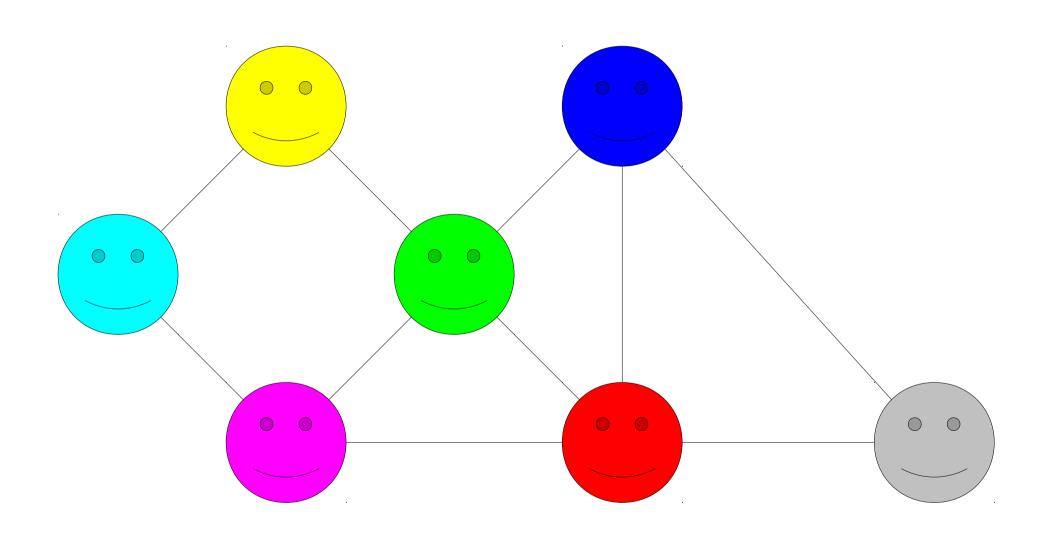
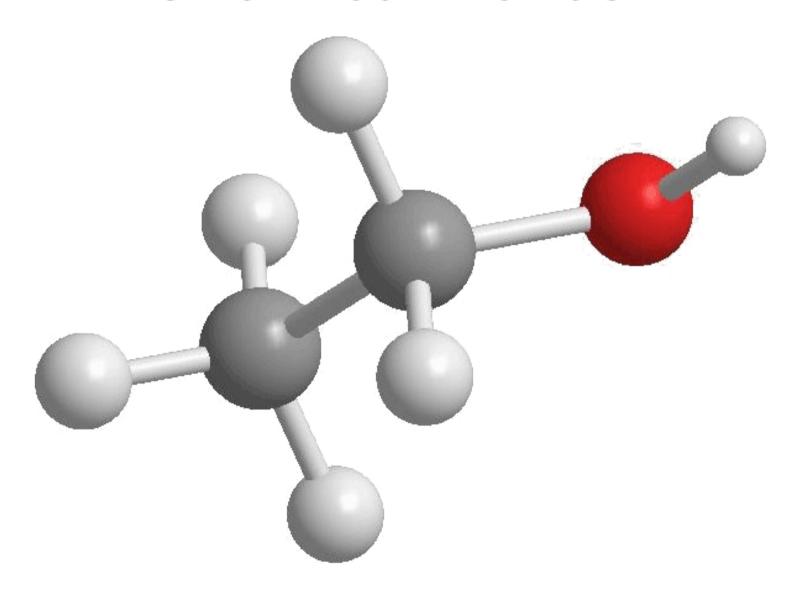
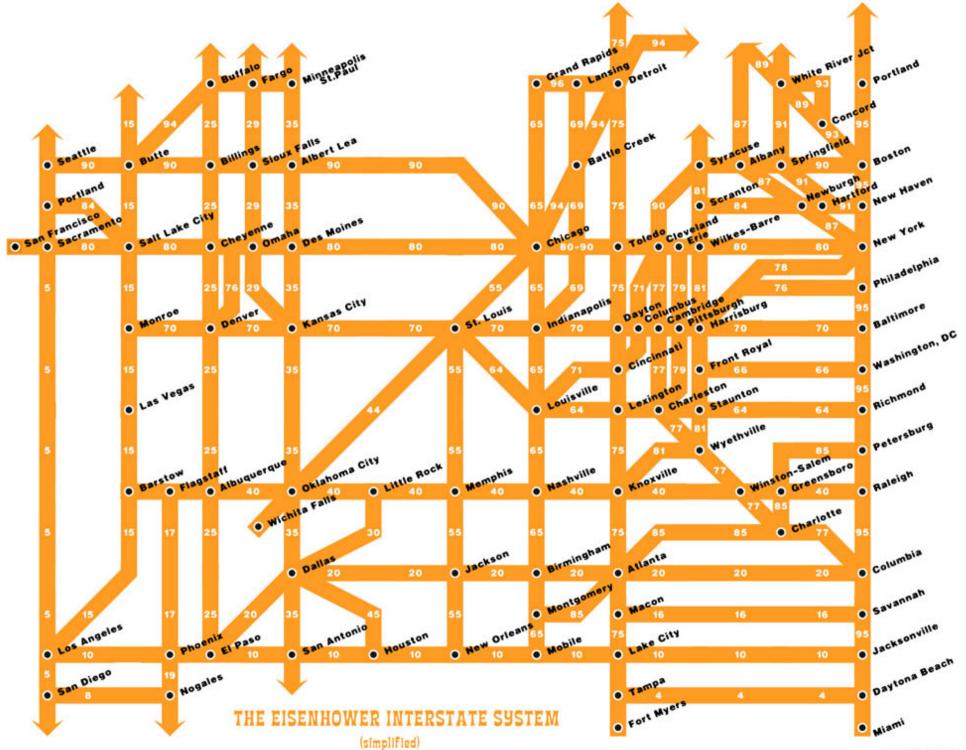
Graphs

