

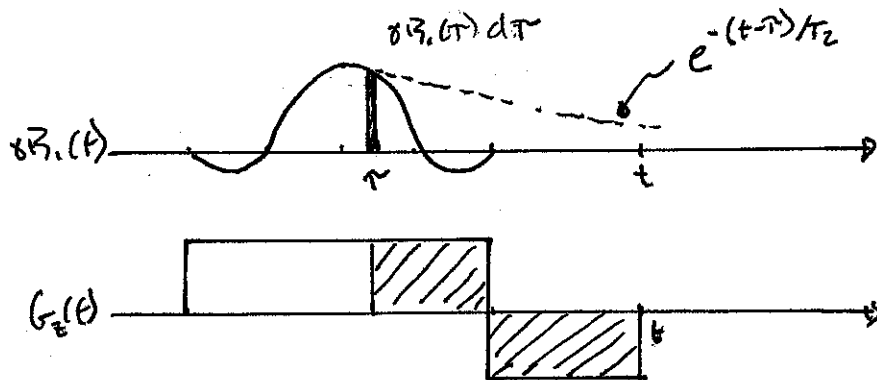
## **Ultra-short echo time (UTE) pulses, and short T2 contrast**

- Short T2 excitation pulses
- Short T2 imaging
- Generating short T2 contrast

# T<sub>2</sub> DECAY DURING EXCITATION

SMALL-TIP-ANGLE CASE

GRAPHICAL DERIVATION



SMALL INCREMENT IN  $M_{xy}$  IS EXCITED AT TIME  $\tau$

• DECAYS BY  $e^{-(t-\tau)/T_2}$

• PRECESSES BY  $K(\tau, t) z$  WHERE

$$K(\tau, t) = -\frac{\gamma}{2\pi} \int_{\tau}^t G_z(s) ds$$

PHASE FACTOR

$$e^{i2\pi K(\tau, t) z}$$

• INCREMENT IN  $M_{xy}$  IS

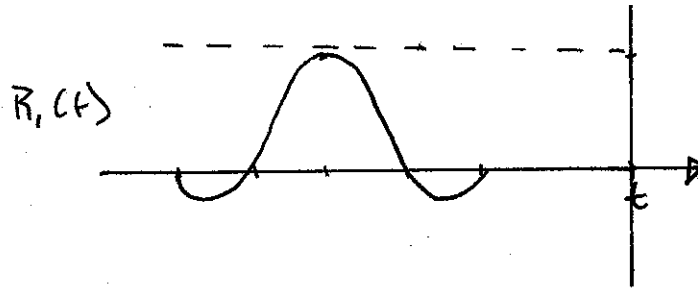
$$\Delta M_{xy} = (\delta B_z(\tau) \Delta \tau) (i m_0) e^{-(t-\tau)/T_2} e^{i2\pi K(\tau, t) z}$$

INTEGRATING

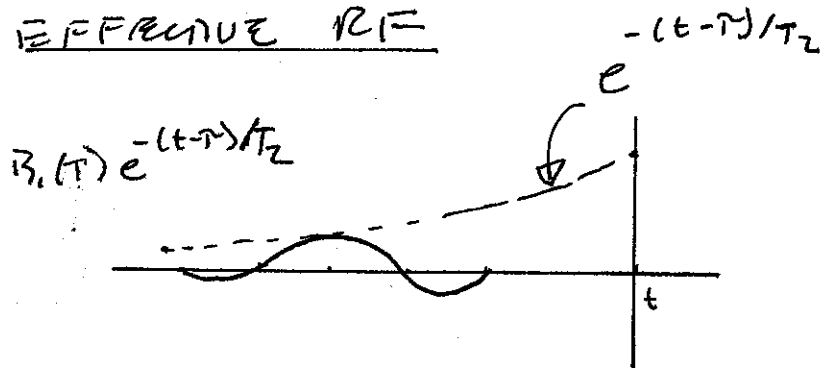
$$M_{xy}(z, t) = i m_0 \int_{-\infty}^t \delta B_z(\tau) e^{-(t-\tau)/T_2} e^{i2\pi K(\tau, t) z} d\tau$$

# FOURIER TRANSFORM OF EXPONENTIALLY WEIGHTED RF

## APPLIED RF



## EFFECTIVE RF



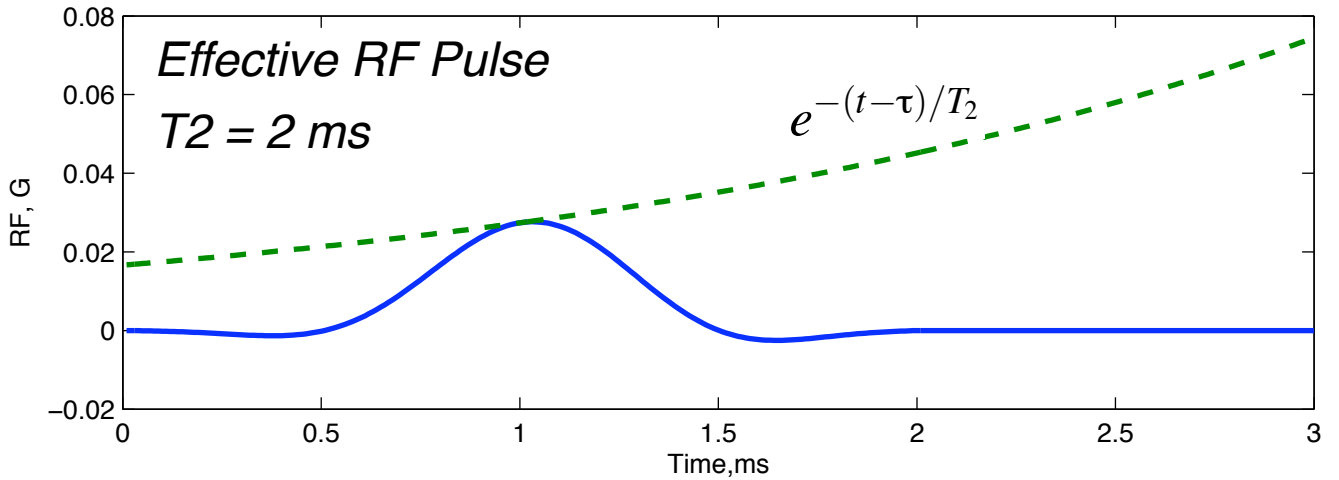
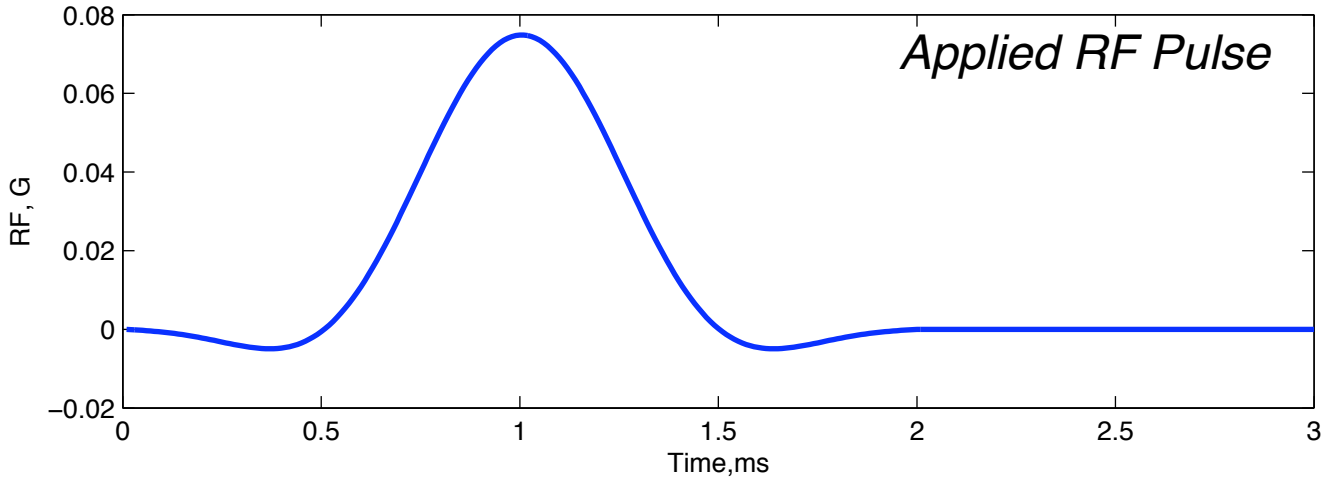
PRIMARY EFFECT:

