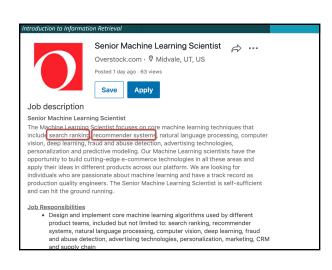
Introduction to Information Retrieval CS276: Information Retrieval and Web Search Christopher Manning and Pandu Nayak Lecture 14: Learning to Rank (with GBDTs) Borrows slides/pictures from Schigehiko Schamoni

Introduction to Information Retrieval

Sec. 15.4

Machine learning for IR ranking?

- We've looked at methods for ranking documents in IR
 - Cosine similarity, inverse document frequency, BM25, proximity, pivoted document length normalization, (will look at) Pagerank, ...
- We've looked at methods for classifying documents using supervised machine learning classifiers
 - Rocchio, kNN, decision trees, etc.
- Surely we can also use machine learning to rank the documents displayed in search results?
 - Sounds like a good idea
 - Known as "machine-learned relevance" or "learning to rank"



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Machine learning for IR ranking

- This "good idea" has been actively researched and actively deployed by major web search engines – in the last 10 years
- Why didn't it happen earlier?
 - Modern supervised ML has been around for about 25 years
 - Naïve Bayes has been around for about 60 years...

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Machine learning for IR ranking

- There's some truth to the fact that the IR community wasn't very connected to the ML community
- But there were a whole bunch of precursors:
 - Wong, S.K. et al. 1988. Linear structure in information retrieval. SIGIR 1988.
 - Fuhr, N. 1992. Probabilistic methods in information retrieval. Computer Journal.
 - Gey, F. C. 1994. Inferring probability of relevance using the method of logistic regression. SIGIR 1994.
 - Herbrich, R. et al. 2000. Large Margin Rank Boundaries for Ordinal Regression. Advances in Large Margin Classifiers.

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Why weren't early attempts very successful/influential?

- Sometimes an idea just takes time to be appreciated...
- Limited training data
 - Especially for real world use (as opposed to writing academic papers), it was very hard to gather test collection queries and relevance judgments that are representative of real user needs and judgments on documents returned
 - This has changed, both in academia and industry
- Poor machine learning techniques
- Insufficient customization to IR problem
- Not enough features for ML to show value

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Why wasn't ML much needed?

- Traditional ranking functions in IR used a very small number of features, e.g.,
 - Term frequency
 - Inverse document frequency
 - Document length
- It was easy possible to tune weighting coefficients by hand
 - And people did
 - You students do it in PA3

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Why is ML needed now?

- Modern (web) systems use a great number of features:
 - Arbitrary useful features not a single unified model
 - Log frequency of query word in anchor text?
 - Query word in color on pag
 - # of images on page?
 - # of (out) links on page?
 - PageRank of page?
 - URL length?
 - URL contains "~"
 - Page edit recency?
 - Page loading speed
- The New York Times in 2008-06-03 quoted Amit Singhal as saying Google was using over 200 such features ("signals") so it's sure to be over 500 today. ©

Simple example: Using classification for ad hoc IR Collect a training corpus of (q, d, r) triples Relevance r is here binary (but may be multiclass, with 3–7 values) Query-Document pair is represented by a feature vector • $\mathbf{x} = (\alpha, \omega)$ α is cosine similarity, ω is minimum guery window size ullet ω is the the shortest text span that includes all query words Query term proximity is an important new weighting factor Train a machine learning model to predict the class r of a documentquery pair example docID cosine score judgment query linux operating system penguin logo operating system runtime environment 0.032 relevant 0.02 nonrelevan 238 0.043 relevant Φ_3 Φ_4 Φ_5 Φ_6 Φ_7 nonrelevan 1741 kernel laver 0.022 relevant



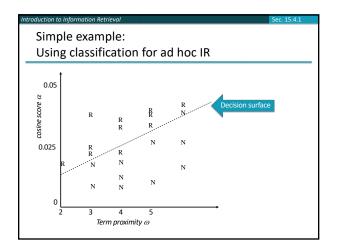
A linear score function is then

 $Score(d, q) = Score(\alpha, \omega) = a\alpha + b\omega + c$

And the linear classifier is

Decide relevant if $Score(d, q) > \theta$

... just like when we were doing text classification



More complex example of using classification for search ranking [Nallapati 2004]

