

## Modification and quantification

Ling233B, Resource accounting at the syntax-semantics interface  
Monday, January 28, 2002

Quantification: The aim

*Every student yawns.*

$$\left[ \begin{array}{l} \text{PRED} \quad \text{'yawn'} \\ \text{SUBJ} \quad \left[ \begin{array}{l} \text{PRED} \quad \text{'student'} \\ \text{SPEC} \quad \text{'every'} \end{array} \right] \end{array} \right]$$

$every(X, student(X), yawn(X))$

- *every* is a *quantifier*
- *student* is its *restriction*
- *yawn* is its *scope*

A simpler example

*Everyone yawns.*

$$\left[ \begin{array}{l} \text{PRED} \quad \text{'yawn'} \\ \text{SUBJ} \quad \left[ \text{PRED} \quad \text{'everyone'} \right] \end{array} \right]$$

$every(X, person(X), yawn(X))$

Meaning contribution of *everyone*:  $\lambda S. every(X, person(X), S(X))$

Meaning contribution of *yawns*:  $\lambda x. yawn(x)$

Goal: combine *everyone* and *yawns* appropriately.

## Quantification in glue

$\forall H.[e_\sigma \multimap H] \multimap H$

Given a resource  $e_\sigma \multimap H$  for some semantic structure  $H$ , we can produce a resource for  $H$ .

$e_\sigma \multimap y_\sigma$

Given a resource  $e_\sigma$  corresponding to the SUBJ, we can produce a resource  $y_\sigma$  for the entire sentence.

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$y_\sigma$

We have produced a resource  $y_\sigma$  for the full sentence.

$\lambda S.\text{every}(X, \text{person}(X), S(X)) : \forall H.[e_\sigma \multimap H] \multimap H$

Glue: given a resource  $e_\sigma \multimap H$  for some semantic structure  $H$ , we can produce a resource for  $H$ . Meaning: apply the predicate  $\lambda S.\text{every}(X, \text{person}(X), S(X))$  to the meaning corresponding to the resource  $e_\sigma \multimap H$ .

$\lambda Y.\text{yawn}(Y) : e_\sigma \multimap y_\sigma$

Glue: given a resource  $e_\sigma$  corresponding to the SUBJ, we can produce a resource  $y_\sigma$  for the entire sentence. Meaning:  $\lambda Y.\text{yawn}(Y)$ .

$\text{every}(X, \text{person}(X), \text{yawn}(X)) : y_\sigma$

We have produced a resource  $y_\sigma$  corresponding to  $\text{every}(X, \text{person}(X), \text{yawn}(X))$ , by assuming that  $H$  is the semantic structure  $y_\sigma$ .

We have seen:

- Combining *everyone* with its scope

Next:

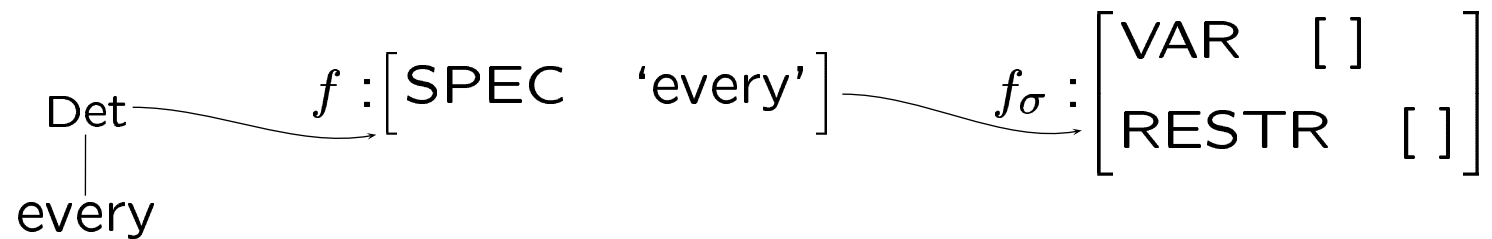
- Combining *every* with *student* to form a meaning constructor like the one for *everyone*

