qtr. and Units } \\ \mathrm{S} & 5 \\ \mathrm{~S} & 5 \\ \mathrm{~S} & 5\end{array}$ (prerequisite ECON 51)
ECON 179. Experimental Economics (not given 2006-07)
EE 261. The Fourier Transform and its Applications
MS\&E 211. Linear and Nonlinear Optimization
MS\&E 212. Mathematical Programming and
Combinatorial Optimization
MS\&E 221. Stochastic Modeling
MS\&E 251. Stochastic Decision Models
MCS 100. Mathematics of Sports (same as STATS 50)
MATH 106. Functions of a Complex Variable
MATH 108. Introduction to Combinatorics and its Applications
MATH 111. Computational Commutative Algebra (not given 2006-07)
MATH 115. Functions of a Real Variable
MATH 116. Complex Analysis
MATH 118. Numerical Analysis (not given 2006-07)
MATH 131. Partial Differential Equations I
MATH 132. Partial Differential Equations II
MATH 135. Nonlinear Dynamics and Chaos
MATH 136. Stochastic Processes
PHIL 151. First-Order Logic
STATS 202. Data Analysis

|  | 5 |
| ---: | ---: |
| A,S | 3 |
| A | $3-4$ |
|  |  |
| S | 3 |
| W | 3 |
| W | 3 |
| S | 3 |
| A | 3 |
| A | 3 |
| 6-07) | 3 |
| A,W | 3 |
| W | 3 |
|  | 3 |
| A,W | 3 |
| S | 3 |
| S | 3 |
| W | 3 |
| W | 4 |
| A | 3 |
| W | 3 |

STATS 217. Introduction to Stochastic Processes
W
For Computer Science (CS), electives can include courses not taken as units under the CS list above and the following:
CME 302. Numerical Linear Algebra

| A | 3 |
| ---: | ---: |
| A,W | $3-4$ |
| A, W | $3-4$ |
| A, W | $3-4$ |
| A | $3-4$ |
| A, W | $3-4$ |
| S | 3 |
| A | $3-4$ |
| W | 3 |
| W | 3 |
| S | 3 |
| W | 3 |
| A | 3 |
| W | $3-4$ |
|  | 3 |
| S | 3 |

108. Object-Oriented Systems Design CS 140. Operating Systems and Systems Programming CS 143. Compilers
CS 157. Logic and Automated Reasoning
CS 161. Design and Analysis of Algorithms
CS 194. Software Project (prerequisite CS 108)
CS 221. Artificial Intelligence: Principles and Techniques
CS 223A. Introduction to Robotics
CS 223B. Introduction to Computer Vision
CS 225A. Experimental Robotics
CS 228. Probabilistic Models in Artificial Intelligence
CS 229. Machine Learning
CS 243. Advanced Compiling Techniques
EE 275. Logic Design (not given 2006-07)
EE 282. Computer Architecture and Organization
With the adviser's approval, courses other than those offered by the sponsoring departments may be used to fulfill part of the elective requirement. These may be in fields such as biology, economics, electrical engineering, industrial engineering, and medicine, that might be relevant to a mathematical sciences major, depending on a students's interests.
109. At least three quarters before graduation, majors must file with their advisers a plan for completing degree requirements.
110. All courses used to fulfill major requirements must be taken for a letter grade with the exception of courses offered satisfactory/no credit only.
111. A course used to fulfill the requirements of one section of the program may not be applied toward the fulfillment of the requirements of another section.
112. The student must have a grade point average (GPA) of 2.0 or better in all course work used to fulfill the major requirement.

## MATHEMATICAL AND COMPUTATIONAL BIOLOGY OPTION

Replace MATH 109/110 with either:
BIOSCI 221. Methods of Theoretical Population Biology
Qtr. and Units

| S | 4 |
| :--- | :--- |
| S | 3 |

Replace STATS 191/203 by
STATS/BIOSCI 141. Biostatistics
A, W 3-5
Take at least 2 courses from the Biological Sciences core: BIOSCI 41. Genetics and Biochemistry

| A | 5 |
| ---: | ---: |
| W | 5 |
| S | 5 |

BIOSCI 42. Cell Biology and Animal Physiology
BIOSCI 43. Plant Biology, Evolution, and Ecology
Take a third course either from the core or
STATS 166. Statistical Methods in Computational Genetics (WIM)
A

BIOSCI 133. Genetics of Prokaryotes
BIOSCI 134. Replication of DNA
BIOSCI 136. Evolutionary Paleobiology (not given 2006-07) or BIOSCI 203. Advanced Genetics
Honors students should take 3 of the following:
STATS 166. Statistical Methods in Computational Genetics (WIM)
ANTHSCI 180. Intro. to Anthropological Genetics
(not given 2006-07)
ANTHSCI 187. The Genetic Structure of Populations (not given 2006-07)
ANTHSCI 188. Research in Anthropological Genetics
BIOSCI 113. Fundamentals of Molecular Evolution
BIOSCI 146. Population Studies
BIOSCI 146. Population Studies
BIOSCI 221. Methods of Theoretical Population Biology
BIOSCI 183A/283A. Population Genetic Theory and Evolution I (not given 2006-07)
BIOSCI 183B/283B. Population Genetic Theory and Evolution II (not given 2006-07)

## MATHEMATICAL AND COMPUTATIONAL SCIENCE ENGINEERING OPTION

Students in the Engineering option take the introductory courses for the Mathematics and Computational Sciences major with the following allowable substitutions.

