

- (p) (1 pt.) Coulomb's friction law is **exact/highly accurate/approximate/wrong**.
- (q) (1 pt.) The range for μ_s , the coefficient of static friction, is $0 \leq \mu_s \leq 1$. **True/False**.
- (r) (1 pt.) Electromagnetic repulsion of two protons is **much weaker/weaker/stronger/-much stronger** than their gravitational attraction.
- (s) (2 pts.) The first measurement of the "universal gravitational constant" G in 1798 by Cavendish and recent (year 2000+) experiments of G are estimated to be accurate to approximately:

| | | | | | |
|----------------------|-----|----|--------|-------------|----------|
| Experiments in 1798 | 10% | 1% | 0.001% | $10^{-7}\%$ | infinite |
| Experiments in 2000+ | 10% | 1% | 0.001% | $10^{-7}\%$ | Infinite |

- (t) (2 pts.) What **two** questions does statics answer?
- -
- (u) (3 pts.) What are the **two** steps in a free-body diagram?
- -
- (v) (2 pts.) What are the **two** vector equations used for **static equilibrium** of a system S ?
- -
- (w) (8 pts.) **Replacement of contact forces on a baseball bat.**

The figure to the right shows a forearm and hand modeled as a single rigid body A that uses a complex set of muscles, bones, ligaments, and tendons to grip a baseball bat B in such a way that a point Q of B cannot translate relative to a point P of A and B is only free to rotate relative to A about B 's long axis.

Note: Point Q is on the butt-end of the bat and is on B 's symmetry axis.

Note: Point P is the point of A coincident with Q .

- Draw and label contact and distance forces on B (think three-dimensional)
- **Fully describe** your **contact** force and/or torque measures on B .
- To facilitate your analysis, introduce helpful unit vectors.



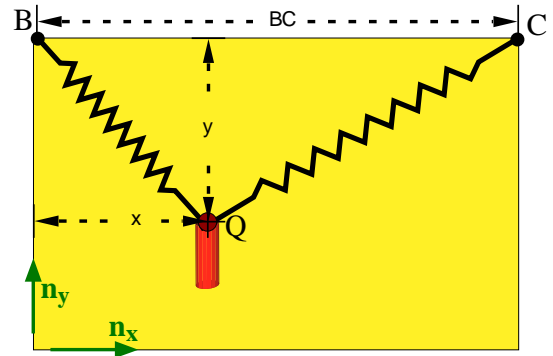
| Complete description of force/torque measures (think 3D) | Scalar symbol |
|--|---------------|
| | |

2. (19 pts.) **Design and statics of hanging a picture.**

A heavy picture Q is attached to pegs B and C by two light flexible cables. Ed, the construction contractor, has cut two cables and wants to know where the picture will be with these two cables.

In addition to a horizontally right unit vector \mathbf{n}_x and a vertically upward unit vector \mathbf{n}_y , the following table of systems facilitate this analysis.

| Description | Symbol |
|---|----------|
| Local gravitational constant | g |
| Mass of Q | m |
| Distance from B to C | BC |
| Natural length of cable \overline{BQ} | L_n^B |
| Natural length of cable \overline{CQ} | L_n^C |
| Material constant associated with springs | κ |
| \mathbf{n}_x measure of the position vector of Q from B | x |
| Vertical distance from B to Q | y |



- (a) (3 pts.) Find the distance between B and Q and the distance between C and Q .

Result:

$$d_B = \quad \quad \quad d_C =$$

- (b) (8 pts.) Express $\mathbf{F}^{Q/B}$ and $\mathbf{F}^{Q/C}$, (the contact forces on Q from the springs connecting Q to B and to C) and $\mathbf{F}^{Q/gravity}$ (the distance force on Q from gravity) in terms of symbols in the table, d_B , d_C , the spring constant k_B of the linear spring connecting Q to B , the spring constant k_C of the linear spring connecting Q to C , and \mathbf{n}_x and \mathbf{n}_y .

Result:

$$\vec{\mathbf{F}}^{Q/B} =$$

$$\vec{\mathbf{F}}^{Q/C} =$$

$$\vec{\mathbf{F}}^{Q/gravity} =$$

- (c) (5 pts.) Using free-body diagrams, form equations that govern **static equilibrium** of Q in N in terms of symbols in the table and κ .

Note: The spring constants k_B and k_C depend on the constant κ as $k_B = \frac{\kappa}{L_n^B}$ and $k_C = \frac{\kappa}{L_n^C}$.

Result:

$$= 0$$

$$= 0$$

- (d) (2 pts.) With known values of symbols in the table, the equations governing the **static equilibrium** values of x and y simplify to (you do not need to show this)

$$1.6 - 0.16667x + \frac{x}{\sqrt{x^2 + y^2}} - \frac{15 - x}{\sqrt{(15 - x)^2 + y^2}} = 0$$

$$981 - 55051y + 330304 \frac{y}{\sqrt{x^2 + y^2}} + 330304 \frac{y}{\sqrt{(15 - x)^2 + y^2}} = 0$$

With a pencil, paper, and a simple calculator, find numerical values for x and y that satisfy both equations. Alternately, describe how you would solve these equations.

- (e) (1 pt.) Sketch two or more configurations that may satisfy the previous set of equations.