- We can generalize this to classifier functions over more features
- We can use other methods for learning the linear classifier weights

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An SVM classifier for information retrieval [Nallapati 2004]

- Let relevance score $g(r|d,q) = \mathbf{w} \cdot f(d,q) + b$
- Uses SVM: want $g(r|d,q) \le -1$ for nonrelevant documents and $g(r|d,q) \ge 1$ for relevant documents
- SVM testing: decide relevant iff $g(r|d,q) \ge 0$
- Features are not word presence features (how would you deal with query words not in your training data?) but scores like the summed (log) tf of all query terms
- Unbalanced data (which can result in trivial always-saynonrelevant classifiers) is dealt with by undersampling nonrelevant documents during training (just take some at random)

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An SVM classifier for information retrieval [Nallapati 2004]

- Experiments:
 - 4 TREC data sets
 - Comparisons with Lemur, a state-of-the-art open source IR engine (Language Model (LM)-based – see IIR ch. 12)
 - Linear kernel normally best or almost as good as quadratic kernel, and so used in reported results
 - 6 features, all variants of tf, idf, and tf.idf scores

An SVM classifier for information retrieval [Nallapati 2004]

Train \ Test		Disk 3	Disk 4-5	WT10G (web)
TREC Disk 3	Lemur	0.1785	0.2503	0.2666
	SVM	0.1728	0.2432	0.2750
Disk 4-5	Lemur	0.1773	0.2516	0.2656
	SVM	0.1646	0.2355	0.2675

- At best the results are about equal to Lemur
 - Actually a little bit below
- Paper's advertisement: Easy to add more features
 - This is illustrated on a homepage finding task on WT10G:
 - Baseline Lemur 52% success@10, baseline SVM 58%
 - SVM with URL-depth, and in-link features: 78% success@10

"Learning to rank"

- Classification probably isn't the right way to think about approaching ad hoc IR:
 - Classification problems: Map to an unordered set of classes
 - Regression problems: Map to a real value [See PA3]
 - Ordinal regression (or "ranking") problems: Map to an ordered set of classes
 - A fairly obscure sub-branch of statistics, but what we want here
- This formulation gives extra power:
 - Relations between relevance levels are modeled
 - Documents are good versus other documents for a query given collection; not an absolute scale of goodness

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"Learning to rank"

- Assume a number of categories C of relevance exist
 - These are totally ordered: $c_1 < c_2 < ... < c_J$
 - This is the ordinal regression setup
- Assume training data is available consisting of documentquery pairs (d, q) represented as feature vectors x_i with relevance ranking c_i

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Algorithms used for ranking in search

- Support Vector Machines (Vapnik, 1995)
 - Adapted to ranking: Ranking SVM (Joachims 2002)
- Neural Nets: RankNet (Burges et al., 2006)
- Tree Ensembles
 - Random Forests (Breiman and Schapire, 2001)
 - Boosted Decision Trees
 - Multiple Additive Regression Trees (Friedman, 1999)
 - Gradient-boosted decision trees: LambdaMART (Burges, 2010)
 - Used by all search engines? AltaVista, Yahoo!, Bing, Yandex, ...
- All top teams in the 2010 Yahoo! Learning to Rank Challenge used combinations with Tree Ensembles!

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Yahoo! Learning to Rank Challenge

(Chapelle and Chang, 2011)

- Yahoo! Webscope dataset: 36,251 queries, 883k documents, 700 features, 5 ranking levels
 - Ratings: Perfect (navigational), Excellent, Good, Fair, Bad
 - Real web data from U.S. and "an Asian country"
 - set-1: 473,134 feature vectors; 519 features; 19,944 queries
 - set-2: 34,815 feature vectors; 596 features; 1,266 queries
- Winner (Burges et al.) was linear combo of 12 models:
 - 8 Tree Ensembles (LambdaMART)
 - 2 LambdaRank Neural Nets
 - 2 Logistic regression models

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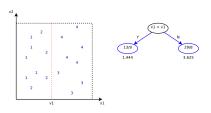
Regression trees