LOSS OF SIGNAL

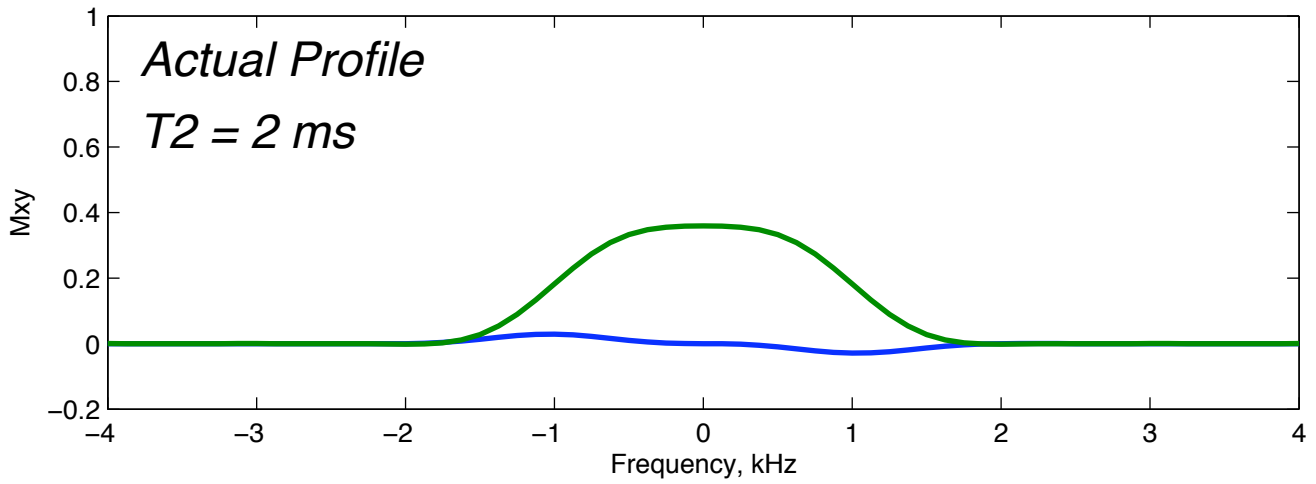
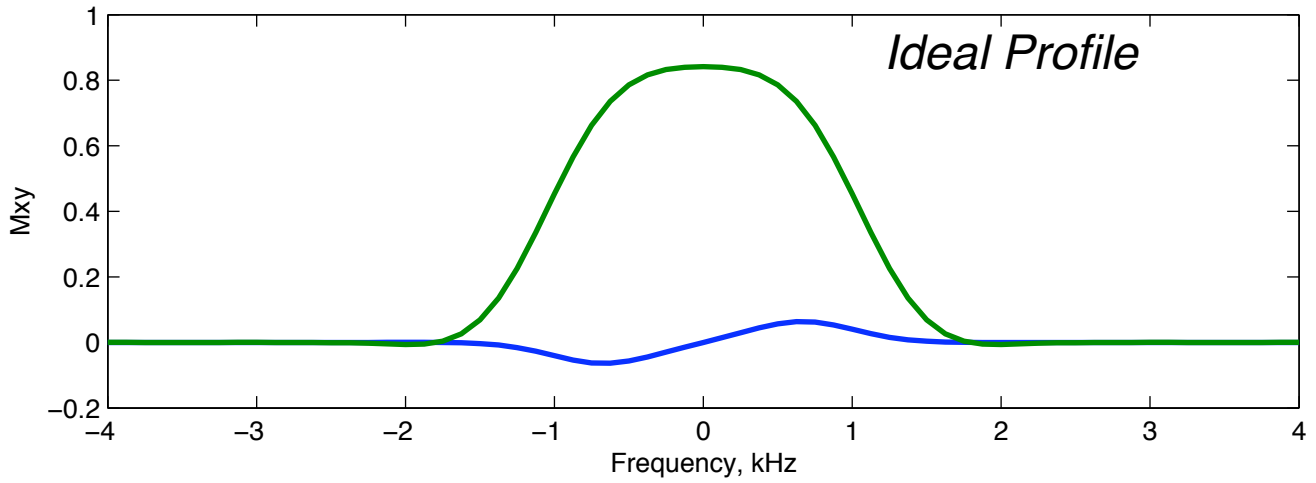
SECONDARY EFFECT:

LOSS OF SECURITY

# Effect of $T_2$ on Small-Tip-Angle Excitation

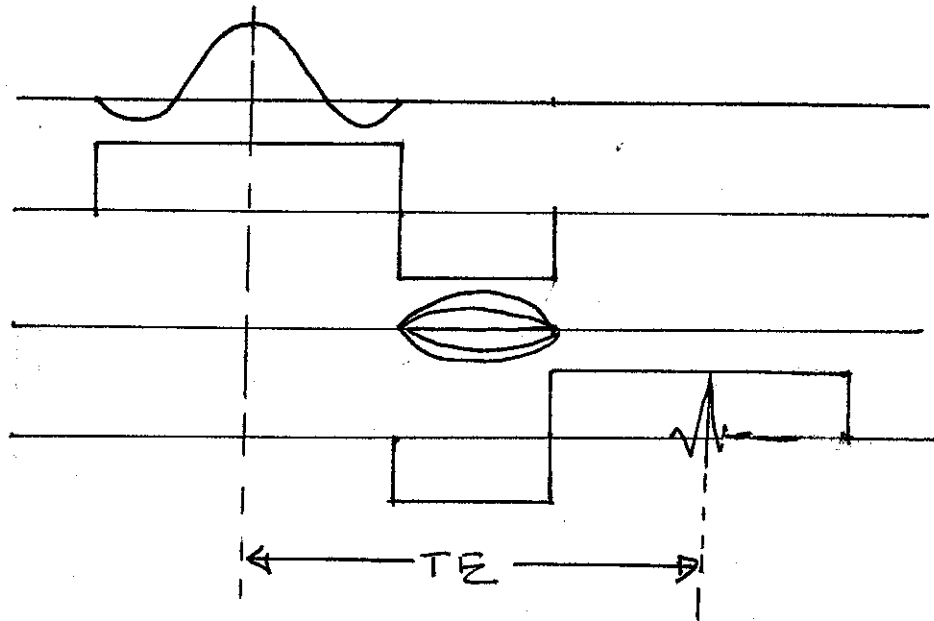


# *Effect of T2 on Small-Tip-Angle Excitation*



# ECHO TIME IN A GRADIENT REVERSED SEQUENCE

ECHO TIME IS DELAY FROM CENTER OF RF TO K-SPACE ORIGIN IN READOUT



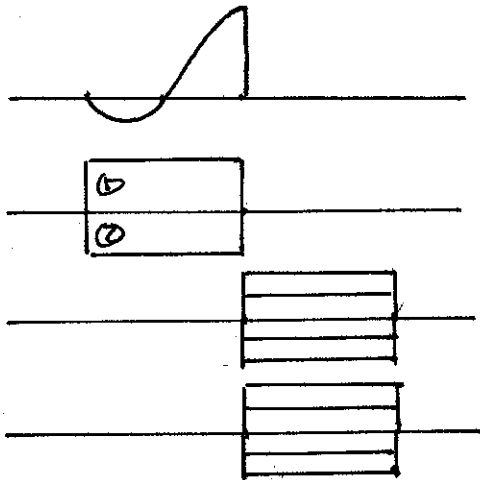
MINIMIZE  $T_2$  DECAY BY MINIMIZING  $TE$