A Social Network

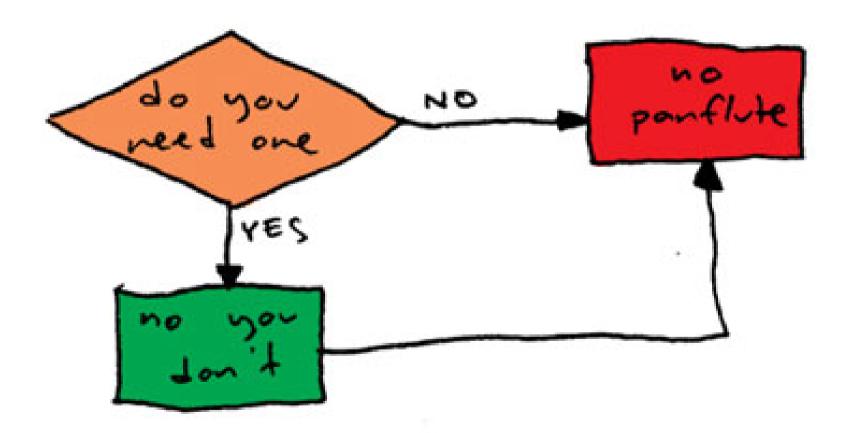


Chemical Bonds

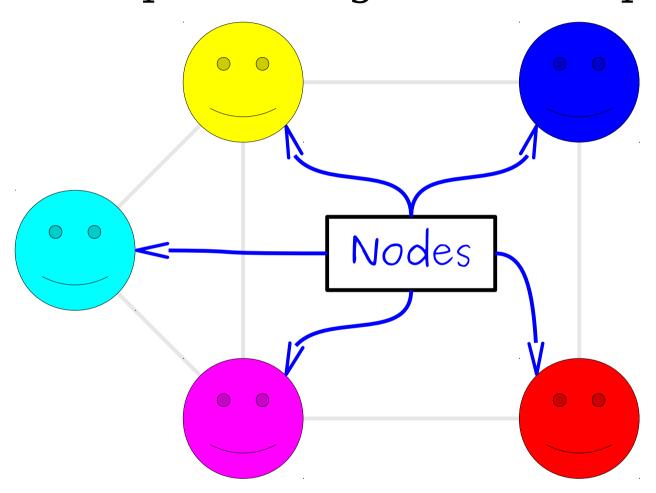




PANFLUTE FLOWCHART

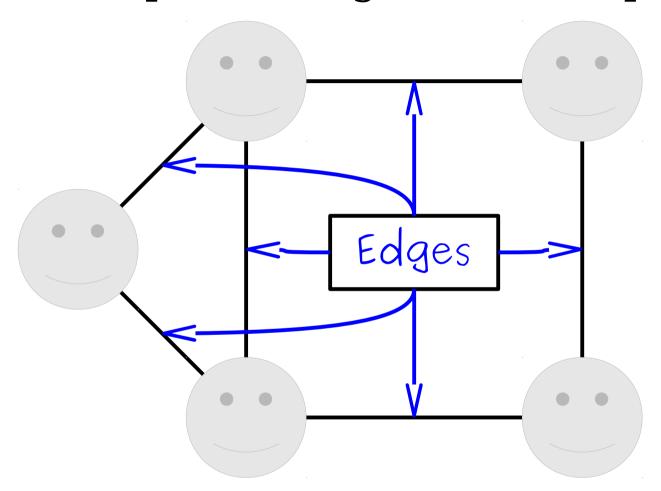


A *graph* is a mathematical structure for representing relationships.