F-structure of a quantified NP, *every student*:

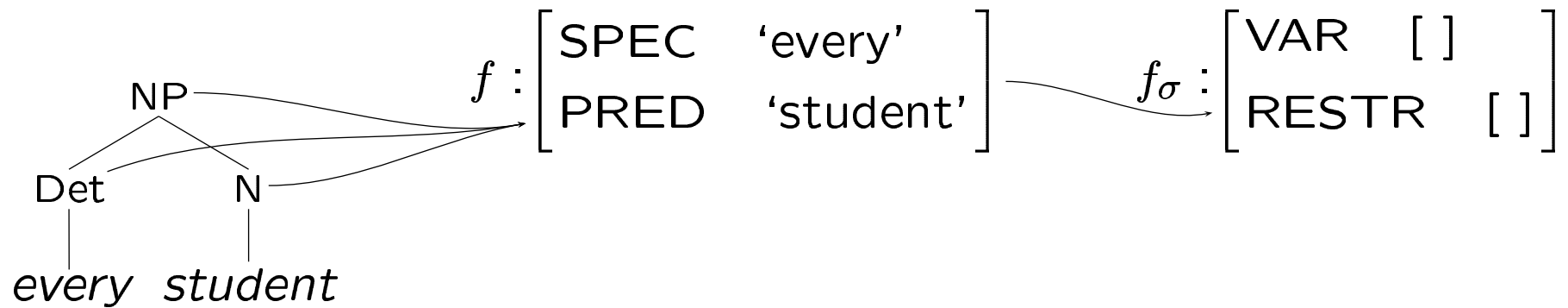
$$f: \left[ \begin{array}{ll} \text{SPEC} & \text{'every'} \\ \text{PRED} & \text{'student'} \end{array} \right]$$

*restr-arg* and *restr* are contributed by 'student' and its arguments and modifiers, if any; this does not correspond to a syntactically well-motivated f-structure constituent.

F-structure and semantic structure for determiners:



C-structure, f-structure, and semantic structures for *every student*:



**every**       $\lambda R. \lambda S. \text{every}(X, R(X), S(X)) : [v \multimap r] \multimap [\forall H. [e_\sigma \multimap H] \multimap H]$

**student**                       $\lambda X. \text{student}(X) : v \multimap r$

$\lambda R.\lambda S.every(X, R(X), S(X)) : [v \multimap r] \multimap [\forall H.[e_\sigma \multimap H] \multimap H]$

*every* requires a resource  $v \multimap r$  corresponding to its restriction meaning  $R$ , and a resource  $e_\sigma \multimap H$  corresponding to its scope meaning  $S$ , to produce a resource  $H$ .

$\lambda X.student(X) : v \multimap r$

This meaning constructor provides an implicational resource  $v \multimap r$  and meaning  $\lambda X.student(X)$ .

$\lambda S.every(X, student(X), S(X)) : \forall H.[e_\sigma \multimap H] \multimap H$

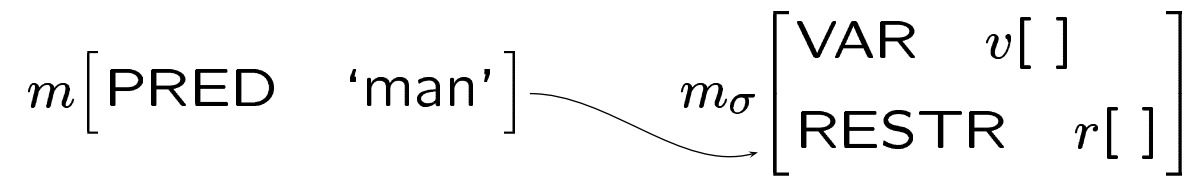
The result is like the meaning constructor for *everyone*, except that the restriction of the quantifier *every* is specified to involve students.