ELIMINATE EVERYTHING BETWEEN DASHED LINES

- HALF-PULSE EXCITATION
- RADIAL READOUT

# SHORT T2 PULSE SEQUENCE

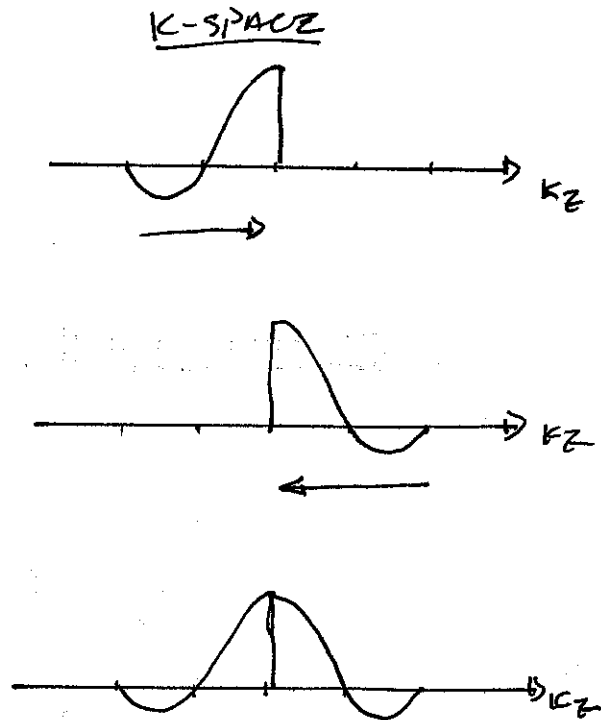
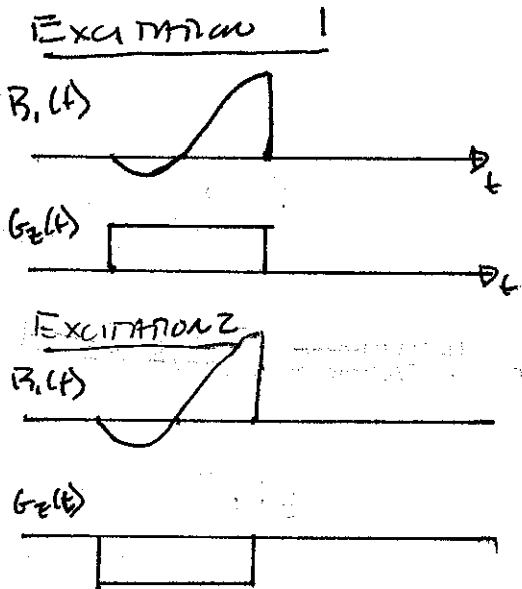
## IDEAL PULSE SEQUENCE



HALF-PULSE EXCITATION  
TWO ACQUISITIONS COMBINED  
Z-GRADIENT FLIP

RADIAL READOUT

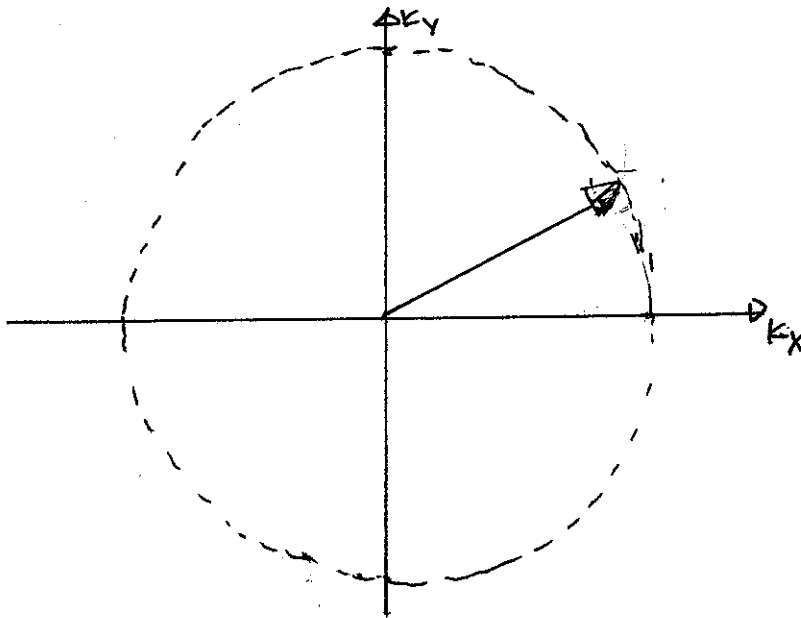
## HALF-PULSE EXCITATION



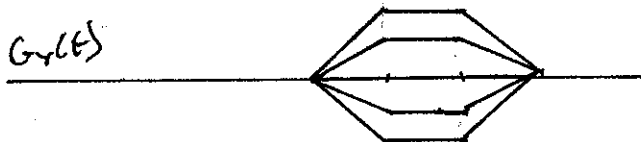
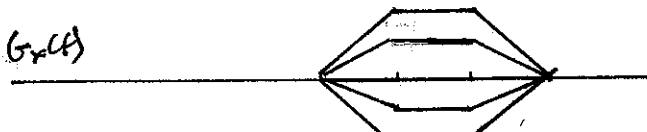
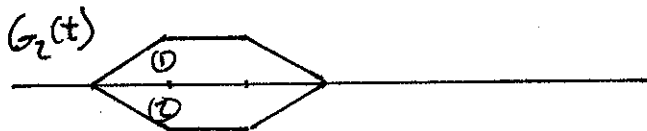
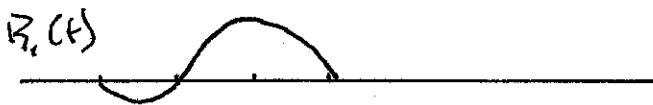
SUM OF TWO ACQUISITIONS  
SAME AS CONVENTIONAL  
SLICE SELECTIVE PULSE!

# RADIAL READOUT

START AT K-SPACE ORIGIN, GO DIRECTLY OUT



## PRACTICAL PULSE SEQUENCE





## LARGE FLIP ANGLE HALF PULSES

HALF PULSES ARE BASED ON A SMALL-TIP ANGLE (FOURIER) MODEL.