- Decision trees can predict a real value
 - They're then often called "regression trees"
- The value of a leaf node is the mean of all instances at the leaf $\gamma_k = f(x_i) = x_i$
- Splitting criterion: Standard Deviation Reduction
 - Choose split value to minimize the variance (standard deviation SD) of the values in each subset S_i of S induced by split A (normally just a binary split for easy search):
 - $SDR(A,S) = SD(S) \sum_{i} \frac{|S_i|}{|S|} SD(S_i)$
 - $SD = \sum_{i} (y_i f(x_i))^2$
- Termination: cutoff on SD or #examples or tree depth

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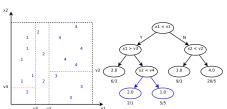
Training a regression tree

• The algorithm searches for split variables and split points, x_1 and v_1 so as to minimize the predicted error, i.e., $\sum_i (y_i - f(x_i))^2$.



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 You can grow tree till 0 error (if no identical points with different scores)



= 3d e.g.: http://arogozhnikov.github.io/2016/06/24/gradient_boosting_explained.html

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The concept of boosting

- Motivating question:
 - Can we use individually weak machine learning classifiers to build a high-accuracy classification system?
- Classic approach (AdaBoost)
 - Learn a small decision tree (often a 1-split decision stump)
 - It will get the biggest split in the data right
 - Repeat:
 - Upweight examples it gets wrong;
 - Downweight examples it gets right
 - Learn another small decision tree on that reweighted data
- Classify with weighted vote of all trees
 - Weight trees by individual accuracy

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Towards gradient boosting: Function estimation

- Want: a function F*(x) that maps x to y, s.t. the expected value of some loss function L(y, F(x)) is minimized:
 - $F^*(\mathbf{x}) = \arg\min_{F(\mathbf{x})} \mathbb{E}_{\mathbf{y},\mathbf{x}} L(\mathbf{y}, F(\mathbf{x}))$
- Boosting approximates $F^*(x)$ by an additive expansion
 - $F(\mathbf{x}) = \sum_{m=1}^{M} \beta_m h(\mathbf{x}; \mathbf{a}_m)$
- where h(x; a) are simple functions of x with parameters a = {a₁, a₂, ..., a_n} defining the function h, and the β are weighting coefficients

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Finding parameters

- Function parameters are iteratively fit to the training data:
 - Set F₀(x) = initial guess (or zero)
 - For each m = 1, 2, ..., M
 - $\quad \bullet \quad \boldsymbol{a}_m = \arg\min_{\boldsymbol{a}} \sum_i L(y_i, F_{m-1}(\boldsymbol{x}_i) + \beta h(\boldsymbol{x}_i, \boldsymbol{a}))$
 - $F_m(\mathbf{x}) = F_{m-1}(\mathbf{x}_i) + \beta h(\mathbf{x}_i, \mathbf{a})$
- You successively estimate and add a new tree to the sum
- You never go back to revisit past decisions

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Finding parameters

- Gradient boosting approximately achieves this for any differentiable loss function
 - Fit the function h(x; a) by least squares
 - $\boldsymbol{a}_m = \operatorname{arg\,min}_a \sum_i [\tilde{y}_{im} h(\boldsymbol{x}_i, \boldsymbol{a})]^2$
 - to the "pseudo-residuals" (deviation from desired scores)

$$\tilde{y}_{im} = -\left[\frac{\partial L(y_i, F(x_i))}{\partial F(x_i)}\right]_{F(x) = F_{m-1}(x)}$$

- Whatever the loss function, gradient boosting simplifies the problem to least squares estimation!!!
 - We can take a gradient (Newton) step to improve model

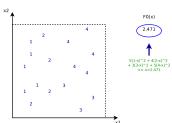
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Gradient tree boosting

- Gradient tree boosting applies this approach on functions h(x; a) which are small regression trees
 - The trees used normally have 1-8 splits only
 - Sometimes stumps do best!
 - The allowed depth of the tree controls the feature interaction order of model (do you allow feature pair conjunctions, feature triple conjunctions, etc.?)