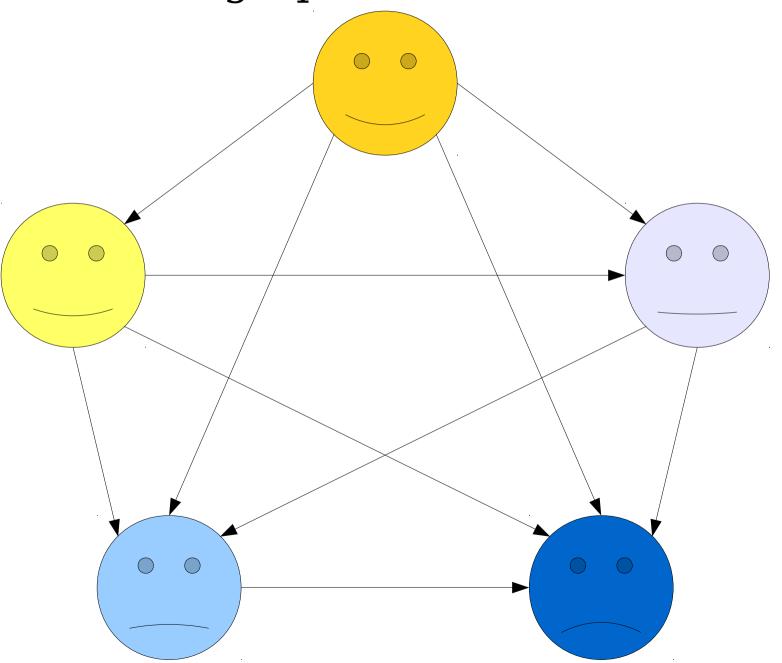
A graph consists of a set of **nodes** connected by **edges**.

A *graph* is a mathematical structure for representing relationships.

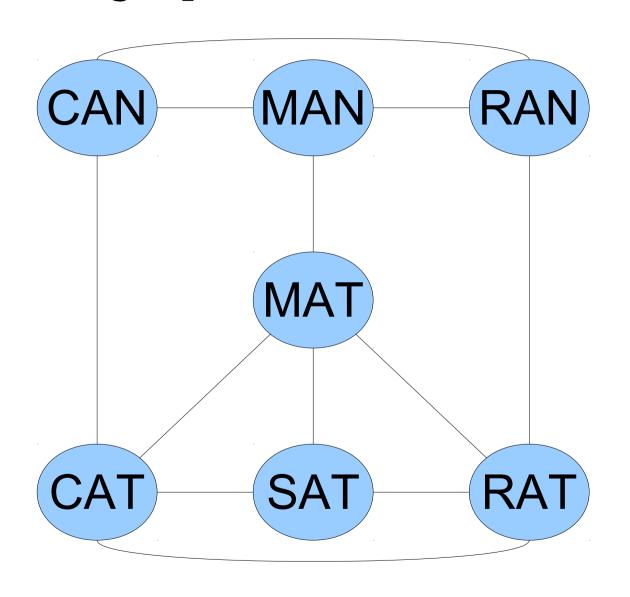


A graph consists of a set of **nodes** connected by **edges**.