WORKS WELL TO  $45^\circ$ , OR EVEN  $60^\circ$

SIGNIFICANT DISTORTION AT  $90^\circ$

### SOLUTION

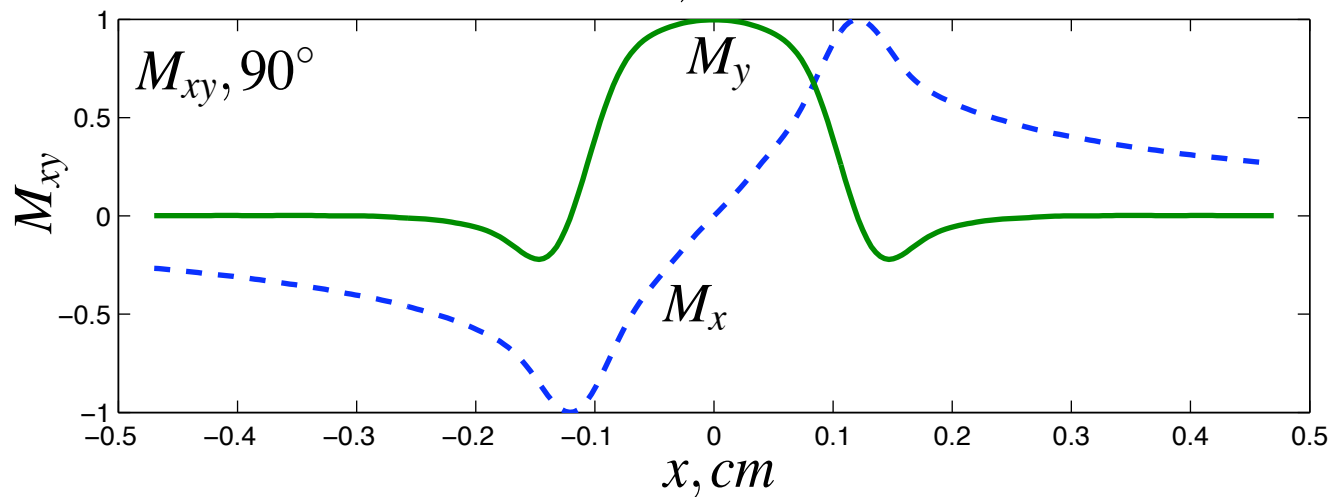
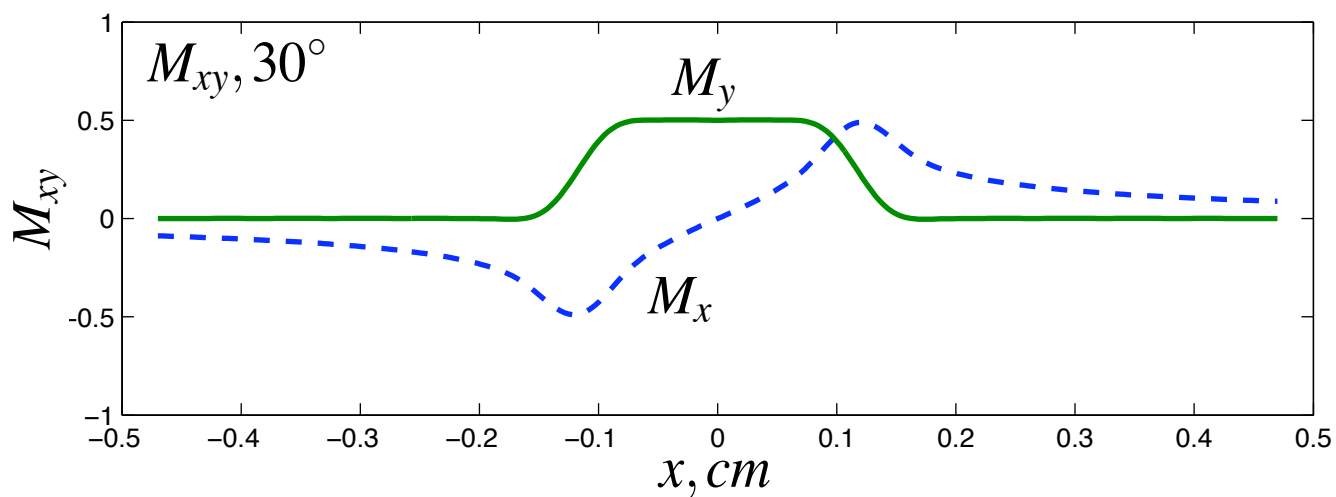
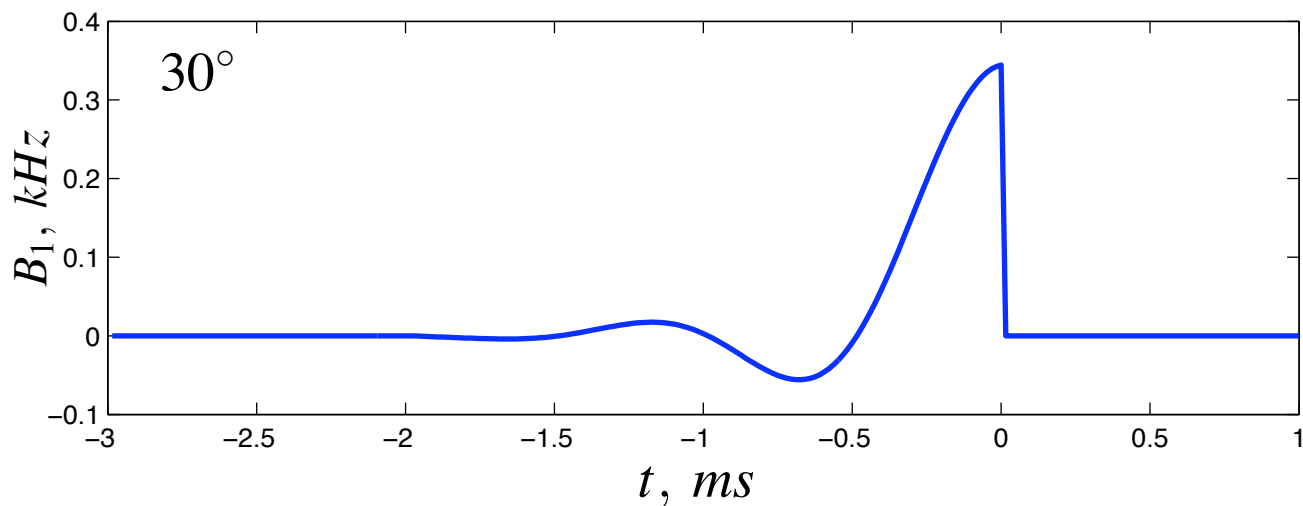
TO DESIGN A HALF PULSE FOR A FLIP ANGLE  $\theta$

1) DESIGN AN SLR PULSE FOR ANGLE  $2\theta$

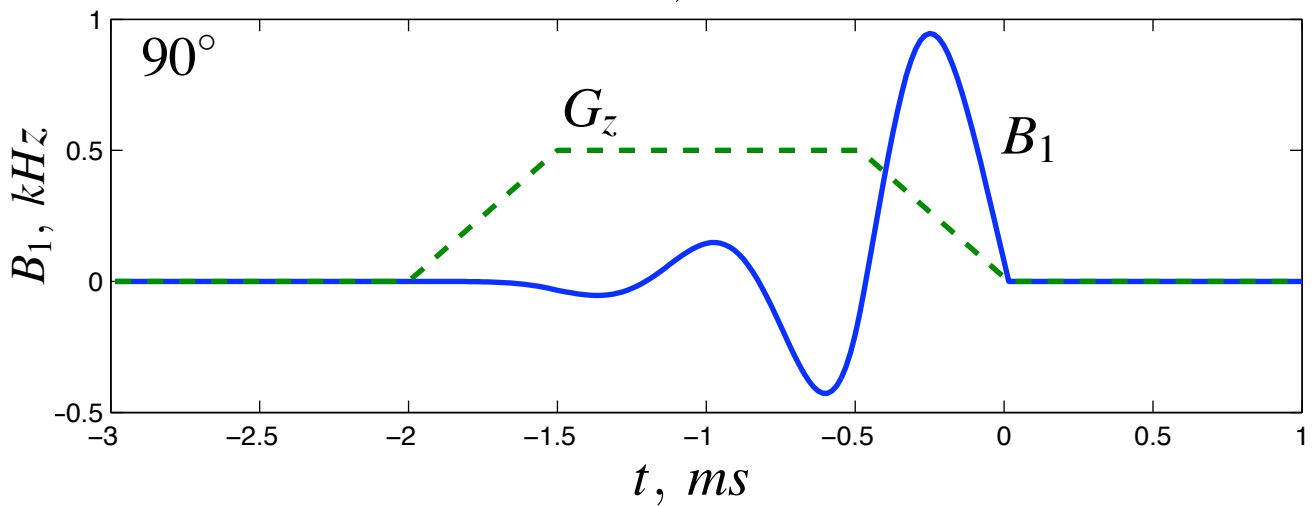
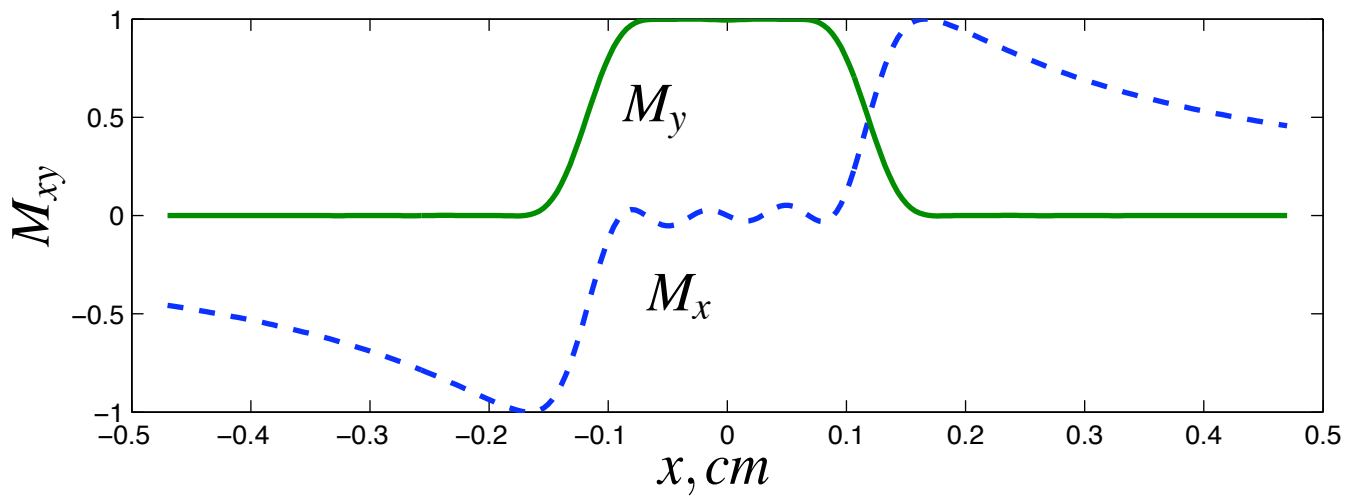
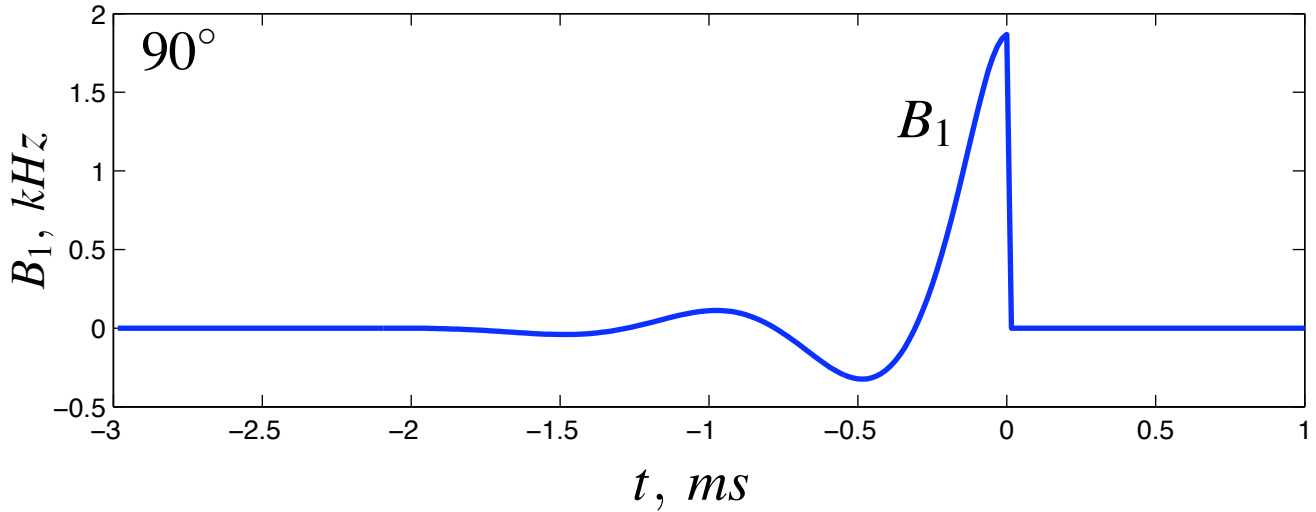
2) TAKE THE FIRST HALF.