Learning a gradient-boosted regression tree

 First, learn the simplest predictor that predicts a constant value that minimizes the error on the training data



Learning a gradient-boosted regression

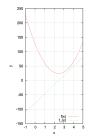
• We want to find value γ_{km} for root node of tree

Quadratic loss for the leaf (red):

$$f(x) = 5 \cdot (1-x)^2 + 4 \cdot (2-x)^2 + 3 \cdot (3-x)^2 + 5 \cdot (4-x)^2$$

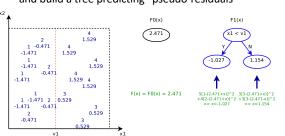
f(x) is quadratic, *convex* \Rightarrow Optimum at f'(x) = 0 (green)

$$\frac{\partial f(x)}{\partial x} = 5 \cdot (-2 + 2x) + 4 \cdot (-4 + 2x)^2 + 3 \cdot (-6 + 2x)^2 + 5 \cdot (-8 + 2x)^2 = -84 + 34x = 34(x - 2.471)$$



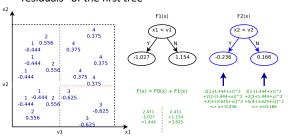
Learning a gradient-boosted regression tree

We split root node based on least squares criterion and build a tree predicting "pseudo-residuals"



Learning a gradient-boosted regression tree

 Then another tree is added to fit the actual "pseudoresiduals" of the first tree



Multiple Additive Regression Trees (MART) [Friedman 1999]

Algorithm 1 Multiple Additive Regression Trees.

1: Initialize
$$F_0(\mathbf{x}) = \arg\min_{\gamma} \sum_{i=1}^N L(y_i, \gamma)$$

2: $\mathbf{for} \ m = 1, ..., M \ \mathbf{do}$
3: $\mathbf{for} \ i = 1, ..., M \ \mathbf{do}$
4: $\widetilde{y}_{im} = -\left[\frac{\partial L(y_i, F(\mathbf{x}_i))}{\partial F(\mathbf{x}_i)}\right]_{F(\mathbf{x}) = F_{m-1}(\mathbf{x})}$
5: $\mathbf{end} \ \mathbf{for}$
6: $\left\{R_{km}\right\}_{k=1}^K //$ Fit a regression tree to targets \widetilde{y}_{im}
7: $\mathbf{for} \ k = 1, ..., K_m \ \mathbf{do}$
8: $\gamma_{km} = \arg\min_{\gamma} \sum_{x_i \in R_{jm}} L(y_i, F_{m-1}(\mathbf{x}_i) + \gamma)$
9: $\mathbf{end} \ \mathbf{for}$
10: $F_m(\mathbf{x}) = F_{m-1}(\mathbf{x}) + \eta \sum_{k=1}^{K_m} \gamma_{km} \mathbf{1}(\mathbf{x}_i \in R_{km})$
11: $\mathbf{end} \ \mathbf{for}$
12: Return $F_M(\mathbf{x})$

Historical path to LambdaMART: via RankNet (a neural net ranker)

- \blacksquare Have differentiable function with model parameters $\boldsymbol{w} :$
 - $x_i \rightarrow f(x; w) = s_i$
- For query q, learn probability of different ranking class for documents $d_i > d_i$ via:

•
$$P_{ij} = P(d_i > d_j) = \frac{1}{1 + e^{-\sigma(s_i - s_j)}}$$

Cost function calculates cross entropy loss:

•
$$C = -P_{ij} \log P_{ij} - (1 - P_{ij}) \log(1 - P_{ij})$$

 Where P_{ij} is the model probability; P_{ij} the actual probability (0 or 1 for categorical judgments)

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RankNet (Burges 2010)

Combining these equations gives

•
$$C = \frac{1}{2}(1 - S_{ij})\sigma(s_i - s_j) + \log(1 + e^{-\sigma(s_i - s_j)})$$

