

CRYO ELECTRON MICROSCOPY TOMOGRAPHY

ELECTRON MICROSCOPY

LONG USED FOR HIGH RESOLUTION IMAGING
ELECTRONS HAVE SHORT WAVELENGTHS ($\sim 0.01 \text{ nm}$)
VERY LITTLE CONTRAST WITH BIOLOGICAL OBJECTS
HISTORICALLY, COAT WITH METAL
DIFFICULT TO SEE INTERNAL STRUCTURES OF CELLS

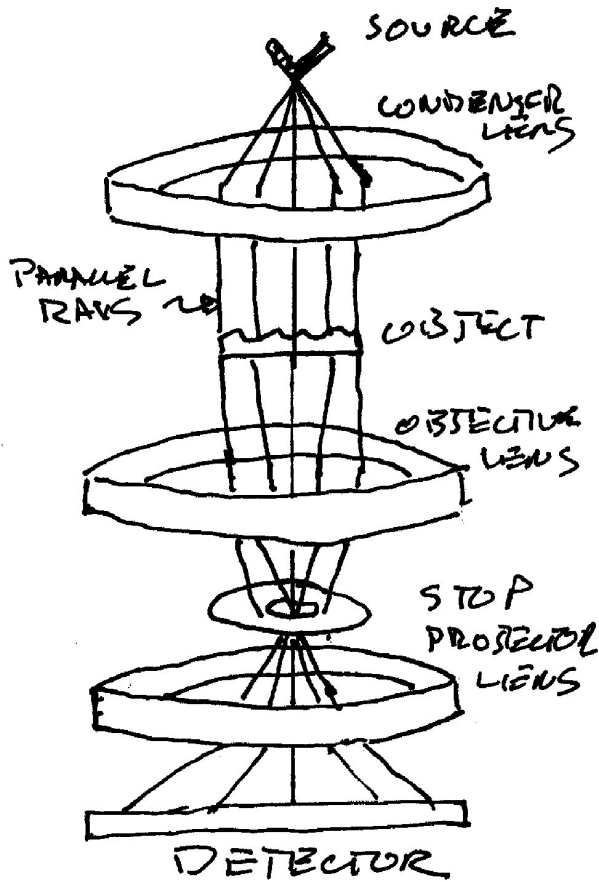
CRYO-EM

FLASH FREEZE THIN FILM OF CELLS IN WATER
NORMAL HYDRATION STATE
WATER FORMS A GLASS, DOESN'T FORM CRYSTALS
WHICH DESTROYS THE CELL
REDUCES DAMAGE FROM ELECTRON BEAM
STILL VERY LITTLE CONTRAST!

CRYO-EM TOMOGRAPHY

ACQUIRE A SERIES OF CRYO-EM IMAGES
AT A RANGE OF TILT ANGLES
RECONSTRUCT 3D WITH FILTERED BACKPROJECTOR
SEVERAL PRACTICAL ISSUES

ELECTRON MICROSCOPE (TRANSMISSION)

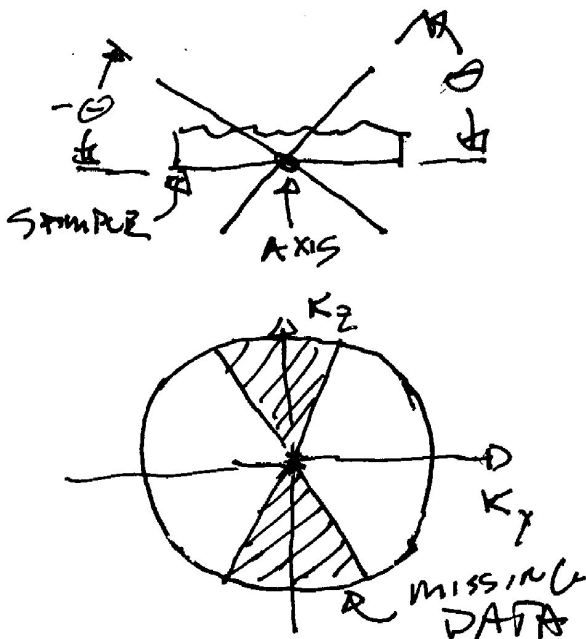


SOURCE $\sim 25 \mu\text{m}$ TIP
 100-300 kV ACCELERATION
 LENS ARE ELECTROMAGNETS
 OBJECT BOTH ATTENUATES
 AND DEFLECTS BEAMS
 BOTH AMPLITUDE AND PHASE