FOR A  $90^\circ$  HALF PULSE, USE THE FIRST HALF OF AN SLR  $180^\circ$ !

# Large-Tip-Angle Half Pulses, Fourier Design



# Large-Tip-Angle Half Pulses SLR Design



# ISSUES WITH HALF PULSES

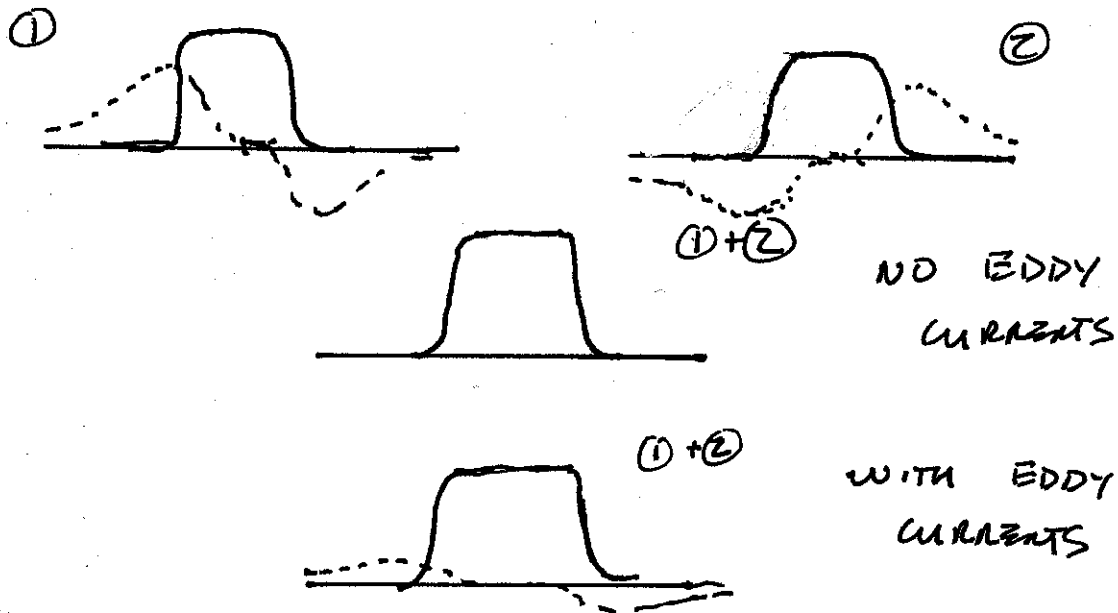
## 1) GRADIENT FIDELITY + EDDY CURRENT EFFECTS

WE ARE COUNTING ON

- SLICE PROFILE ADDING

- ANTI-SYMMETRIC TAILS CANCELING

BETWEEN TWO EXCITATIONS



SMALL PHASE ERRORS LEAVE RESIDUAL TAILS

THIS CAN BE A LARGE SIGNAL OVER A VOLUME

## 2) STEADY STATE EFFECTS

CENTER OF SLICE SEES

$$\theta_x, \theta_x, \theta_x$$

TAIL SEES

$$\phi_y, -\phi_y, \phi_y, -\phi_y$$

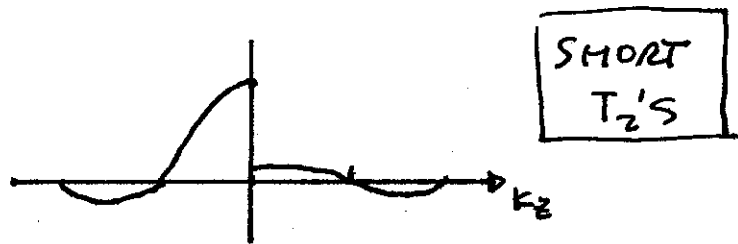
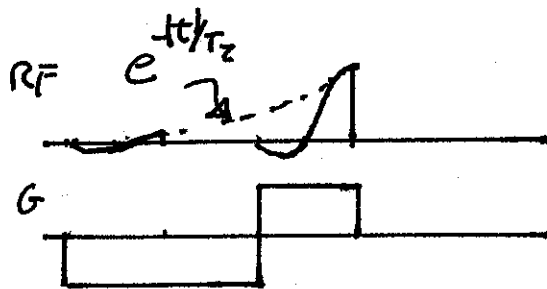
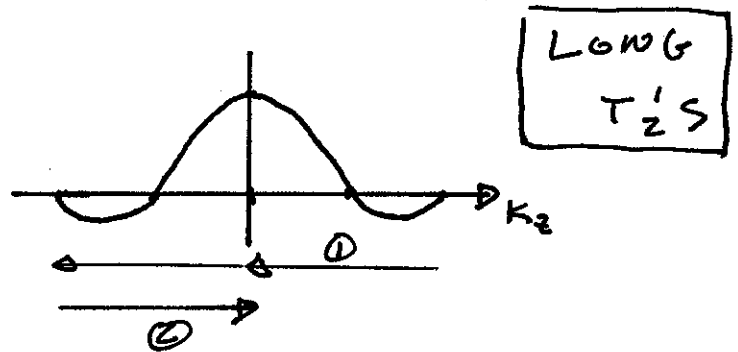
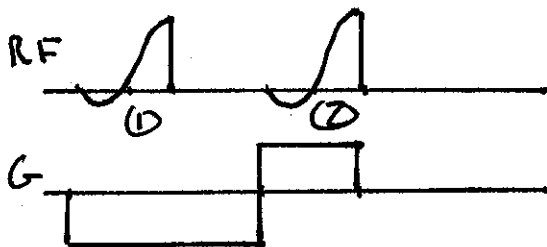
STEADY STATES CAN BE VERY DIFFERENT

