

Sharing Chocolate

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Consider a chocolate bar consisting of 3×4 segments. You can break the chocolate bar along any of the divisions between the rows or columns of the bar, creating two bars that themselves can be recursively split in the same manner.

A specific question: Can the 3×4 chocolate bar be split into 4 pieces with 1, 2, 3, and 6 segments? The more general question: Can an m by n chocolate bar ($1 \leq m, n \leq 100$) be split into p pieces ($1 \leq p \leq 15$) with $a_1, a_2, a_3, \dots, a_{p-1},$ and a_p segments?

The problem can be solved using recursive backtracking and memoization, and while challenging, it's accessible to everyone, since we've covered both topics in lecture. It's possible to use recursive backtracking alone, but the memoization can be used to remember common sub-problems and bring an exponential running time solution down to a polynomial one. Even 100×100 chocolate bars can be recursively divided to discover the desired split in less than a second.

Input

The data needs to be read in from a file named **sharing-chocolate.in**. The input file consists of multiple test cases, each describing a chocolate bar. Each description starts with a line containing two integers, which are the dimensions of a chocolate bar. The next line contains a list of (unsorted) integers, which are the sizes of the segments. The end of input is the end of file (i.e. an attempt to read two integers would bring an **ifstream** into a fail state.)

Output

For each test case, simply output "yes" or "no", one per line with no additional white space. Naturally, print "yes" if the desired split is possible, and print "no" otherwise.

Sample Input:

```
3 4
1 2 3 6
5 5
6 4 9 6
2 3
1 5
```

Sample Output:

```
yes
yes
no
```