# Modification

## Nouns: Syntax and semantics

*man*



$\lambda X. \text{man}(X) : v \multimap r$

## Noun modification by intersective adjective

*Swedish man*

$$\left[ \begin{array}{l} \text{PRED} \quad \text{'man'} \\ \text{ADJ} \quad \left\{ \left[ \text{PRED} \quad \text{'Swedish'} \right] \right\} \end{array} \right] \longrightarrow \left[ \begin{array}{l} \text{VAR} \quad v[ ] \\ \text{RESTR} \quad r[ ] \end{array} \right]$$

$$\lambda X. \text{Swedish}(X) \wedge \text{man}(X) : v \multimap r$$

Intersective modification:

$X$  is in the intersection of men and Swedish things.

Noun modification by gradable adjective  
 (Montague 1974; Kamp 1975; Kennedy 1997)

*big mouse*

$$\left[ \begin{array}{l} \text{PRED} \quad \text{'mouse'} \\ \text{ADJ} \quad \{ \left[ \text{PRED} \quad \text{'big'} \right] \} \end{array} \right] \longrightarrow \left[ \begin{array}{l} \text{VAR} \quad v[ ] \\ \text{RESTR} \quad r[ ] \end{array} \right]$$

$$\lambda X. \text{big}(X, \mathcal{P}) \wedge \text{mouse}(X) : v \multimap r$$

$X$  is a mouse, and is big relative to individuals that have the property  $\mathcal{P}$ ;  
 here  $\mathcal{P}$  is the property of being a mouse.

$\lambda X. big(X, \mathcal{P}) \wedge mouse(X) : v \multimap r$

What is  $\mathcal{P}$ ? – A contextually-salient property of  $X$   
(McConnell-Ginet 1979; Pollard and Sag 1994; Kennedy 1997)

The Linguistics Department has an important volleyball game coming up against the Philosophy Department. I see the Phils have recruited Julius to play with them, which means we are in real trouble unless we can find a good linguist to add to our team in time for the game. (Pollard and Sag 1994)

Noun modification by intensional adjective  
 (Kamp 1975; Siegel 1976)

*former senator*

$$\left[ \begin{array}{l} \text{PRED} \quad \text{'senator'} \\ \text{ADJ} \quad \left\{ \left[ \text{PRED} \quad \text{'former'} \right] \right\} \end{array} \right] \longrightarrow \left[ \begin{array}{l} \text{VAR} \quad v[ ] \\ \text{RESTR} \quad r[ ] \end{array} \right]$$

$$\lambda X. \text{former}(\text{senator}, X) : v \multimap r$$

$X$  is an individual that stands in the *former* relation to the property of being a senator.

We have seen:

- Noun modifiers: Syntax and semantics

Next:

- How modified noun meanings are obtained by semantic deduction

*Swedish man*

$$\left[ \begin{array}{l} \text{PRED} \quad \text{'man'} \\ \text{ADJ} \quad \left\{ \left[ \text{PRED} \quad \text{'Swedish'} \right] \right\} \end{array} \right] \longrightarrow \left[ \begin{array}{l} \text{VAR} \quad v[ ] \\ \text{RESTR} \quad r[ ] \end{array} \right]$$

**man**

$$\lambda X. \text{man}(X) : v \multimap r$$

**Swedish**

$$\lambda P. \lambda X. \text{Swedish}(X) \wedge P(X) : [v \multimap r] \multimap [v \multimap r]$$

General form of modifiers:  $\mathcal{M} : S \multimap S$

$\lambda X.man(X) : v \multimap r$

The meaning  $\lambda X.man(X)$  is associated with the implicational contribution  $v \multimap r$ .