# DOUBLE HALF PULSES

DESIGN PULSES THAT ARE

- SLICE SELECTIVE FOR LONG  $T_2$ 'S (NO ASYMMETRIC TAILS)
- HALF PULSES FOR SHORT  $T_2$ 'S

## EXAMPLE



## ADVANTAGES

NO OUT-OF-SLICE TAILS FOR LONG  $T_2$ 'S

NO CANCELLATION PROBLEMS, STEADY STATE EFFECTS

IMMUNE TO EDDY CURRENT EFFECTS

EASIER TO CALIBRATE

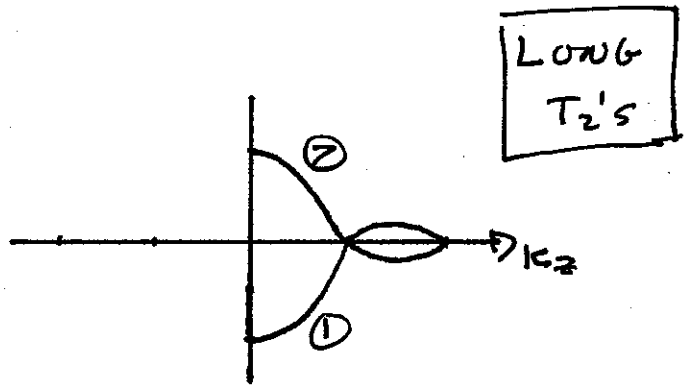
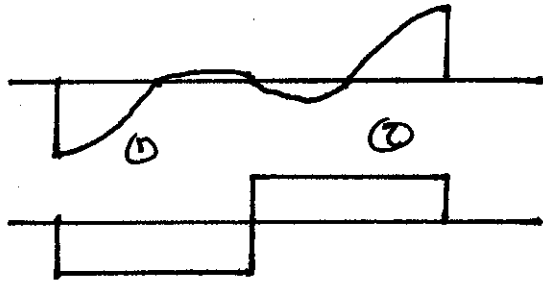
NO EFFECTS DURING READOUT

## ISSUES

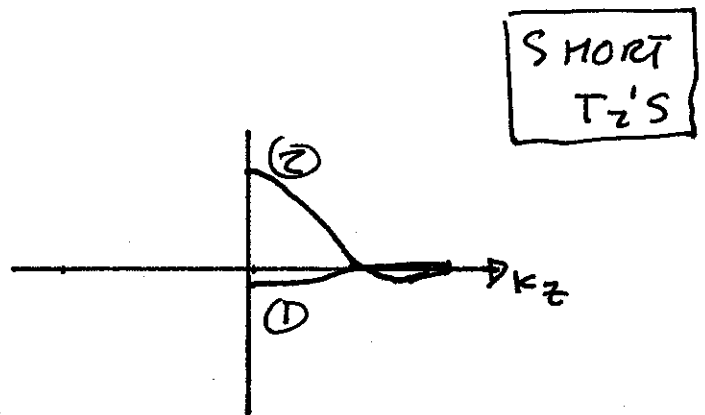
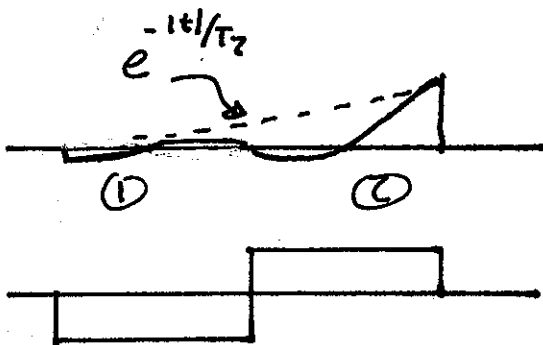
SPECTRAL RESPONSE

LOSS OF SHORT  $T_2$  SIGNAL

ANOTHER OPTION



LONG T<sub>2</sub>'S CANCEL.



SHORT T<sub>2</sub>'S SEE A HALF PULSE

## PROBLEM WITH SHORT-T<sub>2</sub> PULSE SEQUENCE

EVERYTHING SHOWS UP

IMAGES SHOW PROTON DENSITY ONLY

HARD TO TELL WHAT HAS SHORT T<sub>2</sub>'S

NEED SHORT-T<sub>2</sub> CONTRAST

### SHORT-T<sub>2</sub> CONTRAST OPTIONS

1) COLLECT SECOND IMAGE WITH TE<sub>2</sub>, COMPUTE DIFFERENCE IMAGE.

$$I_{ST2} = I_{TE1} - I_{TE2}$$

SHOULD SHOW ONLY SHORT-T<sub>2</sub> COMPONENTS.

#### PROBLEMS:

- SECOND IMAGE ONLY ADDS NOISE TO SHORT-T<sub>2</sub> VOXELS
- INHOMOGENEITY IN A VOXEL LOOKS LIKE SHORT-T<sub>2</sub>

### 2) EXPLOIT T<sub>1</sub> DIFFERENCES

TISSUES WITH SHORT T<sub>2</sub>'S TEND TO HAVE SHORT T<sub>1</sub>'S (NOT LIKE SOLIDS)

RF SPOILED SHORT TR SEQUENCES WILL SHOW SHORT T<sub>1</sub>'S, EMPHASIZE SHORT T<sub>2</sub>'S

## PROBLEMS:

- STILL NOT  $T_2$  SELECTIVE UNLESS COMBINED WITH (1).

### 3) EXPLOIT EXCITATION DIFFERENCES

$T_2$  EFFECTS OUR ABILITY TO EXCITE OR INVERT MAGNETIZATION

USE PREPULSES TO ESTABLISH SHORT- $T_2$  CONTRAST.

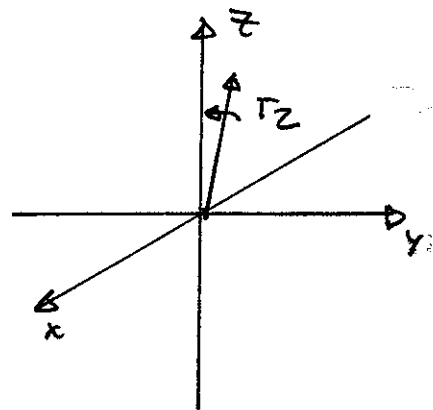
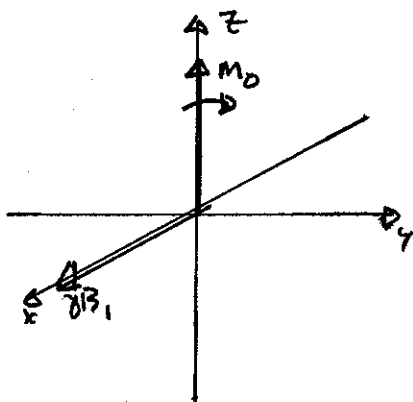
DESIGN  $T_2$  SELECTIVE EXCITATIONS