Some graphs are *directed*.



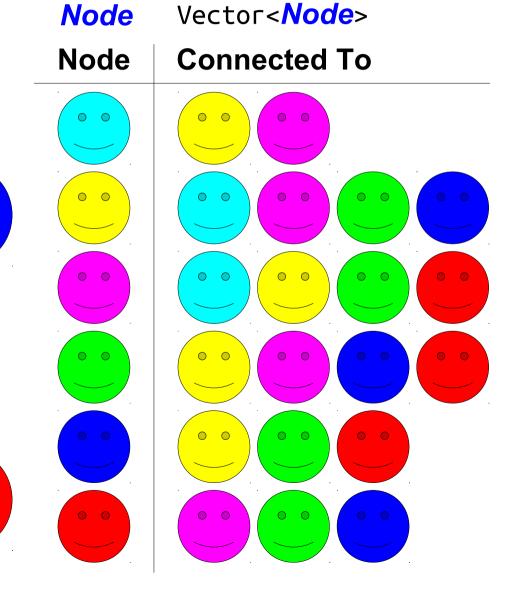
Some graphs are *undirected*.



How can we represent graphs in C++?

Representing Graphs

We can represent a graph as a map from nodes to the list of nodes each node is connected to.



Map<Node, Vector<Node>>

Representing Graphs

 The approach we just saw is called an *adjacency list* in comes in a number of different forms:

Map<string, Vector<string>>
 Map<string, Set<string>>
HashMap<string, HashSet<string>>
 Vector<Vector<int>>

 The core idea is that we have some kind of mapping associating each node with its outgoing edges.

Representing Graphs

The approach we just saw is called an *adjacency list* in comes in a number of different forms:

Map<string, Vector<string>>

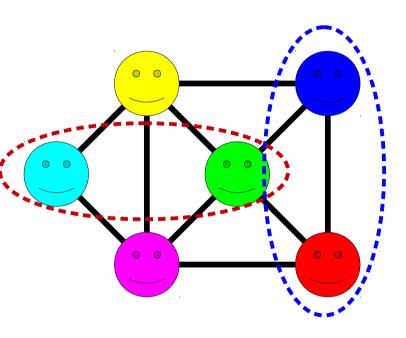
Map<string, Set<string>>

HashMap<string, Question to ponder:

Where have you seen this before?

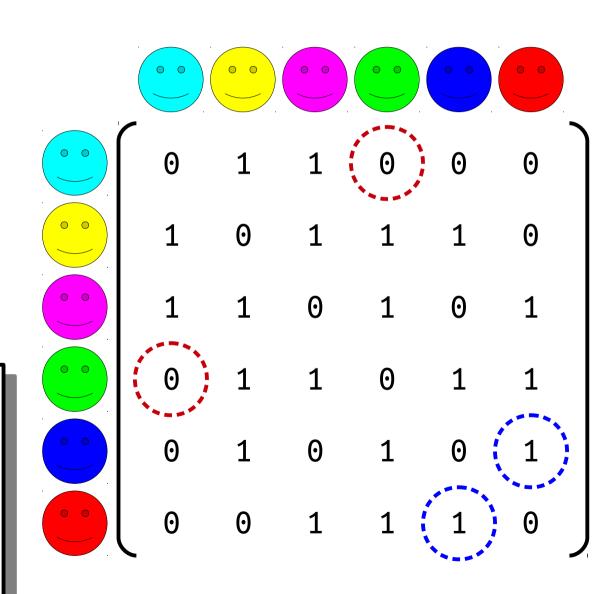
The core idea is that we have some kind of mapping associating each node with its outgoing edges.