• where, for a given query, $S_{ij} \in \{0, +1, -1\}$ 1 if d_i is more relevant than d_j ; -1 if the reverse, and 0 if the they have the same label

$$\begin{split} \bullet & \frac{\partial \mathcal{C}}{\partial s_{i}} = \sigma\left(\frac{1}{2}\left(1 - S_{ij}\right) - \frac{1}{1 + e^{\sigma(s_{i} - s_{j})}}\right) = -\frac{\partial \mathcal{C}}{\partial s_{j}} \\ & \frac{\partial \mathcal{C}}{\partial w_{k}} = \frac{\partial \mathcal{C}}{\partial s_{i}} \frac{\partial s_{i}}{\partial w_{k}} + \frac{\partial \mathcal{C}}{\partial s_{j}} \frac{\partial s_{j}}{\partial w_{k}} = \sigma\left(\frac{1}{2}(1 - S_{ij}) - \frac{1}{1 + e^{\sigma(s_{i} - s_{j})}}\right) \left(\frac{\partial s_{i}}{\partial w_{k}} - \frac{\partial s_{j}}{\partial w_{k}}\right) \\ & = \lambda_{ij} \left(\frac{\partial s_{i}}{\partial w_{k}} - \frac{\partial s_{j}}{\partial w_{k}}\right) \end{split}$$

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RankNet lambdas

The crucial part of the update is

$$\frac{\partial C}{\partial w_k} = \frac{\partial C}{\partial s_i} \frac{\partial s_i}{\partial w_k} + \frac{\partial C}{\partial s_j} \frac{\partial s_j}{\partial w_k} = \lambda_{ij} \left(\frac{\partial s_i}{\partial w_k} - \frac{\partial s_j}{\partial w_k} \right)$$

- \(\lambda_{ij}\) describes the desired change of scores for the pair of documents \(d_i\) and \(d_i\)
- The sum of all λ_{ij} 's and λ_{ji} 's of a query-doc vector x_i w.r.t. all other differently labelled documents for q is

$$\lambda_i = \sum_{j:\{i,j\}\in I} \lambda_{ij} - \sum_{k:\{k,i\}\in I} \lambda_{ki}$$

• λ_i is (sort of) a gradient of the pairwise loss of vector x_i

.

RankNet lambdas (Burges 2010)

 (a) is the perfect ranking, (b) is a ranking with 10 pairwise errors, (c) is a ranking with 8 pairwise errors. Each blue arrow represents the λ_i for each query-document vector x_i



RankNet lambdas (Burges 2010) Problem: RankNet is based on pairwise error, while modern IR measures emphasize higher ranking positions. Red arrows show better \(\lambda\)'s for modern IR, esp. web search.

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From RankNet to LambdaRank

- Rather than working with pairwise ranking errors, scale by effect a change has on NDCG
- Idea: Multiply λ 's by $|\Delta Z|$, the difference of an IR measure when d_i and d_j are swapped
- E.g. |ΔNDCG| is the change in NDCG when swapping d_i and d_j giving:

•
$$\lambda_{ij} = \frac{\partial C(s_i - s_j)}{\partial s_i} = \frac{-\sigma}{1 + e^{\sigma(s_i - s_j)}} |\Delta \text{NDCG}|$$

 Burges et al. "prove" (partly theory, partly empirical) that this change is sufficient for model to optimize NDCG

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From LambdaRank to LambdaMART

- LambdaRank models gradients
- MART can be trained with gradients ("gradient boosting")
- Combine both to get LambdaMART
 - MART with specified gradients and optimization step

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LambdaMART algorithm

set number of trees N, number of training samples m, number of leaves per tree L, learning rate η for i=0 to m do

 $F_0(x_i) = \operatorname{BaseModel}(x_i)$ //If BaseModel is empty, set $F_0(x_i) = 0$ end for

 $\mathbf{for}\ k = 1\ \mathrm{to}\ N\ \mathbf{do}$ $\mathbf{for}\ i = 0\ \mathrm{to}\ m\ \mathbf{do}$

 $y_i = \lambda_i$ $w_i = \frac{\partial y_i}{\partial F_{k-1}(x_i)}$ end for

 $\{R_{lk}\}_{l=1}^{L}$ // Create L leaf tree on $\{x_i, y_i\}_{i=1}^{m}$ R_{lk} is data items at leaf node l

 $\gamma_{lk} = \frac{\sum_{x_i \in R_{lk}} y_i}{\sum_{x_i \in R_{lk}} w_i}$ // Assign leaf values based on Newton step.