# LONG $T_2$ SUPPRESSION PULSES

BASIC IDEA: EXCITATION AND RELAXATION  
ARE COMPETING PROCESSES

EXCITATION CREATES MAGNETIZATION ( $m_{xy}$ ) - AND -  
RELAXATION DESTROYS MAGNETIZATION



BOTH ARE EFFECTUVELY ROTATION RATES FOR  
SMALL-TIP-ANGLE CASE

IF  $\delta B_1 \gg T_2$

MAGNETIZATION IS ROTATED AWAY FROM  $z$

IF  $\delta B_1 \ll T_2$

NO TRANSVERSE MAGNETIZATION IS CREATED

$m$  STAYS UNTOUCHED ALONG  $z$

# LONG $T_2$ SUPPRESSION PULSES

LONG, LOW AMPLITUDE  $90^\circ$  PULSES

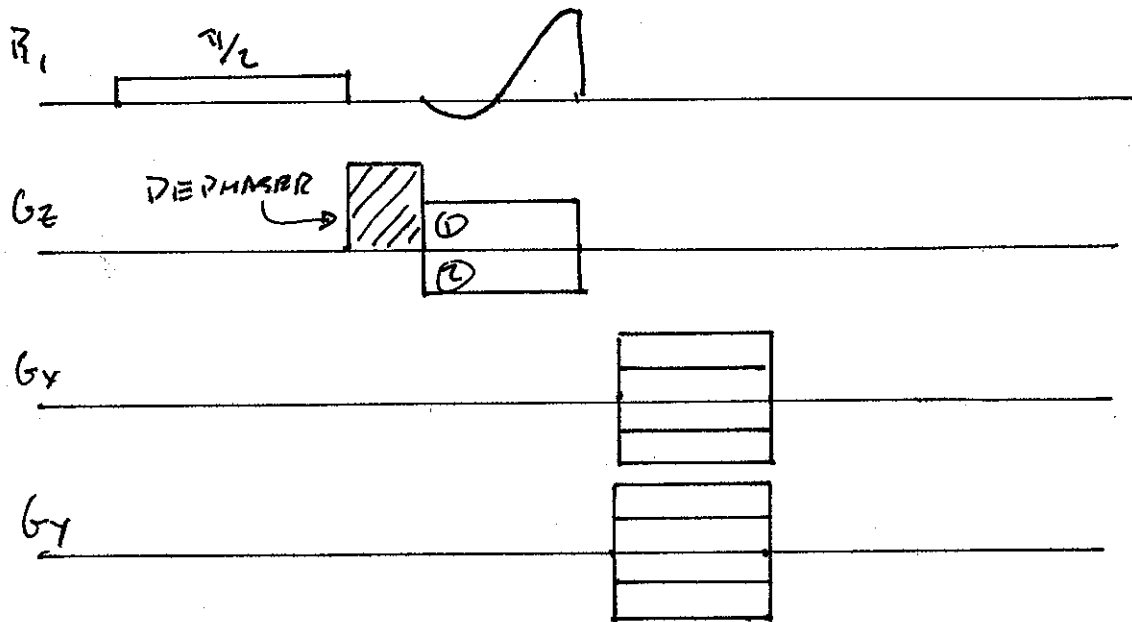
IF  $T$  IS PULSE LENGTH

$T_2$ 's  $\ll T$  ARE UNEXCITED

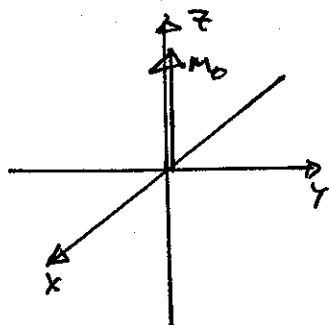
$T_2$ 's  $\gg T$  ARE COMPLETELY EXCITED

EXCITED MAGNETIZATION IS DEPHASED

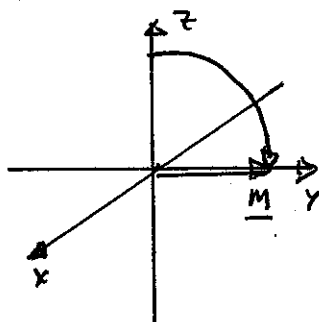
REMAINING MAGNETIZATION IS ENAGED WITH  
SHORT  $-T_2$  PULSE SEQUENCE



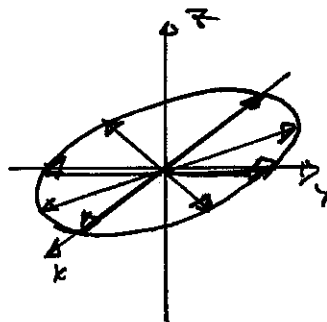
## LONG- $T_2$ SPECIES



EQUILIBRIUM

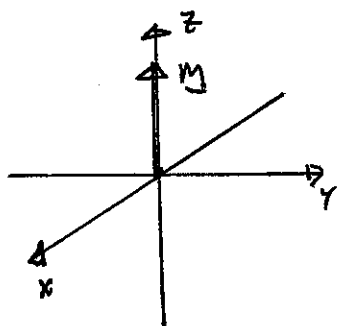


EXCITATION

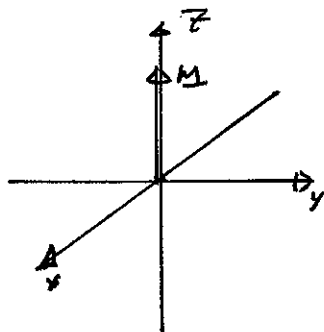


DEPHASING

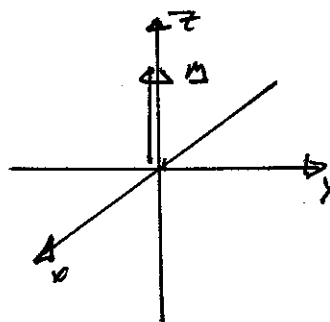
## SHORT- $T_2$ SPECIES



EQUILIBRIUM



EXCITATION



DEPHASING

LONG- $T_2$  SPECIES ARE EXCITED AND DEPHASED

SHORT- $T_2$  SPECIES ARE NOT EXCITED AT ALL.

## LONG- $T_2$ SUPPRESSION RESPONSE

### RECTANGULAR $\pi/2$ PULSE

$$\begin{pmatrix} \dot{m}_x \\ \dot{m}_y \\ \dot{m}_z \end{pmatrix} = \begin{pmatrix} -1/T_2 & 0 & 0 \\ 0 & -1/T_2 & \delta B_1 \\ 0 & -\delta B_1 & 0 \end{pmatrix} \begin{pmatrix} m_x \\ m_y \\ m_z \end{pmatrix}$$

LAST TWO EQUATIONS DECOUPLE

$$\begin{pmatrix} \dot{m}_y \\ \dot{m}_z \end{pmatrix} = \begin{pmatrix} -1/T_2 & \delta B_1 \\ -\delta B_1 & 0 \end{pmatrix} \begin{pmatrix} m_y \\ m_z \end{pmatrix}$$

WRITE AS A SINGLE EQUATION IN  $m_z$

$$\ddot{m}_z + \frac{1}{T_2} \dot{m}_z + (\delta B_1)^2 m_z = 0$$

LINEAR CONSTANT COEFFICIENT ODE. ROOTS ARE

$$\lambda_{1,2} = -\frac{1}{2T_2} \pm \sqrt{\left(\frac{1}{2T_2}\right)^2 - (\delta B_1)^2}$$

SOLUTION FOR  $m_z$  IS

$$m_z(t) = \frac{1}{\lambda_1 - \lambda_2} \left[ (\lambda_1 + \frac{1}{T_2}) e^{\lambda_1 t} - (\lambda_2 + \frac{1}{T_2}) e^{\lambda_2 t} \right]$$