Other Graph Representations

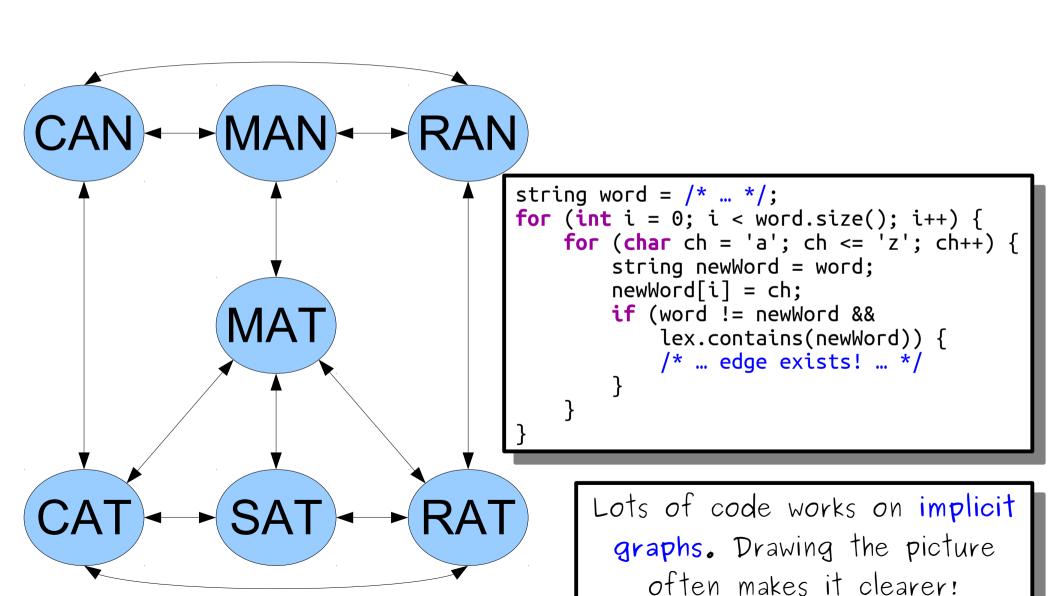


This representation is called an adjacency matrix.

For those of you in Math 51: if A is an adjacency matrix for a graph G, what is the significance of the matrix A²?



Other Representations



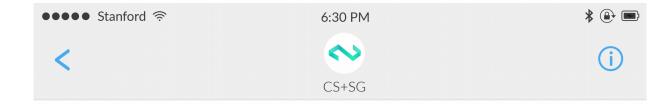
You'll find graphs just about everywhere you look.

They're an *extremely* versatile and powerful abstraction to be aware of.

Time-Out for Announcements!

Assignment 6

- Assignment 6 is due this Friday.
- Have questions?
 - Stop by the LaIR!
 - Ask your section leader!
 - Stop by Keith's office hours on Tuesday!
 - Stop by Anton's office hours on Wednesday!
 - Ask on Piazza!



CS+SOCIAL GOOD MIXER

Black Community Services Center

March 8th, 6:30-8:00pm

Mingle with your fellow students and faculty for a night of conversation about social good issues.

Tasty snacks & light refreshments will be served!





Stanford Engineers for a Sustainable World is looking for a team member to travel to Indonesia for a 9 week fellowship this summer to work with rural development NGO IBEKA.

This is the fourth year of Engineers for a Sustainable World's collaboration with IBEKA on an Internet of Things Remote Monitoring System for Micro-hydroelectric Plants. Learn more about the project here.

We are looking for students of any year with skills and interests in Electrical Engineering, Computer Science, and Product Design. Participation requires enrolling in CEE177S Spring Quarter.

If interested, please email <u>riyav@stanford.edu</u> with a short paragraph explaining your interest and qualifications.