STOP SUPPRESSES WIDELY
 SCATTERED ELECTRONS, REDUCE
 BACKGROUND
 PROJECTOR MAGNIFIES IMAGE

DETECTOR, DIGITAL PHOTON
 COUNTING (WAS CCD, FILM)

TOMOGRAPHY



FOR TOMOGRAPHY TILT THE
 STAGE

ANGLES FROM $\pm 60^\circ$ OR SO
 MISSING 30° ON EACH END
 "MISSING WEDGE"

IN K-SPACE, MISSING
 SPATIAL FREQUENCY DATA

SAMPLE CONTRAST

INCIDENT
WAVEFRONTS



$$\psi_0$$

SAMPLE



$$\psi_s(\underline{r}) = \psi_0 e$$

ATTENUATION PHASE
 $(\sigma(\underline{r}) + i\phi(\underline{r}))$

CONVENTIONALLY IN TRANSMISSION EM, SAMPLE IS COATED IN METAL TO MAKE $\sigma(\underline{r})$ LARGE (AND NEGATIVE)

IN BIOLOGICAL SAMPLES, $\sigma(\underline{r}) = 0$ AND $\phi(\underline{r})$ IS SMALL

SMALL ANGLE APPROXIMATION

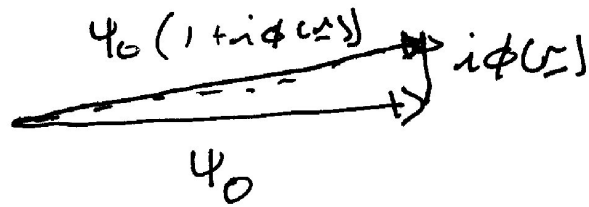
$$\begin{aligned} \psi_s(\underline{r}) &= \psi_0 e^{i\phi(\underline{r})} \\ &\approx \psi_0 (1 + i\phi(\underline{r})) \end{aligned}$$

THE DETECTED INTENSITY IS

$$\begin{aligned} \psi_s(\underline{r}) \psi_s^*(\underline{r}) &= \psi_0^2 (1 + i\phi(\underline{r})) (1 - i\phi(\underline{r})) \\ &= \psi_0^2 (1 + \phi^2(\underline{r})) \end{aligned}$$

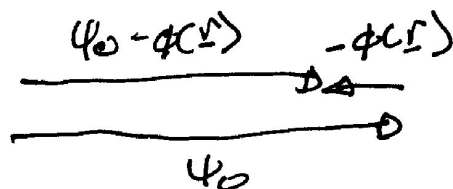
IF $\phi(\underline{r})$ IS SMALL, $\phi^2(\underline{r})$ IS VERY SMALL
VERY LITTLE CONTRAST!

GRAPHICALLY



THE MAGNITUDE IS INSENSITIVE TO SMALL PHASE SHIFTS

WE WANT TO ADD $\pi/2$ PHASE SHIFT, SO THAT



THEN

$$\begin{aligned}\psi_0 \cos \psi_0^* &= \psi_0^2 (1 - \phi(\omega))(1 - \phi(\omega)) \\ &\approx \psi_0^2 (1 - 2\phi(\omega))\end{aligned}$$

MUCH LARGER CONTRAST.

HOW DO WE INTRODUCE THIS PHASE SHIFT?