FOR A  $\pi/2$  PULSE, IF THE PULSE LENGTH IS  $T$ ,

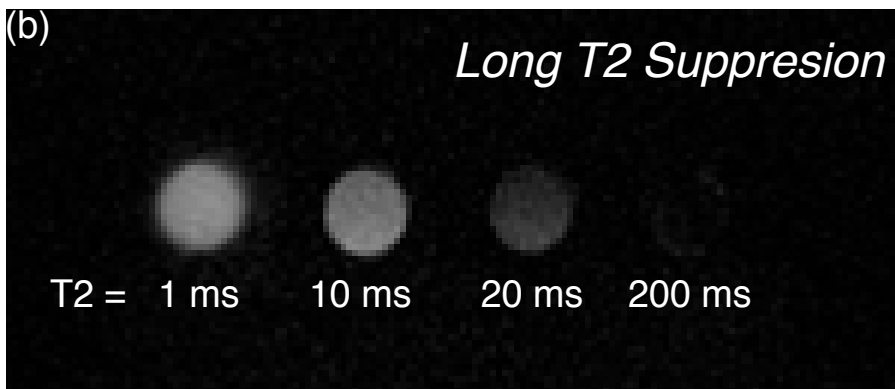
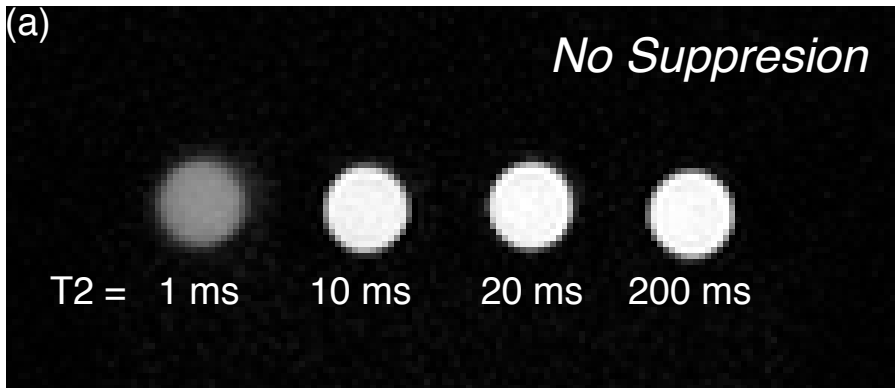
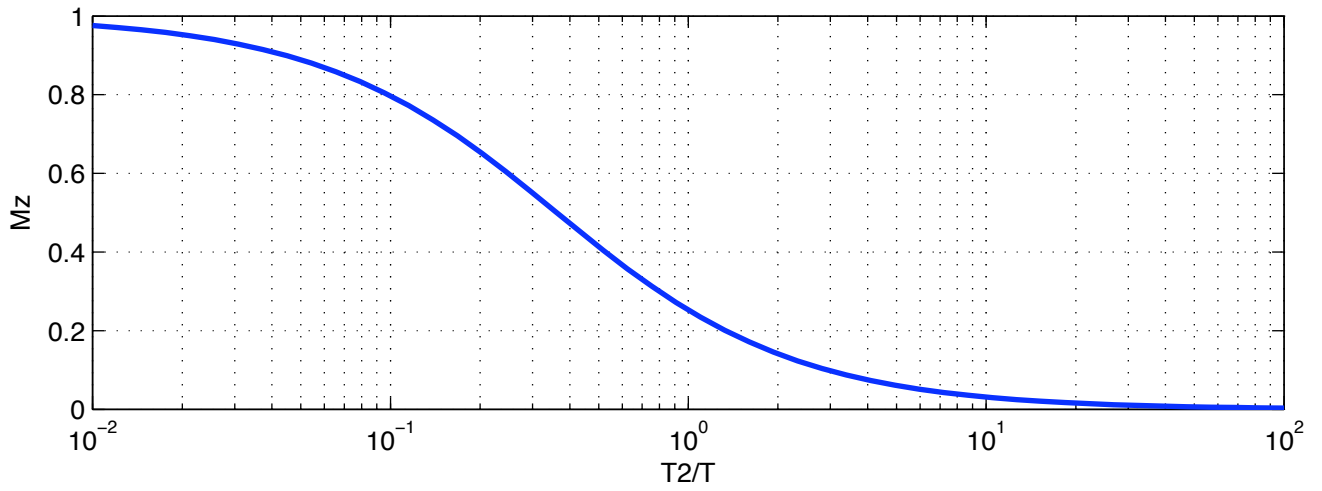
$$\delta\beta_1 = \frac{\pi/2}{T} = \frac{\pi}{2T}$$

SUBSTITUTING FOR  $t=T$ , AND  $\delta\beta_1$ , AND SIMPLIFYING CONSIDERABLY

$$M_z(T) = e^{-\frac{\pi}{2} \left( \frac{T}{\pi T_2} \right)} \left\{ \frac{\left( \frac{T}{\pi T_2} \right)}{\sqrt{\left( \frac{T}{\pi T_2} \right)^2 - 1}} \sinh \left( \frac{\pi}{2} \sqrt{\left( \frac{T}{\pi T_2} \right)^2 - 1} \right) + \cosh \left( \frac{\pi}{2} \sqrt{\left( \frac{T}{\pi T_2} \right)^2 - 1} \right) \right\}$$

THIS IS A FUNCTION OF  $T_2/T$ .

# Long-T2 Suppression



FOR A GIVEN PULSE LENGTH  $T$

- $T_2$ 'S  $< T$  ARE PRESERVED
- $T_2$ 'S  $> T$  ARE SUPPRESSED

IF WE WANT TO PRESERVE  $T_2$ 'S OF  $2\text{ms}$   
WITH 80% EFFICIENCY, WE NEED A  $10 \times 2\text{ms} = 20\text{ms}$   
PULSE!

PROBLEM: A  $20\text{ms}$  RECTANGULAR PULSE  
HAS A BANDWIDTH OF

$$\frac{1}{20\text{ms}} = \underline{50\text{ Hz}}$$

THIS IS MUCH LESS THAN  $B_0$  INHOMOGENEITY  
EXPERIENCED OVER MUCH OF BODY ( $\approx 1.5\text{T}$ )

CAN I USE ANOTHER WAVEFORM TO BROADEN  
THE BANDWIDTH?

UNDER REASONABLE ASSUMPTIONS, WE CAN SHOW:

$$m_z(t) \approx m_0 \left( 1 - T_z \int_{-\infty}^{\infty} (\delta B_r(f))^2 df \right)$$

THIS MEANS THAT THE DECREASE IN  $m_z$  IS DUE ONLY TO

- 1)  $T_z$
- 2) RF POWER

$T_z$  IS FIXED, SO OUR ONLY VARIABLE IS RF POWER.

### RESULT:

WIDER BANDWIDTH SUPPRESSION PULSES WILL ALSO SUPPRESS SHORT  $T_z$ 'S MORE, DUE TO PARSEVAL'S THEOREM.

IF

$$w_r(t) = \delta B_r(t)$$

$$W_r(f) = \mathcal{F}\{w_r(t)\}$$

THEN

$$\int_{-\infty}^{\infty} |w_r(t)|^2 dt = \int_{-\infty}^{\infty} |W_r(f)|^2 df$$

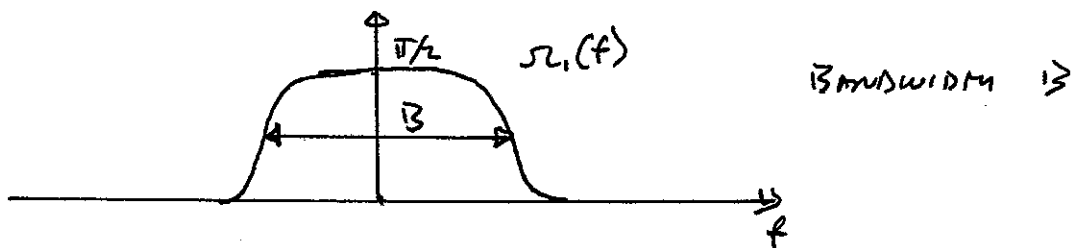


IN ORDER TO MINIMIZE SUPPRESSION OF  
SHORT  $T_2$ 'S, WHICH IS

$$M_z = 1 - T_2 \underbrace{\int_0^T |\omega_1(t)|^2 dt}_{\text{MINIMIZE THIS}}$$

$$= 1 - T_2 \int_{-\infty}^{\infty} |\Omega_1(f)|^2 df$$

FOR LONG- $T_2$ 'S THE EXCITATION PROFILE IS  $\tilde{F}(\delta B, (A)) = \Omega_1(f)$   
AND THIS SHOULD BE  $\pi/2$  IN THE SUPPRESSION BAND



THE SUPPRESSION IS THEN

$$M_z \approx 1 - T_2 \left(\frac{\pi}{2}\right)^2 B$$

NEED TO MINIMIZE B.

# Approximate vs Exact Solution Rectangular Suppression Pulse