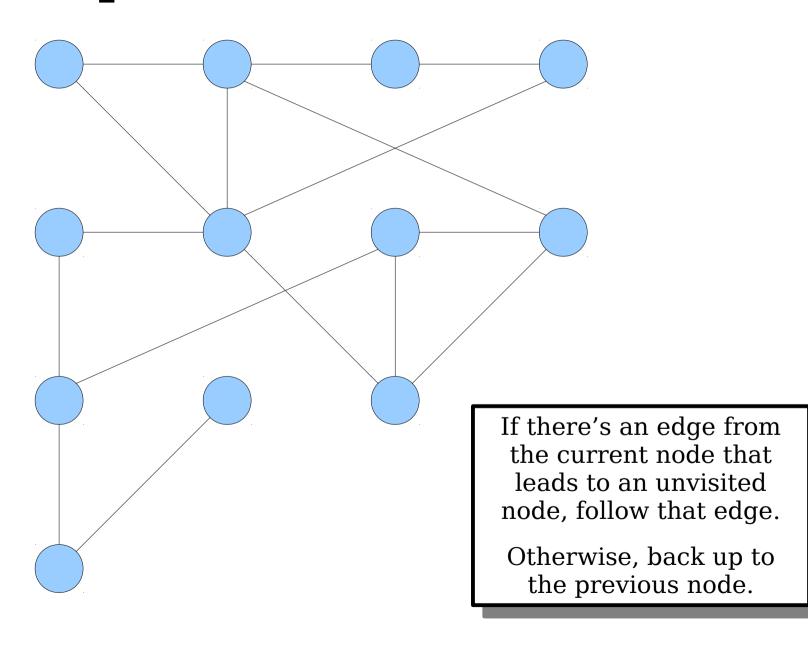
Back to CS106B!

Traversing Graphs

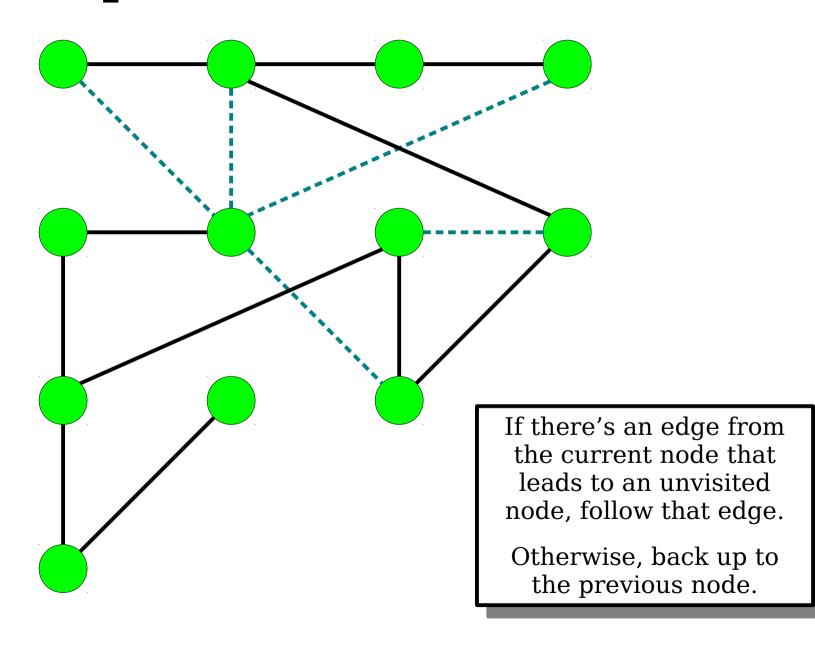
Iterating over a Graph

- In a singly-linked list, there's pretty much one way to iterate over the list: start at the front and go forward!
- In a binary search tree, there are many traversal strategies:
 - An *inorder traversal* that produces all the elements in sorted order.
 - A *postorder traversal* used to delete all the nodes in the BST.
- There are *many* ways to iterate over a graph, each of which have different properties.

Depth-First Search



Depth-First Search



DFS: The Rundown

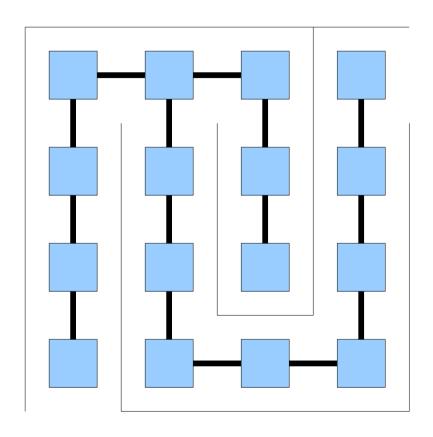
- Starting a DFS at a given node will find all nodes *reachable* from that node.
- If you have an adjacency list, doing a DFS in an n-node, m-edge graph takes time O(m + n) and uses space O(n).
 - Talk to me after class for details!
- There are some **beautiful** properties of the order in which DFS visits nodes (take CS161!), but until you know them the order of nodes found can look pretty random. Come talk to me after class for more info.