$\lambda P.\lambda X.Swedish(X) \wedge P(X) : [v \multimap r] \multimap [v \multimap r]$

Glue: The meaning constructor consumes the noun contribution  $v \multimap r$  and produces a new modified meaning which is also associated with  $v \multimap r$ . Meaning: apply the function  $\lambda P.Swedish(X) \wedge P(X)$  to the unmodified meaning contributed by  $man$ ,  $\lambda X.man(X)$ .

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$\lambda X.Swedish(X) \wedge man(X) : v \multimap r$

We have produced a modified meaning  $\lambda X.Swedish(X) \wedge man(X)$  associated with the implicational contribution  $v \multimap r$ .

*big mouse*

$$\left[ \begin{array}{l} \text{PRED} \quad \text{'mouse'} \\ \text{ADJ} \quad \{ \left[ \text{PRED} \quad \text{'big'} \right] \} \end{array} \right] \longrightarrow \left[ \begin{array}{l} \text{VAR} \quad v[ ] \\ \text{RESTR} \quad r[ ] \end{array} \right]$$

**mouse**                     $\lambda X. \text{mouse}(X) : v \multimap r$

**big**                     $\lambda R. \lambda X. \text{big}(X, \mathcal{P}) \wedge R(X) : [v \multimap r] \multimap [v \multimap r]$

**big, mouse**  $\vdash \lambda X. \text{big}(X, \mathcal{P}) \wedge \text{mouse}(X) : v \multimap r$

*former senator*

$$\left[ \begin{array}{l} \text{PRED} \quad \text{'senator'} \\ \text{ADJ} \quad \left\{ \left[ \text{PRED} \quad \text{'former'} \right] \right\} \end{array} \right] \longrightarrow \left[ \begin{array}{l} \text{VAR} \quad v[ ] \\ \text{RESTR} \quad r[ ] \end{array} \right]$$

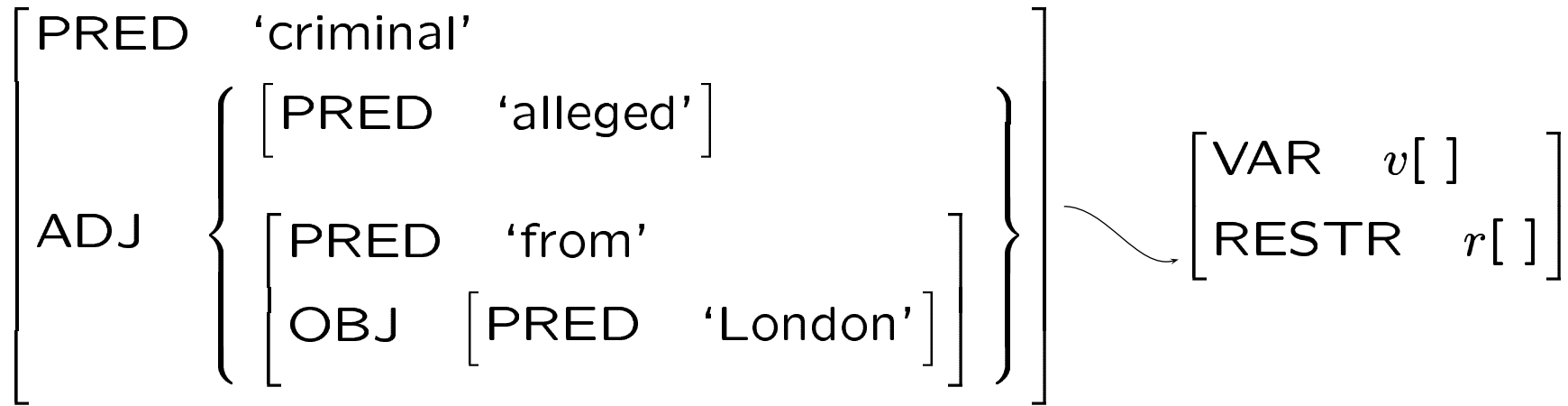
**senator**       $\lambda X. \text{senator}(X) : v \multimap r$