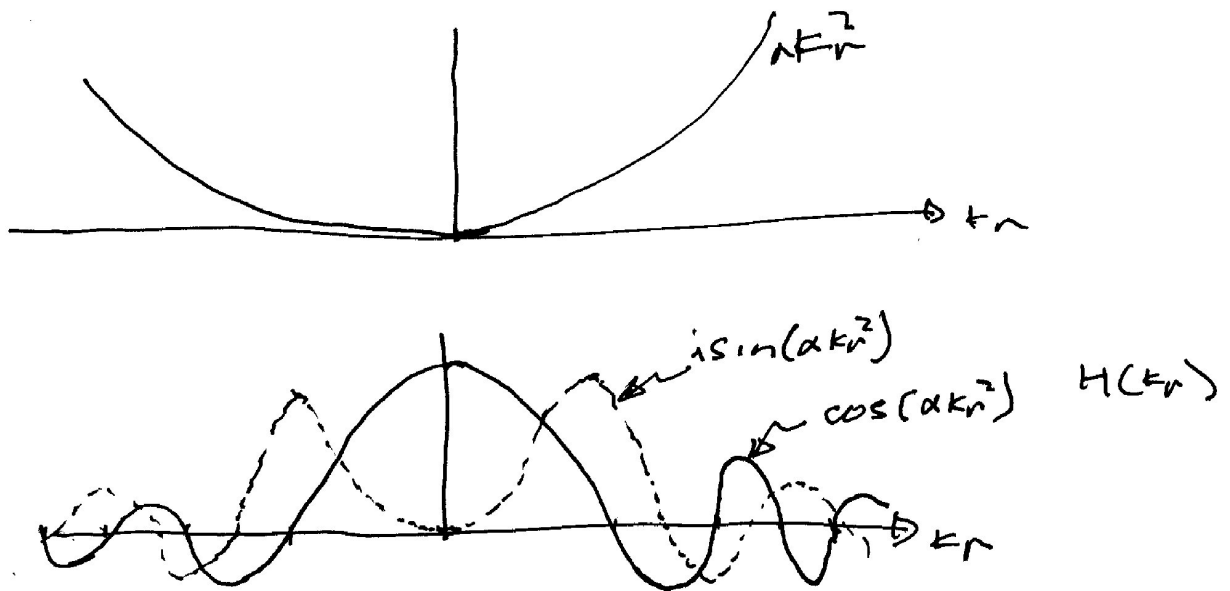
RECALL THAT BEING OUT OF FOCUS IN AN OPTICAL SYSTEM IS A SPHERICAL ABERRATION (MRI AUTOFOCUS LECTURE)

$$H(k_r) = e^{i\alpha k_r^2}$$

WHERE k_r IS THE RADIAL SPATIAL FREQUENCY

$$H(k_r) = \cos(\alpha k_r^2) + i \sin(\alpha k_r^2)$$

THIS LOOKS LIKE



TWO TERMS

$\cos(\alpha k_r^2)$ IS REAL, EVEN, AND LOWPASS. IT CORRESPONDS TO A REAL FILTER IN IMAGE SPACE. IT AFFECTS THE IN-PHASE COMPONENT.

$i \sin(\alpha k_r^2)$ IS IMAGINARY AND EVEN, AND BANDPASS. IT CORRESPONDS TO AN IMAGINARY FILTER IN IMAGE SPACE. THIS ROTATES THE PHASE SIGNAL TO THE REAL CHANNEL

IF WE INTENTIONALLY DEFOCUS, WE GET
 LOWPASS REAL COMPONENT FOR REFERENCE
 BANDPASS REAL COMPONENT
 (IMAGINARY PHASE). (IMAGINARY FILTER)

