

Harmonic Grammar, Gradual Learning, and Phonological Gradience

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June 29, 2007

Harmonic Grammar (HG; Smolensky and Legendre 2006) is a close relative of Optimality Theory (OT; Prince and Smolensky 1993/2004). In HG, the optimal candidate is the one with maximal Harmony, where Harmony is calculated using a simple linear equation. Given a representation's scores on a set of constraints, and a set of coefficients, or weights, Harmony is the sum of the weighted constraint scores. If, as in OT, constraints assign scores based on the number of violations, then the scores are the corresponding negative integers, and the weights are positive reals. An OT-style tableau using Harmony maximization as the criterion for optimality appears in (1). The weights are in the top row, and the rightmost column provides the Harmony values for the candidates. Output₁ has the highest Harmony, and is thus optimal.

(1) A weighted constraint tableau

<i>Weight</i>	2	1	\mathcal{H}
Input	Constraint 1	Constraint 2	
☞ Output ₁		-1	-1
Output ₂	-1		-2

OT's use of ranking rather than weighting is sometimes justified in terms of its restrictiveness: weighted interaction is claimed to be too powerful for HG to function as a realistic model of human language (Prince and Smolensky 1993/2004: 236; 1997: 1608, Legendre et al. 2006b).

In this talk, I present results of several ongoing collaborative research projects on HG. I will discuss the following points:

- (2) i. HG is (perhaps surprisingly) restrictive, due to inherent limitations on the types of languages that can be generated by an optimization system (Bhatt et al. 2007; Pater et al. 2007)
- ii. HG is compatible with a simple correctly convergent gradual learning algorithm, the Perceptron algorithm of Rosenblatt (1958) (Boersma and Pater 2007; Pater 2007; see Jäger 2006, Soderstrom et al. 2006 for precedents).
- iii. To deal with variation, HG can be implemented with noise, as in stochastic OT (Boersma 1998; Boersma and Hayes 2001). Testing shows that the noisy HG+Perceptron combination is robust, unlike the stochastic OT+GLA one (Boersma and Pater 2007).
- iv. Gradual learning yields Harmony values that reflect frequency distributions. A problem for the HG account of gradient well-formedness (Keller 2006; Legendre et al. 2006a) raised by Boersma (2004) can be resolved with a revised HG acceptability metric (Coetzee and Pater 2007).

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