Depth-First Search

- To do a depth-first search (DFS) from a node u, do the following:
 - If *u* isn't *gray* (unvisited), stop.
 - Color *u yellow* (active).
 - For each neighbor *v* of *u*:
 - Recursively run DFS from ν .
 - Color *u green* (done).
- The code for DFS is amazingly short!

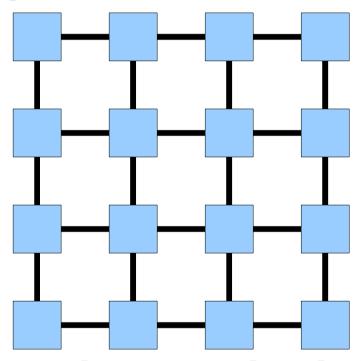
A Whimsical Application

Mazes as Graphs



Creating a Maze with DFS

• Create a *grid graph* of the appropriate size.

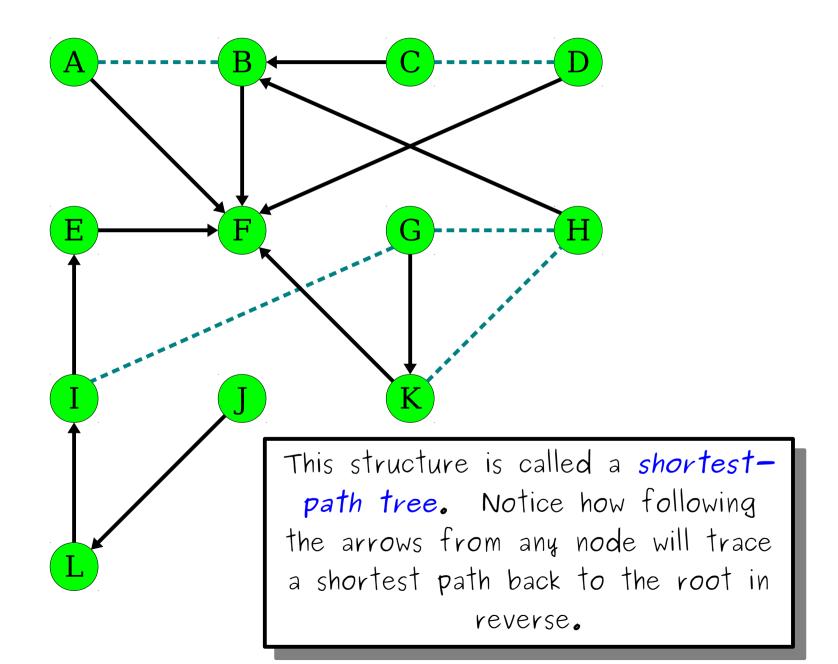


- Starting at any node, run a depth-first search, choosing neighbor orderings at random.
- The resulting DFS tree is a maze with one solution.

Breadth-First Search

How do you find the fastest route from one point to another?

Breadth-First Search



BFS: The Rundown

- Breadth-first search will find all nodes reachable from the starting node.
- It will visit them in *increasing* order of distance.
- In an n-node, m-edge graph, it takes time O(m + n) and uses space O(n).
 - Though in practice, the space usage is much higher than in DFS.
 - Curious where this runtime comes from?
 Come talk to me after class!

BFS: The Logic

- Color all nodes gray.
- Make a worklist with the starting node.
- Color the starting node yellow.
- While the worklist isn't empty:
 - Dequeue a node from the worklist.
 - Color that node green.
 - For each adjacent node:
 - If that node is *gray*:
 - Color the node yellow.
 - Add it to the queue.

Next Time

• Shortest Paths

- Dijkstra's Algorithm.
- Shortest-Path Trees
- A* Search.