**former**     $\lambda P. \lambda X. \text{former}(P, X) : [v \multimap r] \multimap [v \multimap r]$

**former, senator**  $\vdash \lambda X. \text{former}(\text{senator}, X) : v \multimap r$

Scope ambiguity = Different deductions from the same premises

*alleged criminal from London*



**criminal**

$\lambda X.criminal(X) : v \multimap r$

**alleged**

$\lambda P.\lambda X.alleged(P, X) : [v \multimap r] \multimap [v \multimap r]$

**from-London**

$\lambda R.\lambda X.from(X, London) \wedge R(X) : [v \multimap r] \multimap [v \multimap r]$

Two deductions from the same premises:

**alleged, criminal, from-London**  $\vdash$   
 $\lambda X. \text{alleged}(\lambda Y. \text{criminal}(Y) \wedge \text{from}(Y, \text{London}), X) : v \multimap r$

**alleged, criminal, from-London**  $\vdash$   
 $\lambda X. \text{alleged}(\text{criminal}, X) \wedge \text{from}(X, \text{London}) : v \multimap r$

We have seen:

- Nouns and their modifiers at the syntax-semantics interface: How modified meanings are obtained

Next:

- A puzzle: Modifying a modifier

'Recursive modification' (Kasper 1995)

*Swedish*

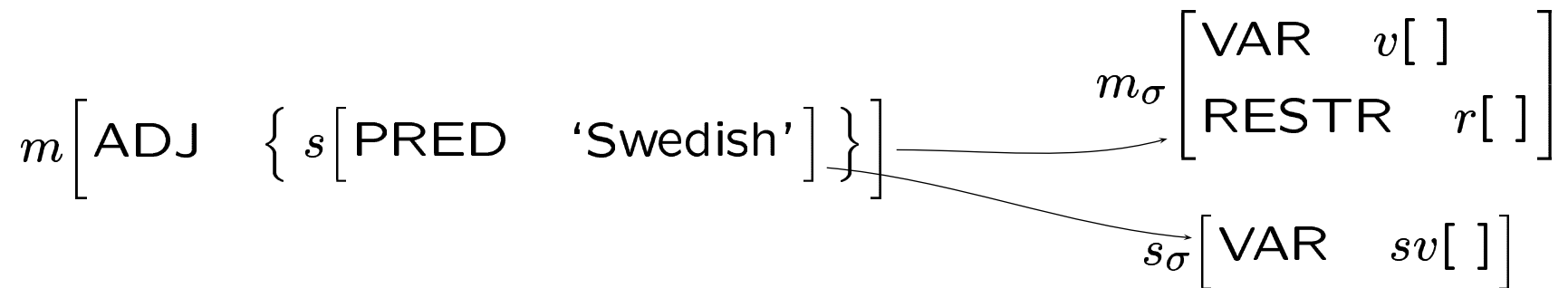
$\lambda P.\lambda X.Swedish(X) \wedge P(X) : [v \multimap r] \multimap [v \multimap r]$

*apparently Swedish*

$\lambda P.\lambda X.apparently(Swedish(X)) \wedge P(X) : [v \multimap r] \multimap [v \multimap r]$

General problem for categorial-style analyses.

Solution: Decomposition of meaning of modifiers.



**Swedish1**                     $\lambda X. \text{Swedish}(X) : [sv \multimap s_\sigma]$

**Swedish2**    $\lambda Q. \lambda P. \lambda X. Q(X) \wedge P(X) : [sv \multimap s_\sigma] \multimap [[v \multimap r] \multimap [v \multimap r]]$

Original adjective meaning **Swedish**  
deducible from **Swedish1** and **Swedish2**