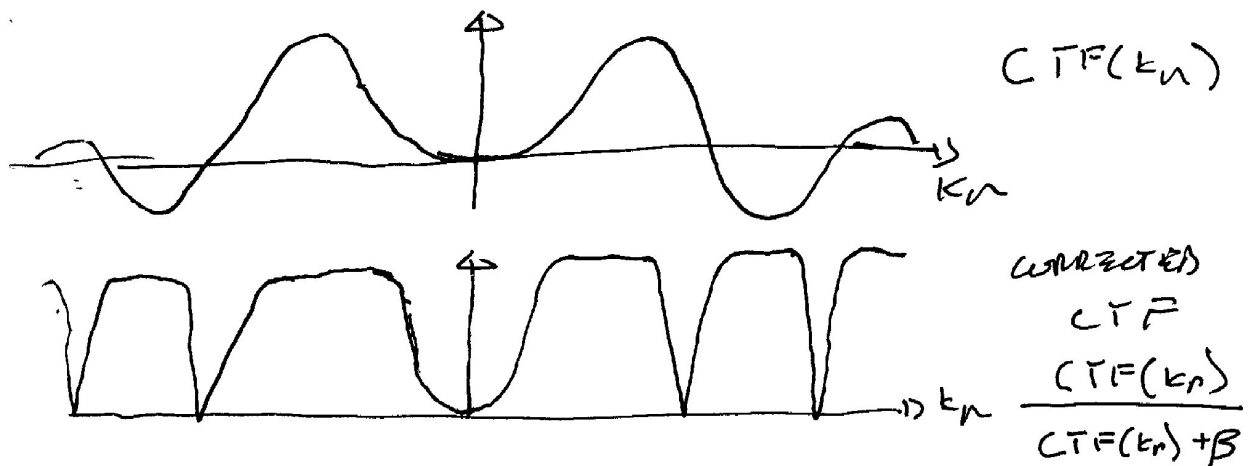
$$\begin{array}{l}
 \leftarrow \begin{array}{c} \text{BANDPASS} \\ \text{Im} \{ H(k_x) \} \end{array} \\
 \begin{array}{c} \text{LOWPASS} \\ \text{Re} \{ H(k_x) \} \end{array} \rightarrow
 \end{array}$$

THE INFORMATION WE CARE ABOUT IS THE IMAGINARY PHASE,
 WHICH SEES THE FILTER

$$CTF(k_x) = i \sin(\alpha k_x^2)$$

THIS IS THE CONTRAST TRANSFER FUNCTION. THIS
 IS APPLIED BEFORE INTENSITY DETECTION.

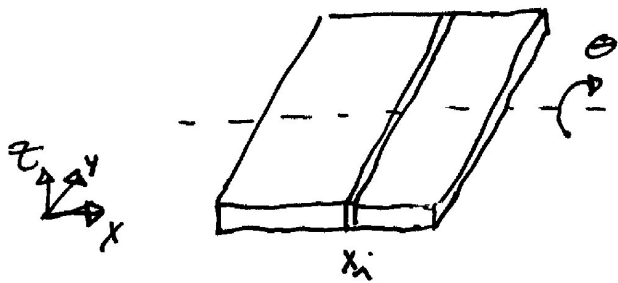
THE CTF IS BOTH POSITIVE AND NEGATIVE.
 IDEALLY WE'D LIKE IT TO BE ALL POSITIVE
 WE CAN CORRECT FOR THIS IN POST-PROCESSING



NOW ALL POSITIVE, NULLS AT ZEROS

THIS GIVES US MOST OF SPATIAL FREQUENCY EXCEPT
 DC, A FEW NULLS

TOMOGRAPHIC RECONSTRUCTION



THIN SLAB ROTATED ABOUT
X AXIS
EACH PROJECTION IS $\sim 4K \times 4K$
RECONSTRUCT ~ 100 SLICES
ANGLES FROM ± 60 DEGREES
AT 2° STEPS