 $F_k(x_i)=F_{k-1}(x_i)+\eta\sum_l\gamma_{lk}I(x_i\in R_{lk})$ // Take step with learning rate η . end for

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Yahoo! Learning to rank challenge

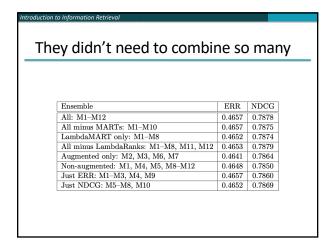
- Goal was to validate learning to rank methods on a large, "real" web search problem
 - Previous work was mainly driven by LETOR datasets
 - Great as first public learning-to-rank data
 - Small: 10s of features, 100s of queries, 10k's of docs
- Only feature vectors released
 - Not URLs, queries, nor feature descriptions
 - Wanting to keep privacy and proprietary info safe
 - But included web graph features, click features, page freshness and page classification features as well as text match features

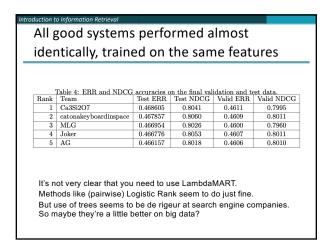
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Burges et al. (2011) entry systems

Model	Description	ERR	NDCG
M1	LambdaMART optimized for ERR	0.461	0.774
M2	LambdaMART optimized for ERR trained on Aug50	0.464	0.786
M3	LambdaMART optimized for ERR trained on Aug70	0.462	0.780
M4	LambdaMART trained for ERR with MART scores as features	0.460	0.775
M5	LambdaMART optimized for NDCG	0.462	0.779
M6	LambdaMART optimized for NDCG trained on Aug50	0.464	0.787
M7	LambdaMART optimized for NDCG trained on Aug70	0.463	0.783
M8	LambdaMART trained for NDCG with MART scores as features	0.461	0.781
M9	LambdaRank optimized for ERR	0.453	0.750
M10	LambdaRank optimized for NDCG	0.453	0.757
M11	MART	0.455	0.772
M12	MART with output scores normalized to unit variance per query	0.455	0.772

ERR = Expected reciprocal rank; see Chapelle and Chang (2011)



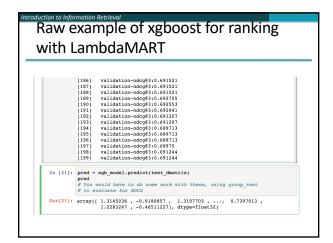


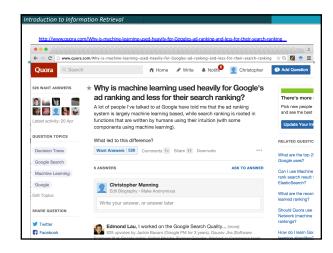
Raw example of xgboost for ranking with LambdaMART

- https://github.com/dmlc/xgboost/tree/master/demo/rank
- git clone https://github.com/dmlc/xgboost.git
- brew install unrar #somehow get unrar if don't have it
- cd gboost/demo/rank
- ./wgetdata.sh # gets one of the LETOR datasets
- python notebook

```
Raw example of xgboost for ranking with LambdaMART

In [1]: import xgboost as xgb from xgboost from xgboost from xgboost from xgboost import DMatrix xgboost import DMatrix xgboost xgboos
```





Summary

- The idea of learning ranking functions has been around for about 20 years
- But only more recently have ML knowledge, availability of training datasets, a rich space of features, and massive computation come together to make this a hot research
- It's too early to give a definitive statement on what methods are best in this area
- But machine-learned ranking over many features now easily beats traditional hand-designed ranking functions in comparative evaluations [in part by using the hand-designed functions as features!]
- There is every reason to think that the importance of machine learning in IR will grow in the future.

Resources

- IIR secs 6.1.2–3 and 15.4
- Nallapati, R. Discriminative models for information retrieval. SIGIR 2004.
- LETOR benchmark datasets
 - Website with data, links to papers, benchmarks, etc.
 - http://research.microsoft.com/users/LETOR/
 - Everything you need to start research in this area! But smallish.
- C. J. C. Burges. From RankNet to LambdaRank to LambdaMART: An Overview. Microsoft TR 2010.
- O. Chapelle and Y. Chang. Yahoo! Learning to Rank Challenge Overview. JMLR Proceedings 2011.