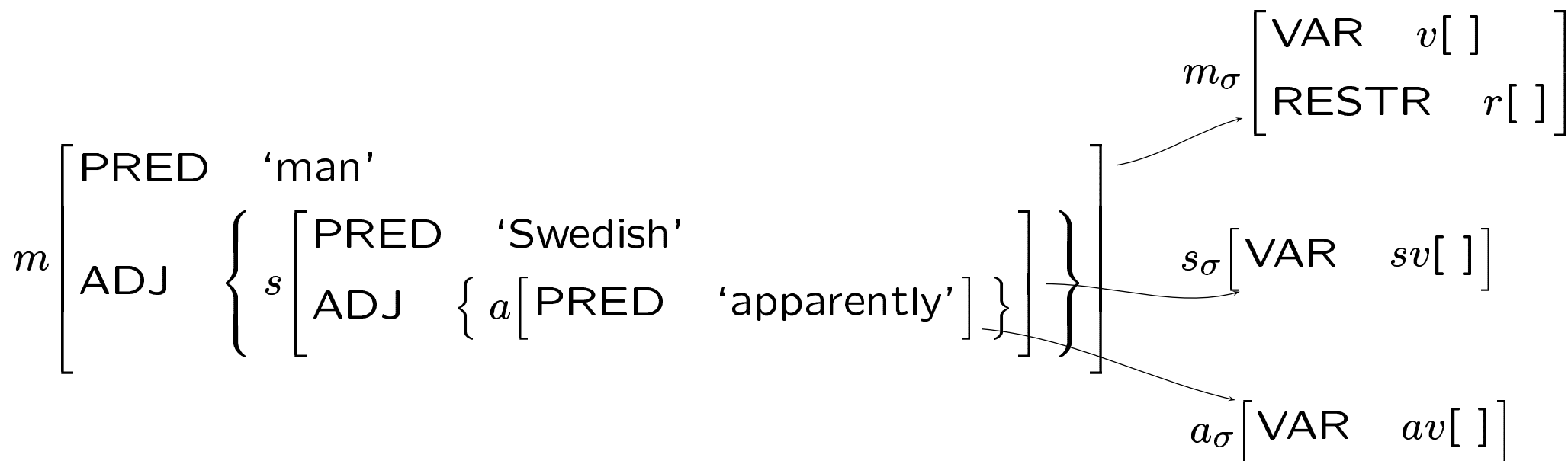
**Swedish1**             $\lambda X. Swedish(X) : [sv \multimap s\sigma]$

**Swedish2**    $\lambda Q. \lambda P. \lambda X. Q(X) \wedge P(X) : [sv \multimap s\sigma] \multimap [[v \multimap r] \multimap [v \multimap r]]$

**Swedish1, Swedish2**  $\vdash$

$\lambda P. \lambda X. Swedish(X) \wedge P(X) : [v \multimap r] \multimap [v \multimap r]$

*[[apparently Swedish] man]*



$\lambda X. \text{apparently}(\text{Swedish}(X)) \wedge \text{man}(X) : v \multimap r$

## Combining **apparently** with **Swedish1**

**apparently**  $\lambda R.\lambda X.apparently(R(X)) : [sv \multimap s\sigma] \multimap [sv \multimap s\sigma]$

**Swedish1**  $\lambda X.Swedish(X) : [sv \multimap s\sigma]$

**apparently, Swedish1**  $\vdash$

$\lambda X.apparently(Swedish(X)) : [sv \multimap s\sigma]$

## Combining **app-Sw**, **Swedish2**, and **man**

**app-Sw**      $\lambda X. \text{apparently}(\text{Swedish}(X)) : [sv \multimap s\sigma]$

**Swedish2**      $\lambda Q. \lambda P. \lambda X. Q(X) \wedge P(X) :$   
                   $[sv \multimap s\sigma] \multimap [[v \multimap r] \multimap [v \multimap r]]$

**man**                      $\lambda X. \text{man}(X) : v \multimap r$

**app-Sw, Swedish2, man**  $\vdash$

$\lambda X. \text{apparently}(\text{Swedish}(X)) \wedge \text{man}(X) : v \multimap r$

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