TOMOGRAPHY PROBLEM

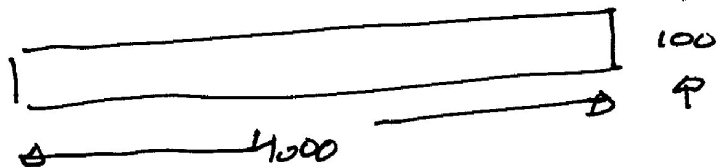
RAYS ARE PARALLEL

ROTATION ABOUT ONLY ONE AXIS

EACH POSITION x IS A SEPARATE 2D

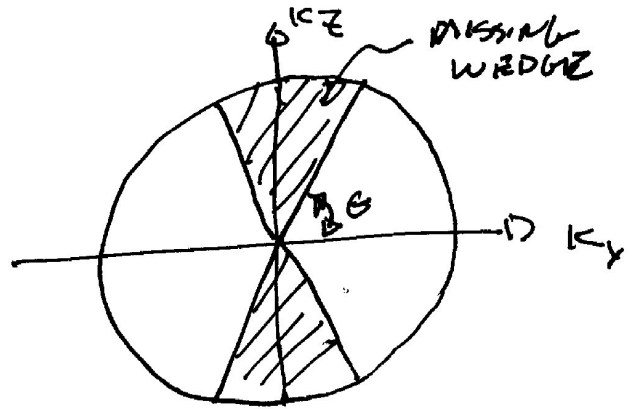
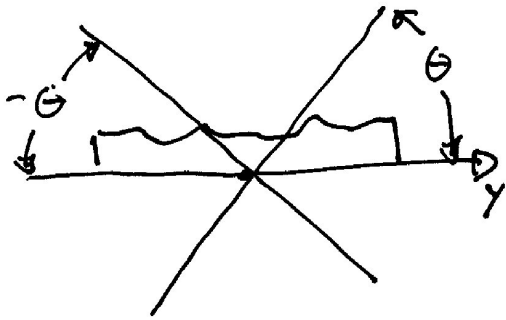
RECONSTRUCTION IN y AND z

GENERALLY SOLVED WITH FILTERING BASIC PROJECTION
EFFICIENT FOR VERY ASYMMETRIC FOV



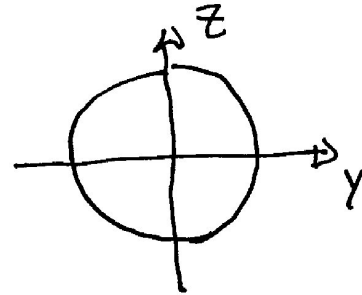
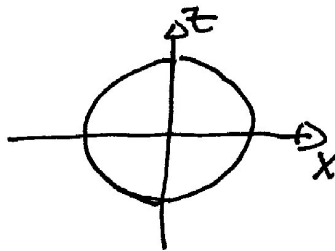
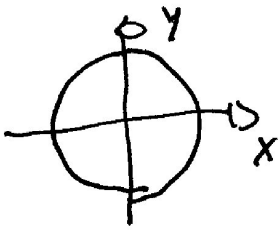
ONLY RECONSTRUCT THE VOXELS YOU WANT

LIMITED TILT ANGLES CAUSES ARTIFACTS

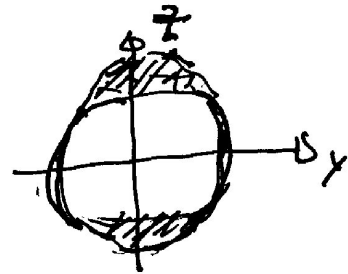
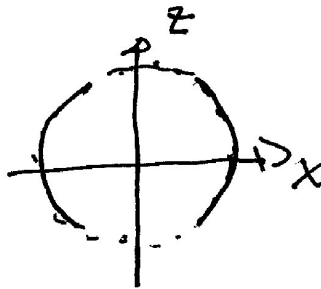
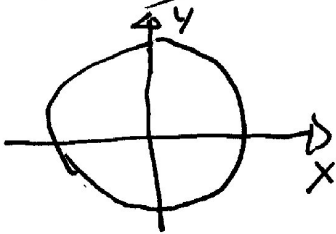


WE ARE MISSING HIGH SPATIAL FREQUENCIES IN Z
 IF WE RECONSTRUCT SLICES THROUGH A SPHERICAL SHELL

IDEAL



RECONSTRUCTED



THE X-Y PLANE LOOKS VERY GOOD, X-Z NOT TOO BAD,
 THE Y-Z PLANE HAS THE WORST ARTIFACTS