The MATH 51-53 series may be replaced by:
CME 100/ENGR 154. Vector Calculus for Engineers
Qtr. and Units
CME 102/ENGR 155A. Ordinary Differential Equatio
A 5
CME 102/ENGR 155A. Ordinary Differential Equations for EngineersW
CME 104/ENGR 155B. Linear Algebra and Partial Differential S
Equations for Engineers
MATH 115. Functions of a Real Variable
A,W
3
STATS 116 may be replaced by either one of the following:
STATS 110. Statistical Methods in Engineering and Physical Sciences A $4-$ or CME 106/ENGR 155C. Introduction to Probability and Statistics for Engineers

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\text { W } \quad 3-4
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STATS 191/STATS 203 may be replaced by:
STATS 202. Data Analysis
Electives; take at least one course from the following list:
MATH 106. Intro to Theory of Functions of a Complex Variable
MATH 108. Intro to Combinatorics Applications
A 3
MATH 116. Complex Analysis
$\begin{array}{rr}\mathrm{A} & 3 \\ \mathrm{~W} & 3\end{array}$
MATH 118. Numerical Analysis (not given 2006-07)
MATH 132. Partial Differential Equations II
S
MATH 139. Intro to the Mathematics of Medical Imaging (not given 2006-07)
PHIL 151. First-Order Logic
Take at least two courses from the following list:
ENGR 15. Dynamics

ENGR 20. Introduction to Chemical Engineering
ENGR 25. Biotechnology
ENGR 30. Engineering Thermodynamics

| S | 3 |
| ---: | ---: |
| S | 3 |
| $\mathrm{~A}, \mathrm{~W}$ | 3 |
| $\mathrm{~A}, \mathrm{~S}$ | 5 |
| $\mathrm{~W}, \mathrm{~S}$ | 4 |
| W | 3 |

ENGR 50. Introductory Science Materials
ENGR 105. Feedback Control Design
W
Take three additional courses from a single engineering department, and two additional courses from any engineering department(s).

## MINORS

The minor in Mathematical and Computational Science is intended to provide an experience of the four constituent areas: Computer Science, Mathematics, ManagementScience and Engineering, and Statistics. Four basic courses are required:
CS 106X. Programming Methodology and Abstractions (Accelerated)
or CS 106A,B. Programming Methodology
MATH 51. Linear Algebra and Differential Calculus of Several Variables or MATH 103. Matrix Theory and its Applications
ENGR 62. Introduction to Optimization
or MS\&E 121. Introduction to Stochastic Modeling
STATS 116. Theory of Probability or STATS 191. Introduction to Applied Statistics
In addition to the above, the minor requires three courses from the
following, two of which must be in different departments:
CME 108. Introduction to Scientific Computing
CS 107. Programming Paradigms
CS 138. MATLAB and MAPLE for Science and Engineering Applications
CS 154. Introduction to Automata and Complexity Theory
EE 261. The Fourier Transform and its Applications
ECON 102C. Advanced Topics in Econometrics
ECON 160. Game Theory and Economic Applications (prerequisite ECON 51)
MS\&E 211. Linear and Nonlinear Optimization
MS\&E 212. Mathematical Programming and Combinatorial Optimization
MS\&E 221. Stochastic Modeling
MS\&E 251. Stochastic Decision Models
MATH 103. Matrix Theory and Its Applications
MATH 106. Functions of a Complex Variable
MATH 108. Introduction to Combinatorics and its Applications
MATH 109. Applied Group Theory
MATH 110. Applied Number Theory and Field Theory
MATH 115. Functions of a Real Variable
or MATH 171. Fundamental Concepts of Analysis
MATH 131. Partial Differential Equations I
MATH 132. Partial Differential Equations II
MATH 135. Nonlinear Dynamics and Chaos PHIL 151. First-Order Logic
STATS 200. Introduction to Statistical Inference
STATS 202. Data Analysis
STATS 203. Introduction to Regression Models and Analysis of Variance
STATS 217. Introduction to Stochastic Processes
Other upper-division courses appropriate to the program major may be substituted with consent of the program director. Undergraduate majors in the constituent programs may not count courses in their own departments.

## HONORS PROGRAM

The honors program is designed to encourage a more intensive study of mathematical sciences than the B.S. program. In addition to meeting all requirements for the B.S., the student must:

1. Maintain an average letter grade equivalent in mathematical sciences courses of at least a 3.4.
2. Complete at least 15 units in mathematical sciences in addition to the requirements for the major listed above. These courses should form a sustained effort in one area and constitute a program approved by the committee in charge of the Mathematical and Computational Science Program.
3. Include in the above 15 units at least one of the following:
a) an approved higher-level graduate course
b) participation in a small group seminar
c) at least 3 units of directed reading

Students interested in doing honors work should consult with their advisers by the last quarter of the junior year to prepare a program of study for submission to the committee in charge for approval. Honors work may be concentrated in fields outside the Mathematical and Computational Science programs such as biological sciences, medicine, physics.

## COURSES

MCS 100. Mathematics of Sports-(Same as STATS 50.) The use of mathematics, statistics, and probability in the analysis of sports performance, sports records, and strategy. Topics include mathematical analysis of the physics of sports and determinations of optimal strategies. New diagnostic statistics and strategies for each sport. Corequisite: STATS 116.

3 units, Spr (Cover)

